

Recent experimental results on charge exchange reactions with VES setup at U-70

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Outline

- **Introductory remarks**
- **VES experiment: scope, methods, setup**
- **The glueball candidate $f_0(1710)$ in the $\omega\phi$ system**
- **The first study of the $\eta'\pi^+\pi^-$ system in charge-exchange reaction**
- **Conclusion**

Intro

- Pomeron exchange dominates at high energy hadron scattering
 - Yet other Regge trajectories contribute at U-70 energy range
 - Different t-channel exchanges are similar in peripheral character =>
common experimental approaches/apparatus
 - BUT: different objects accessible
- Experimental studies with these two are complementary

Scope of the VES experiment

Light mesons spectroscopy

- **New resonances incl. Exotics**
- **New decay channels**
- **Production mechanism studies**
- **Form-factors**

Method

- (Quasy)Exclusive production of systems of mesons with nuclear target
- (Kind of) Partial Wave Analyses (PWA) for quantum numbers of structures
- Cross-section measurements (recently started)

For a system X on a thin target

N_X^{obs} – number of registered events of the system under study

ε – overall efficiency (from modelling)

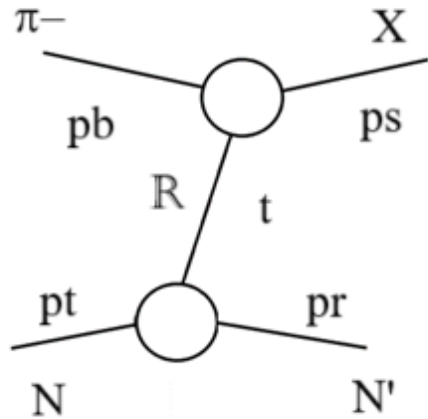
N_{beam} – number of beam particles through the target with **nuclei** concentration n and of length L

A.A.Shumakov. The Methods of Measuring the Cross Sections of the Reactions in the VES Experiment.

Physics of Particles and Nuclei 56 (2025) 3, pp. 662–667

$$\sigma_X = \frac{N_X^{\text{obs}}}{\varepsilon_X N_{\text{beam}} nL}$$

Sketch of a reaction under study



X = dedicated system of mesons

($\omega\phi$, $\eta'\pi^+\pi^-$ -- cases of this report)

Target = A, N

Recoil = A', N, N^*, Δ not detected directly

Target fragmentation **suppressed** with VETO

Missing mass squared mm^2 related to recoil

Momentum transferred squared t related to t-channel exchange

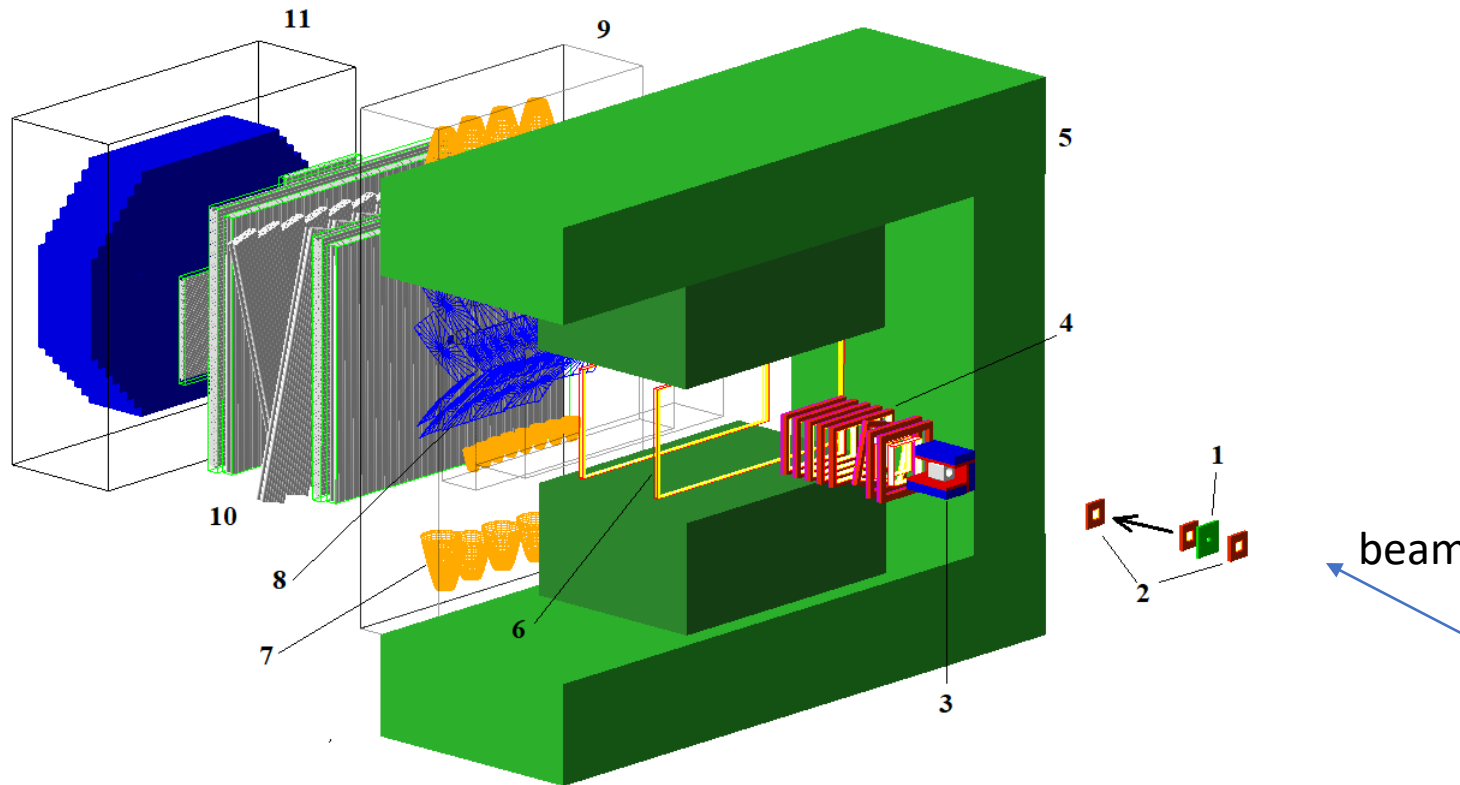
R = P or other Reggeon, mostly OPE

$$mm^2 = (p_{beam} + p_{target} - p_{system})^2$$

$$t = (p_{beam} - p_{system})^2 = (p_{recoil} - p_{target})^2$$

$$t' = |t| - |t|_{min}$$

Updated VES setup



1 - last beam counter; 2- beam proportional chambers; 3 – target veto; 4 – proportional chambers; 5- main magnet; 6 - drift chambers; 7 - light collectors, 8 - mirrors, and 9 - body of the Cherenkov counter; 10 – drift tubes; 11 - electromagnetic calorimeter.

Trigger components:

Beam particle to target

$$BEAM = S1 \cdot S2 \cdot S3 \cdot \overline{(A10 + A11)}$$

Beam particle disappearance after target
== beam fragmentation

$$MWG = BEAM \cdot \overline{(BK1 + BK2)}$$

No target veto response
== interaction w/o target fragmentation

$$MAIN = MWG \cdot \overline{(VETO)}$$

Major characteristics of the setup

- Secondary beam $\sim 2 \cdot 10^6/\text{s}$; $p=29 \text{ GeV}$, $dp \sim \pm 1\%$; 98% π^- , 1.6% K^- , 0.2% $\bar{p}$
- Beam spectrometer with 0.7% accuracy
- Target: ^9Be $D=45 \text{ mm}$, $L=40 \text{ mm}$
- Target Veto with crude segmentation for charged and neutral particles
- Main magnet: $H \times V \sim 2 \times 1 \text{ m}^2$, $\int B \, dL \sim 1.5 \text{ T} \cdot \text{m}$
- Tracking Spectrometer: 0.5% (1.2%) @3 GeV (@25 GeV)
- Good transparency for γ : $< 15\% X_0$ before the EM-calorimeter
- EMC: resolution @5 Γ_{EB} 4% (E) and 3.2 mm (X)

Typical events selection

- Trigger by choice
- Good status of reconstruction
- Beam through target and with momentum measured (ID optional)
- Final state topology according to system under study (PID optional) w/o debris of tracks and/or gammas
- Primary vertex within target (secondary optional)
- Total momentum of reconstructed particles close to beam momentum
- Narrow signal(s) in inv. masses of subsystem(s) if applicable (π^0 , η , η' , ω , ϕ , $K_s \dots$)

Study of a scalar resonance in the $\omega\phi$ system in pion-Be interaction at momentum 29 GeV

Eur.Phys.J.A 60 (2024) 5, 105

Scalar mesons $J^{PC} = 0^{++}$

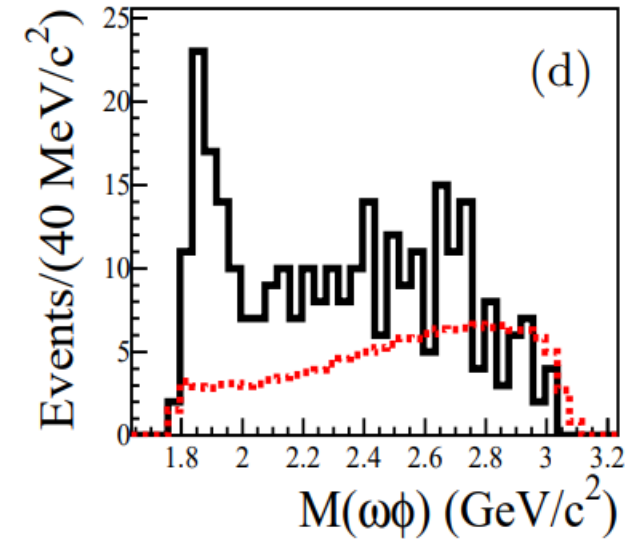
- Light scalars: uncertainty and redundancy in the $SU(3)_{\text{flavor}}$ multiplet filling
($M = 500; 980; 1500; 1710; \dots$ MeV)
- Diversity of theoretical models (molecule, 4 - quark, glueball...)

Mass range of 1700 – 1800 MeV:

- $I^G J^{PC} = 0^+ 0^{++}$ signals in various reactions
- One of major sources: $J/\psi \rightarrow \gamma f_0$
- PDG: $f_0(1710)$ $M = 1733^{+8}_{-7}$ MeV, $\Gamma = 150 \pm 12$ MeV
- $\text{Br}(J/\psi \rightarrow \gamma f_0(1710)) > \text{than for others } f_0$
 $\hookrightarrow (4\pi, K K, \pi\pi, \omega\phi, \omega\omega)$

Channel $\omega(783) \phi(1020)$

BES: $e^+e^- \rightarrow J/\psi \rightarrow \gamma \omega(783) \phi(1020)$
Ablikim, M., et al. . Phys. Rev. Lett. 96, 162002 (2006)
<https://arxiv.org/abs/hep-ex/0602031>.



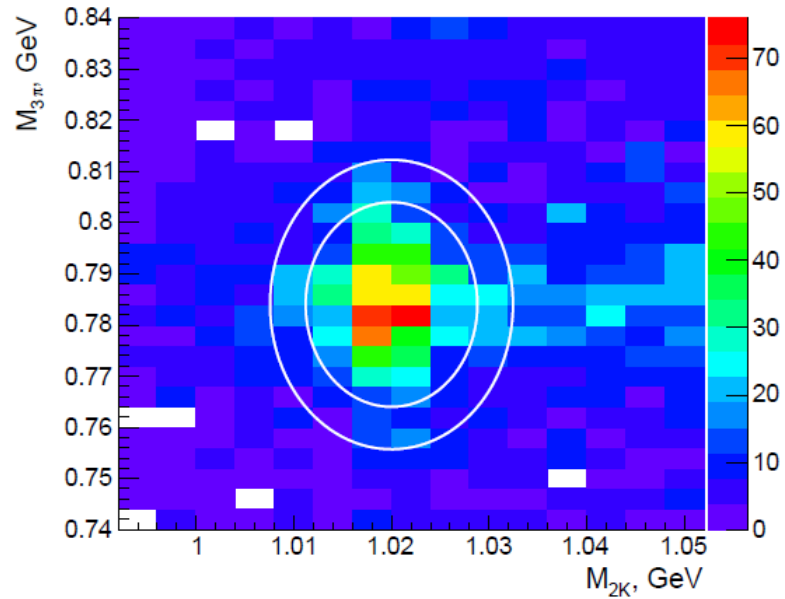
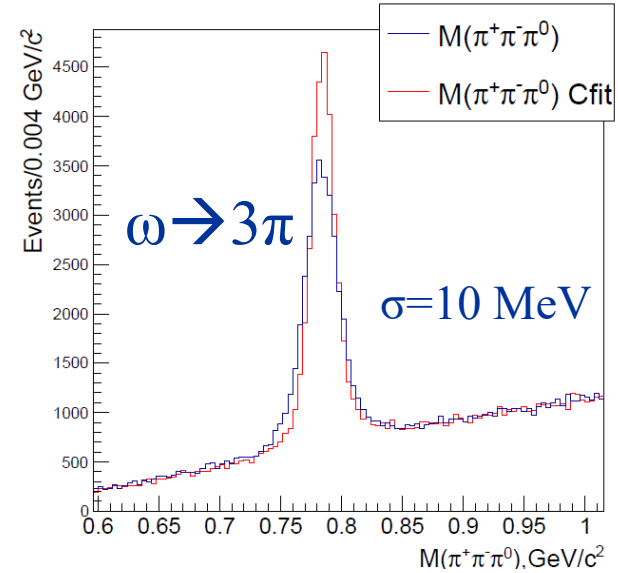
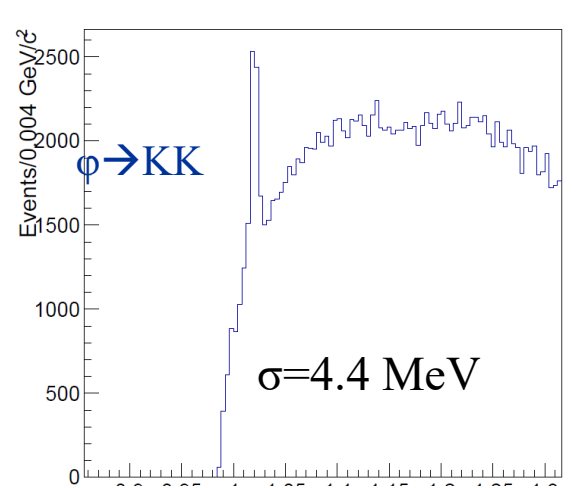
This work by VES:

$$\pi^- \text{ Be} \rightarrow A' \omega(\pi^+ \pi^- \pi^0) \phi(K^+ K^-)$$

(A' – nucleus and neutron)

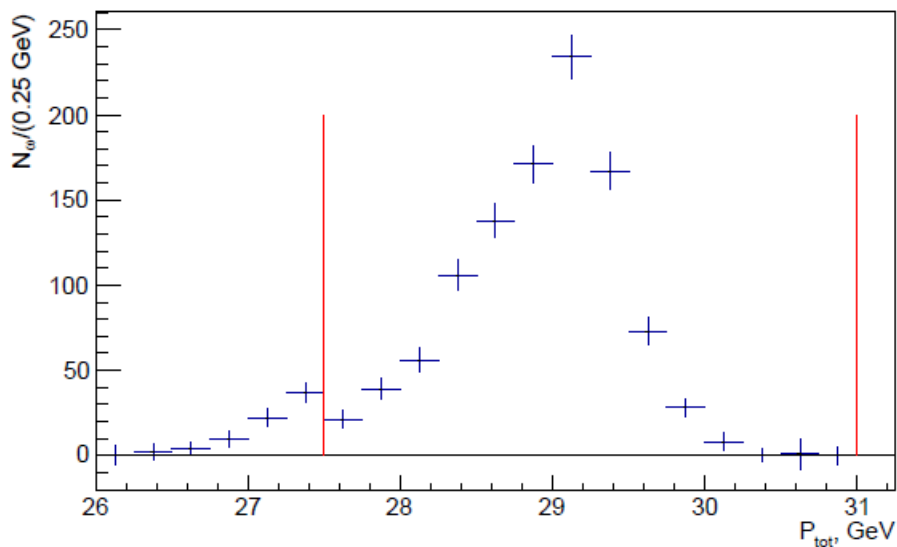
at $p = 29 \text{ GeV}$

Some features of $\omega\phi$ system



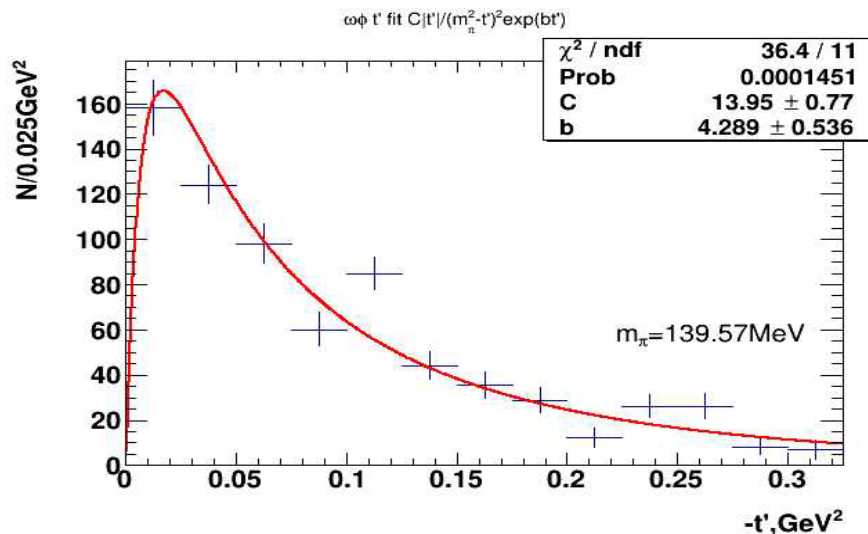
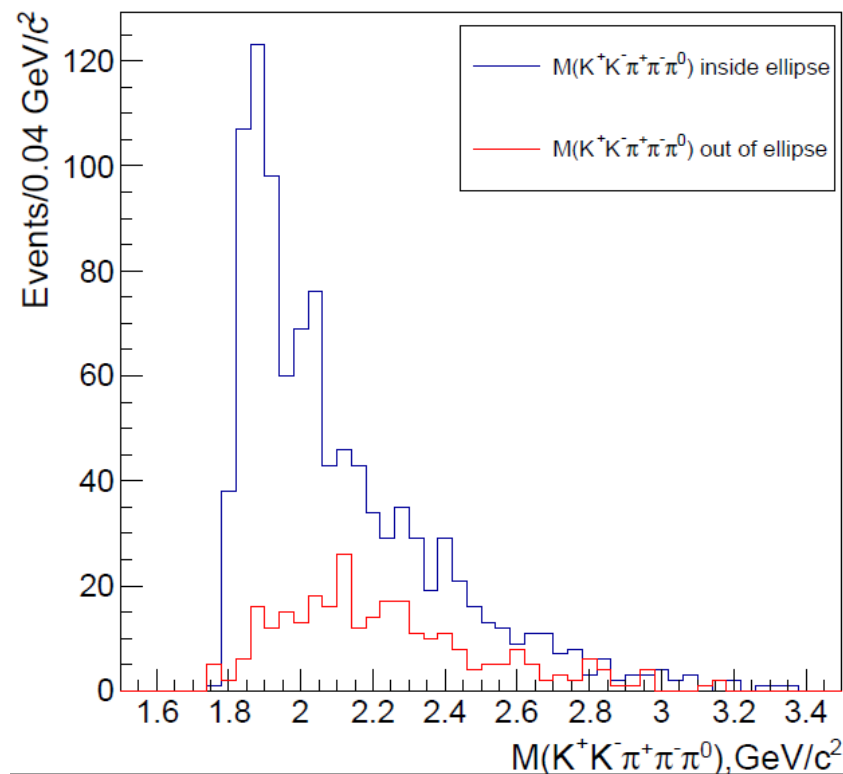
$$r_{2M}^2 = (M_{3\pi} - M_\omega)^2 / (2\sigma_\omega)^2 + (M_{2K} - M_\phi)^2 / (2\sigma_\phi)^2 \leq 1$$

Some features of $\omega\phi$ system (2)



P_{tot} : “exclusivity” cut

Invariant mass spectra in **signal** and **background** regions



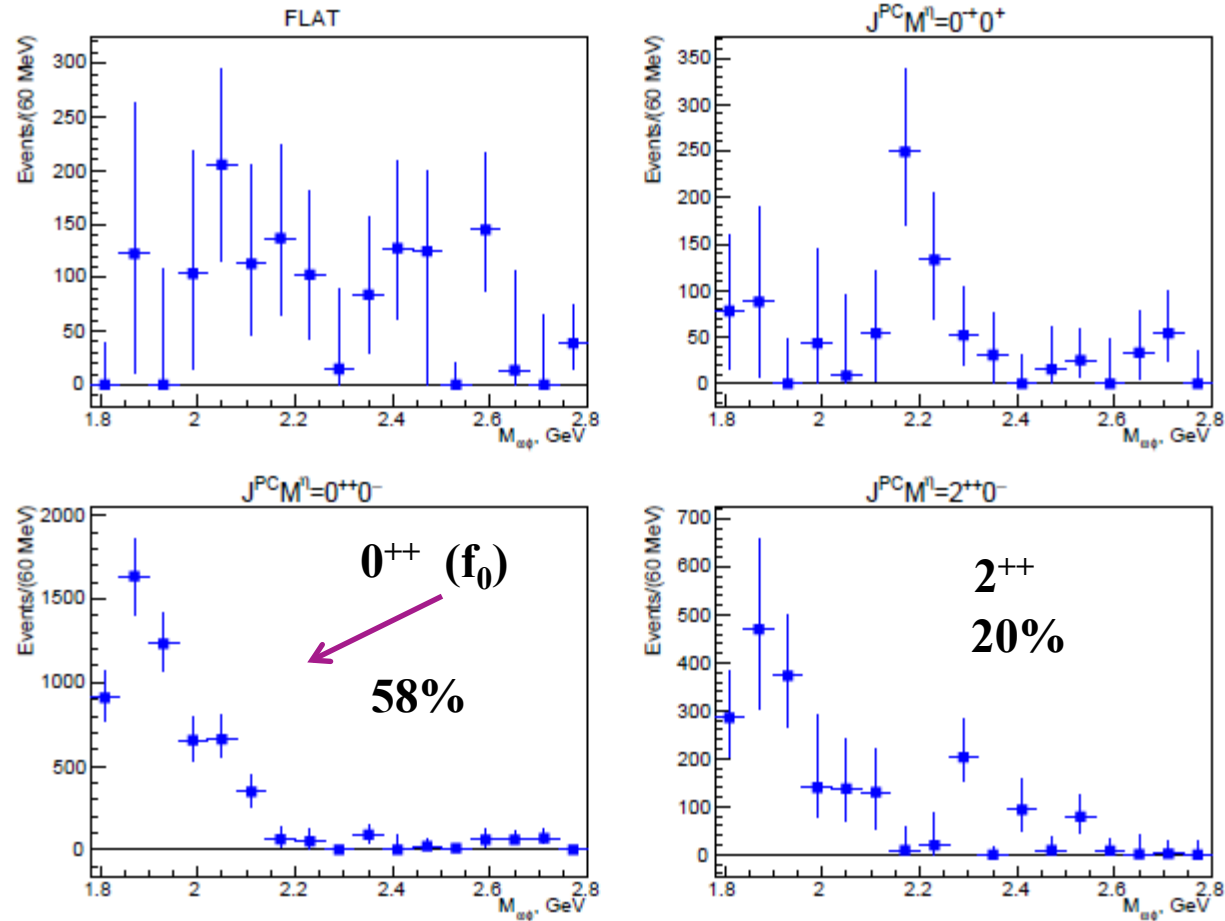
t – distribution and OPE fit

Partial Wave Analysis of $\omega\phi$

- ❖ Mass-independent PWA in 60-MeV bins, no t - binning
- ❖ Approximation of narrow ω, ϕ (quasi-2-particle PWA)
- ❖ Production matrix $r=1$ in Gottfried-Jackson system => complex elements = fit parameters
- ❖ «reflectivity» basis: $\eta=\pm 1$ correspond to NPE, UPE
- ❖ Decay amplitudes in Zemach tensor formalism; $s_1+s_2 \rightarrow S, S+L \rightarrow J$
- ❖ Event-by-event extended Likelihood method
- ❖ Acceptance (efficiency) integrals with Monte-Carlo

Major PWA fit

($t < 0.15 \text{ GeV}^2$, 580 events)

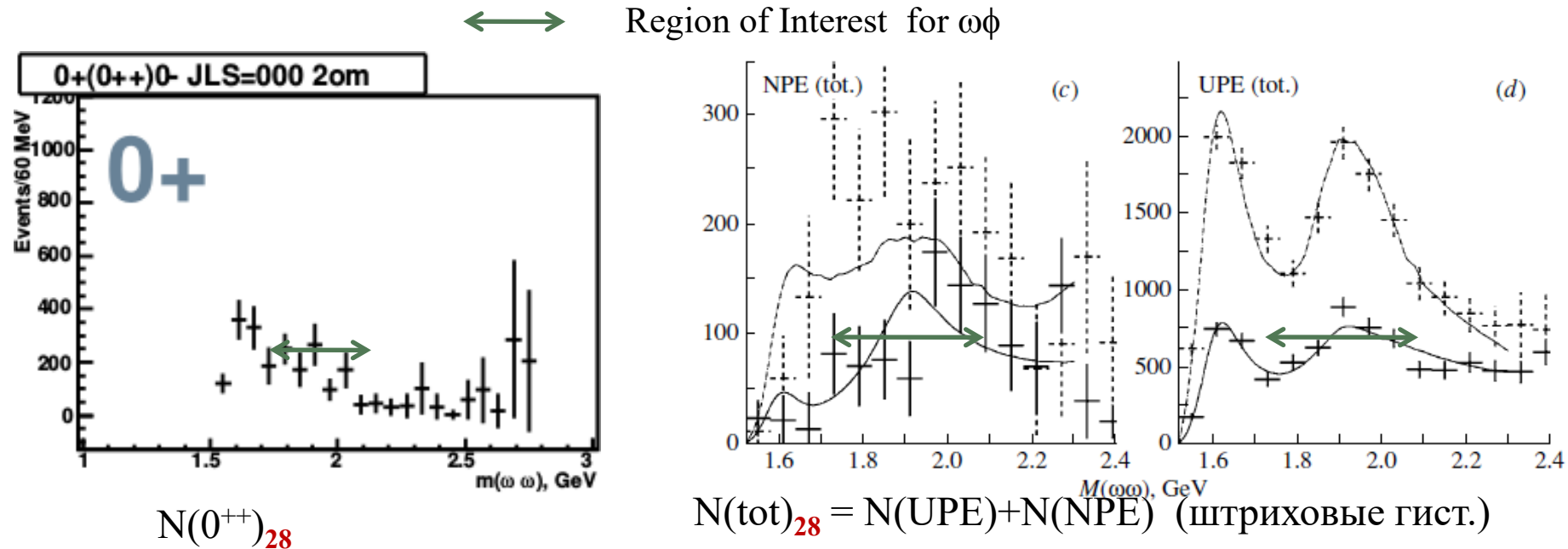


UPE waves dominate
supporting OPE

Comparison of $\omega \phi$ and $\omega \omega$ channels

- OZI rule: in various hadron reactions w. light quarks yields ratio
 $R(\phi/\omega) \sim \tan^2 \theta = 4.2 \cdot 10^{-3}$ ($\theta = 3.7^\circ$, $\phi = s \bar{s} \cos \theta + n \bar{n} \sin \theta$)
- Nomokonov, V.P., Sapozhnikov, M.G.: Experimental tests of the Okubo-Zweig-Iizuka rule in hadron interactions. Phys.Part.Nucl. 34, 94–123 (2003)
- **Use older VES results on $\omega\omega$ @28 GeV for comparison with $\omega\phi$ @29 GeV**

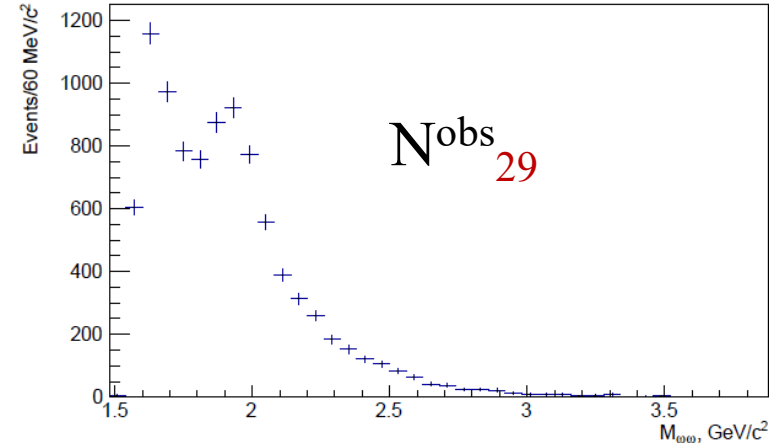
Amelin D.V, et al.. PAN 69, 690-698 (2006); Ivashin, A., et al.: AIP Conf. Proc. 1257(1), 262–266 (2010).



Comparison of $\omega\phi$ and $\omega\omega$ channels (2)

- Newly measured spectrum $M(\omega\omega)$
- GEANT-model efficiency
 $\langle\epsilon_{29}\rangle = 0.06 \pm 0.003$

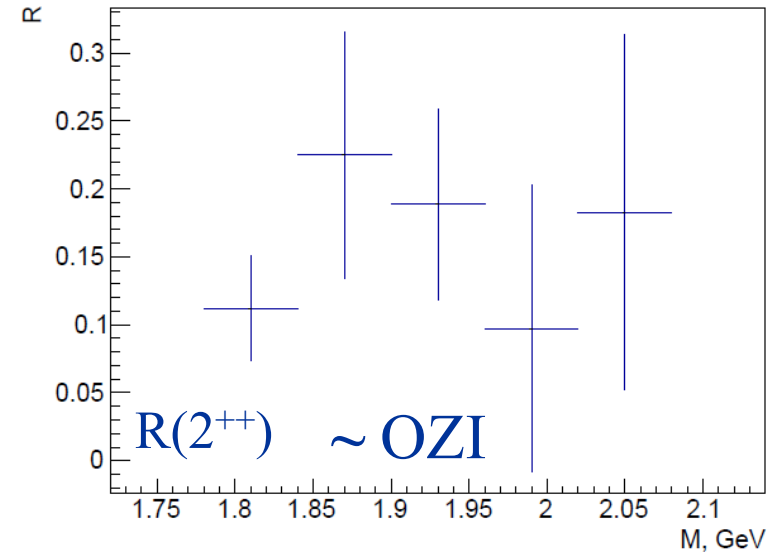
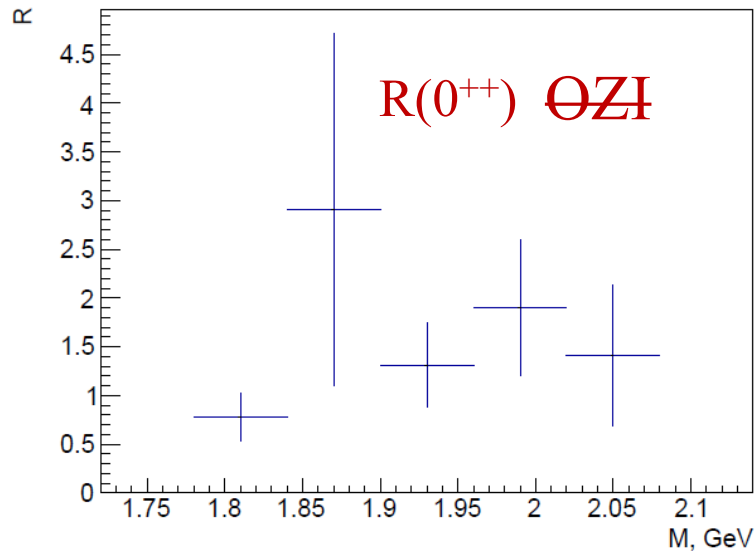
$$N_{\omega\omega,29}^{0+}(M_{\omega\omega}) = \frac{N_{\omega\omega,29}^{obs}}{\epsilon_{29}} \cdot \frac{N_{\omega\omega,28}^{0+}}{N_{\omega\omega,28}}$$



$$R = \frac{N_{\omega\phi,29}^{0+}}{N_{\omega\omega,29}^{0+}} \cdot \frac{Br(\omega \rightarrow \pi^+\pi^-\pi^0)}{Br(\phi \rightarrow K^+K^-)}$$

Ratio of 0^{++}
intensities in $\omega\phi$
and $\omega\omega$

Comparison of $\omega\phi$ and $\omega\omega$ channels (3)



Maximal OZI – rule violation

$R_A = R \cdot q_{\omega\omega}/q_{\omega\phi}$ (q – decay momenta) -- to account for phase space difference
 $M=[1.84\dots 2.08]$

$$\langle R_A \rangle (0^{++}) = 2.4 \pm 0.5 \quad (!)$$

$$\langle R_A \rangle (2^{++}) = 0.30 \pm 0.08$$

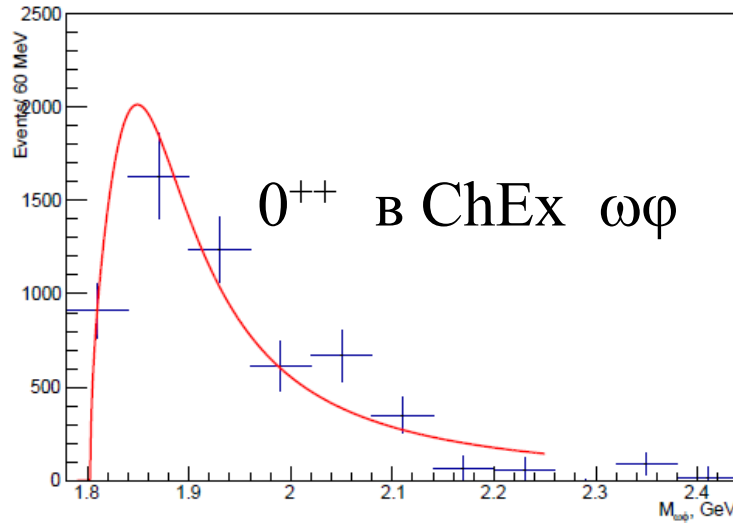
✓ Large mixing of scalars (but not tensors) w. different quark content ?

Isgur, N., Thacker, H.B.: On the origin of the OZI rule in QCD. Phys.Rev. D 64, 094507 (2001)

Comparison of 0^{++} in two production processes

$$\begin{array}{ccc} \diamond \pi^- \text{Be} \rightarrow A' f_0 & \text{vs} & J/\psi \rightarrow \gamma f_0(1710) \\ \quad \quad \quad \downarrow \rightarrow (\omega\phi, \omega\omega) & & \quad \quad \quad \downarrow \rightarrow (\omega\phi, \omega\omega) \\ R(\text{ChEx}) = 0.7 \pm 0.15 & & R(\text{Rad.dec.}) = 0.8 \pm 0.4 \quad (M > M_{\omega\omega}) \end{array}$$

$$\diamond \frac{dN}{dM} = \frac{CM_R^2 \Gamma_0 g q_{\omega\phi}}{(M_R^2 - M^2)^2 + M_R^2 (\Gamma_0 + g q_{\omega\phi})^2} \quad (M > M_{\omega} + M_{\phi})$$



$$\begin{aligned} M_R &= 1834 \pm 14 \text{ (stat.) } {}^{+2}_{-10} \text{ (syst.) MeV} \\ \Gamma_0 &= 114 \pm 15 \text{ (stat.) } {}^{+5}_{-15} \text{ (syst.) MeV} \\ \text{Br}(R \rightarrow \omega\phi) &\approx g = 0.1 \end{aligned}$$

N.B. Rad.dec.:

$$\begin{aligned} M_R &= 1795 \pm 7 {}^{+23}_{-20} \text{ MeV} \\ \Gamma_0 &= 95 \pm 10 {}^{+78}_{-82} \text{ MeV} \end{aligned}$$

✓ Conclusion: the same object observed

(?) $f_0(1710)$ according to PDG: $M=1733 {}^{+8}_{-7} \text{ MeV}$, $\Gamma = 150 {}^{+12}_{-10} \text{ MeV}$

ChEx cross-section for $f_0(1710)$

❖ The key element in the analysis

$$\sigma(\pi^- \text{ Be} \rightarrow \Lambda \omega \phi) (J^{PC}=0^{++}, M_{\omega\phi} < 2.14 \text{ GeV}, |t| < 0.15 \text{ GeV}^2) = \\ 98 \pm 7(\text{stat.}) \pm 7(\text{syst.}) \quad \text{nBn}$$

❖ ChEx on light nuclei*: $\sigma \propto Z^{0.73 \pm 0.03}$

$$\sigma(\pi^- p \rightarrow n \omega \phi) (J^{PC}=0^{++}, M_{\omega\phi} < 2.14 \text{ GeV}, |t| < 0.15 \text{ GeV}^2) = \\ 36 \pm 5 \quad \text{nBn}$$

[12] Kolbig, K.S., Margolis, B.: Particle production in nuclei and unstable particle cross-sections. Nucl. Phys. B **6**, 85–101 (1968). [https://doi.org/10.1016/0550-3213\(68\)90271-X](https://doi.org/10.1016/0550-3213(68)90271-X)

[13] Guisan, O., Bonamy, P., Le Du, P., Paul, L.: Study of $\pi^- p \rightarrow \pi^0 n$ and $\pi^- p \rightarrow \eta n$ reactions in nuclei at 7.82 gev/c. Nucl. Phys. B **32**, 681–690 (1971). [https://doi.org/10.1016/0550-3213\(71\)90500-1](https://doi.org/10.1016/0550-3213(71)90500-1)

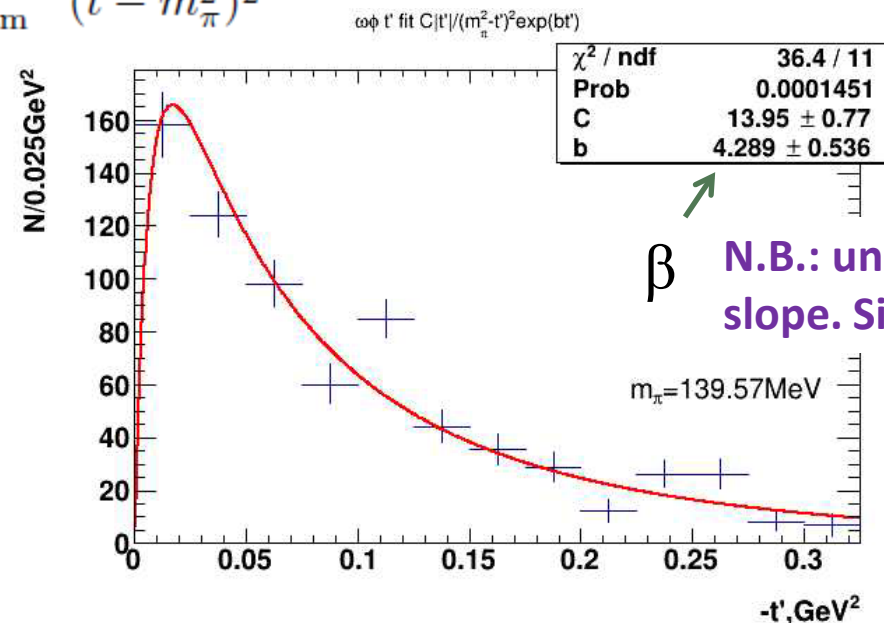
*

[14] Apokin, V.D., *et al.*: DETERMINATION OF THE CROSS-SECTION OF THE PROCESS $\pi^+ \pi^- \rightarrow \pi^0 \pi^0$ IN THE DIPION MASS RANGE $0.55\text{-GeV} < M < 2\text{-GeV}$ FROM THE REACTION $\pi^- p \rightarrow \pi^0 \pi^0 n$ AT 39.1-GeV/c. Sov. J. Nucl. Phys. **49**, 278 (1989)

From OPE X-section to $\text{Br}(f_0 \rightarrow 2\pi)$

$$\frac{d\sigma(\pi^- p \rightarrow nX) \text{Br}(X \rightarrow \text{channel})}{d|t|} =$$

$$26.9 \text{ mb } \text{Br}(X \rightarrow \pi\pi) \text{Br}(X \rightarrow \text{channel}) \frac{M_X \Gamma_X}{P_{\text{beam}}^2} \frac{|t| e^{\beta(t-m_\pi^2)}}{(t-m_\pi^2)^2}$$



- [16] Chew, G.F., Low, F.E.: Unstable particles as targets in scattering experiments. Phys. Rev. 113, 1640–1648 (1959). <https://doi.org/10.1103/PhysRev.113.1640>
- [17] Williams, P.K.: Extrapolation model for pi pi scattering. Phys. Rev. D 1, 1312–1318 (1970). <https://doi.org/10.1103/PhysRevD.1.1312>
- [18] Hyams, B., *et al.*: t Dependence and Production Mechanisms of the rho, f and g Resonances from $\pi^- p \rightarrow \pi^- \pi^+ n$ at 17.2-GeV. Phys. Lett. B 51, 272–278 (1974). [https://doi.org/10.1016/0370-2693\(74\)90290-1](https://doi.org/10.1016/0370-2693(74)90290-1)

Combining probabilities from ChEx and RadDecay data:

- $\text{Br}(f_0 \rightarrow \pi\pi) \cdot \text{Br}(f_0 \rightarrow \omega\phi) = (4.8 \pm 1.2) \cdot 10^{-3}$ (this work) &
- $\text{Br}(J/\psi \rightarrow \gamma f_0(\rightarrow \pi\pi)) \cdot \text{Br}(J/\psi \rightarrow \gamma f_0(\rightarrow \omega\phi)) = (9.5 \pm 2.6) \cdot 10^{-8}$ (PDG)



✓ $\text{Br}(J/\psi \rightarrow \gamma f_0(1710)) = (4.5 \pm 0.8) \cdot 10^{-3}$

- Lattice calculations for a scalar glueball:

$$\text{Br}(J/\psi \rightarrow \gamma 0^+ gg) = (3.8 \pm 0.9) \cdot 10^{-3}$$

[19] Gui, L.-C., Chen, Y., Li, G., Liu, C., Liu, Y.-B., Ma, J.-P., Yang, Y.-B., Zhang, J.-B.: Scalar Glueball in Radiative J/ψ Decay on the Lattice. Phys. Rev. Lett. 110(2), 021601 (2013) <https://arxiv.org/abs/1206.0125> [hep-lat]. <https://doi.org/10.1103/PhysRevLett.110.021601>

- ✓ Large (dominant ?) glueball component in $f_0(1710)$

More about glueball

❖ A model for Rad.Dec. of heavy vector quarkonium

Close, F.E., Farrar, G.R., Li, Z.-p.: Determining the gluonic content of isoscalar mesons. Phys. Rev. D 55, 5749–5766 (1997):

$$\Gamma [(1^- \text{ } Q \bar{Q}) \rightarrow \gamma R_J] \propto \Gamma [R_J \rightarrow gg]$$

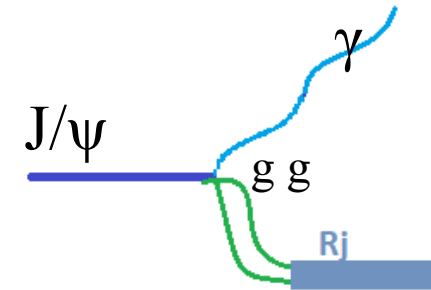
The coefficient of proportionality is calculated

Using our finding

$$\text{Br} (J/\psi \rightarrow \gamma f_0(1710)) = (4.5 \pm 0.8) \cdot 10^{-3}$$

one gets

$$\text{Br}(f_0(1710) \rightarrow gg) = 1.7 \pm 0.4$$



Alternative for $f_0(1710)$ «from PDG»

- 2 scalars are discussed in $1.7 < M < 1.8$ GeV range
- A comprehensive analysis :

[12] Sarantsev, A.V., Denisenko, I., Thoma, U., Klempt, E.: Scalar isoscalar mesons and the scalar glueball from radiative J/ψ decays. Phys. Lett. B 816, 136227 (2021) <https://arxiv.org/abs/2103.09680> [hep-ph]. <https://doi.org/10.1016/j.physletb.2021.136227>

$BR_{J/\psi \rightarrow \gamma f_0 \rightarrow}$	$\gamma\pi\pi$	$\gamma K\bar{K}$	$\gamma\eta\eta$	$\gamma\eta\eta'$	$\gamma\omega\phi$	Missing		Total	Unit
						$\gamma 4\pi$	$\gamma\omega\omega$		
$f_0(1710)$	6 ± 2	23 ± 8	12 ± 4	6.5 ± 2.5	1 ± 1	7 ± 3		56 ± 10	$\cdot 10^{-5}$
$f_0(1770)$	24 ± 8	60 ± 20	7 ± 1	2.5 ± 1.1	22 ± 4	65 ± 15		181 ± 26	
$f_0(1750)$	38 ± 5	99^{+10}_{-6}	24^{+12}_{-7}		25 ± 6	97 ± 18	31 ± 10		

- ✓ Splitting of $f_0(1710)$ to **another $f_0(1710)$** and $f_0(1770)$
- ✓ **Only $f_0(1770)$** contributes to $\omega\phi \rightarrow$ is observed in VES
- ✓ Using parameters for $f_0(1770)$ and our data on X-section in $\omega\phi \rightarrow$ small change of quantitative results:

$$Br(f_0(1770) \rightarrow \pi\pi) Br(f_0(1770) \rightarrow \omega\phi) = (3.9 \pm 1.0) \cdot 10^{-3}$$

$$Br(J/\psi \rightarrow \gamma f_0(1770)) = (3.7 \pm 0.8) \cdot 10^{-3}$$

$$Br(f_0(1770) \rightarrow gg) = 1.12 \pm 0.32$$

Conclusion

❖ VES experiment measures

$$\sigma(\pi^- \text{Be} \rightarrow \Lambda f_0 (|t| < 0.15 \text{ GeV}^2)) \cdot \text{Br}(f_0 \rightarrow \omega \varphi) = 98 \pm 7(\text{stat.}) \pm 7(\text{syst.}) \text{ nBn}$$

❖ With OPE approximation, identifying the f_0 either as $f_0(1710)$ or $f_0(1770)$

and together with J/ψ Rad.Dec. data:

$$\text{Br}(J/\psi \rightarrow \gamma f_0(1710)) = (4.5 \pm 0.8) \cdot 10^{-3}$$

$$\text{or Br}(J/\psi \rightarrow \gamma f_0(1770)) = (3.7 \pm 0.8) \cdot 10^{-3}$$

According to models this points to **large glueball component** in this meson.

Study of the $\eta'\pi^+\pi^-$ system

in charge-exchange reaction of pions with Be at 29 GeV

Motivation

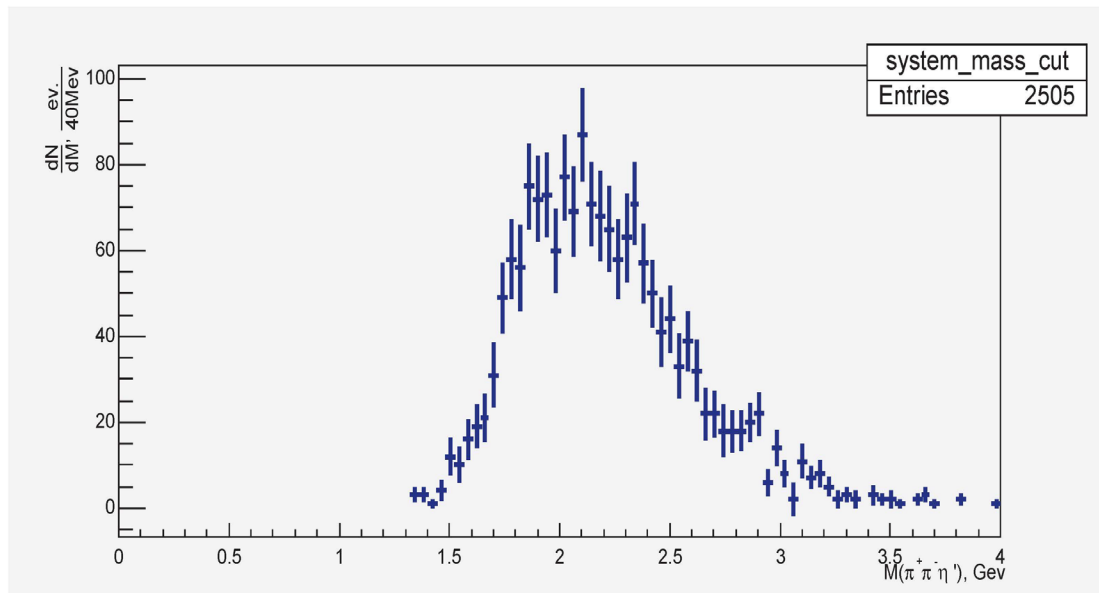
- A special role of the η' in $J^P = 0^-$ ($\mathbb{P}$) nonet. Large mass due to $\blacktriangleright$ - anomaly
- What are its radial excitations ? In particular in the $\eta'\pi^+\pi^-$ channel
- $\mathbb{P}$ – glueball also coupled to $\eta'\pi^+\pi^-$
- Wide set of quantum numbers possible. Comparison of structures in $\eta'\pi\pi$ and $\eta\pi\pi$ from point for a search for hybrids.
- Possible qq –exotic $J^{PC} = 1^{-+}$ wave in the subsystem $\eta'\pi$
- Experimental data on $\eta'\pi\pi$ are scarce: some from pp, majority from e^+e^- , including rad.decays of J/ψ . In particular $X(2600)$ with $I^G J^{PC} = 0^+0^{-+}$ or 0^+2^{-+} .
- **No data** in ChEx. Another mechanism $\rightarrow$ possible access to different set of states

Characteristics of the selected sample

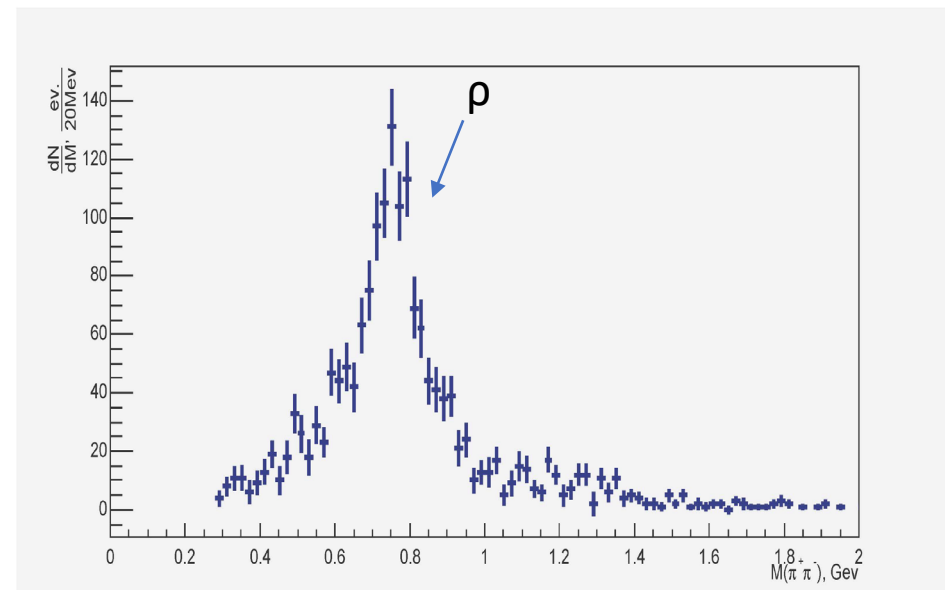
$$\eta' \pi^+ \pi^- \quad \eta' \rightarrow \pi^+ \pi^- \eta \rightarrow \pi^+ \pi^- 2\gamma \quad \text{Br} = 16.75\%$$

➤ Data of 7 runs y. 2013 - 2024 ; $\sim 2.8 \cdot 10^{11}$ beam particles during live-time

$\pi\pi\eta'$ invariant mass spectrum



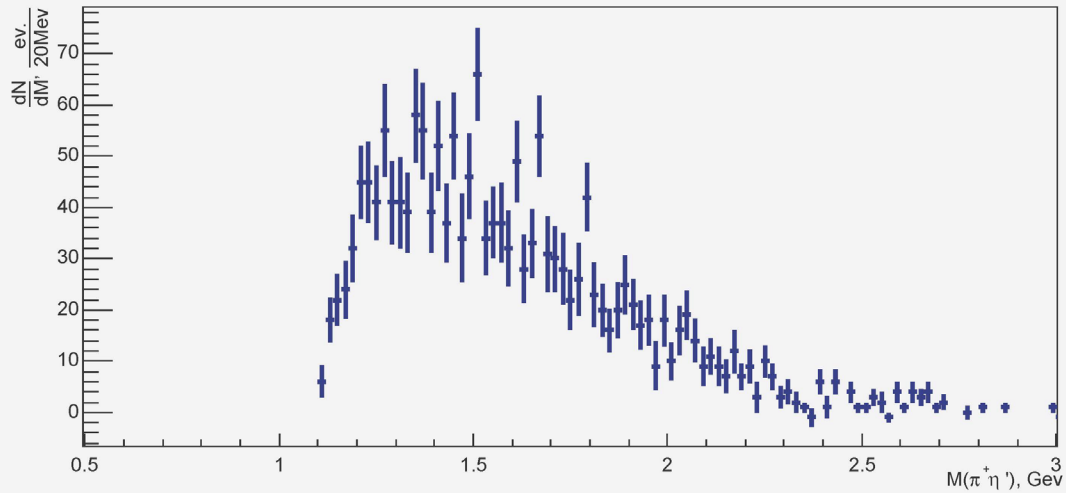
$\pi^+\pi^-$ mass spectrum



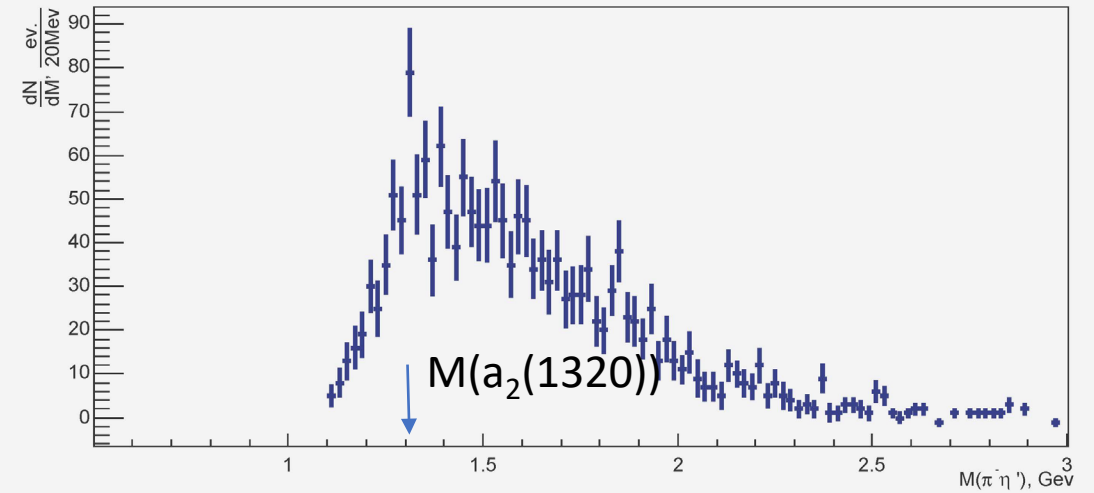
➤ **I=1 states $\rho\eta'$ dominate in the $\pi\pi\eta'$**

Characteristics of the selected sample (2)

$\pi^+ \eta'$ mass spectrum



$\pi^- \eta'$ mass spectrum

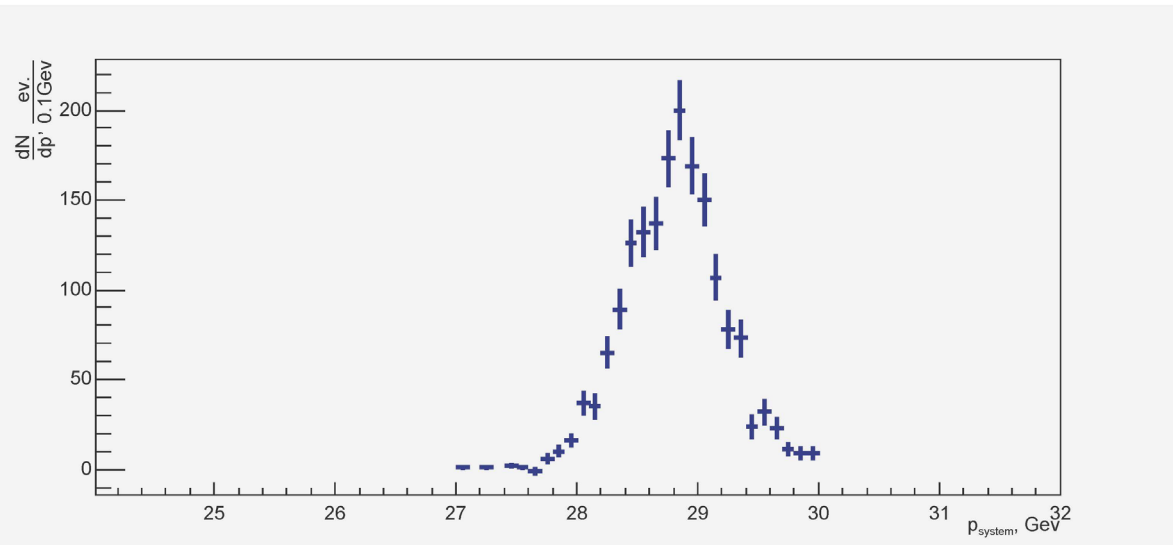


No evident structures

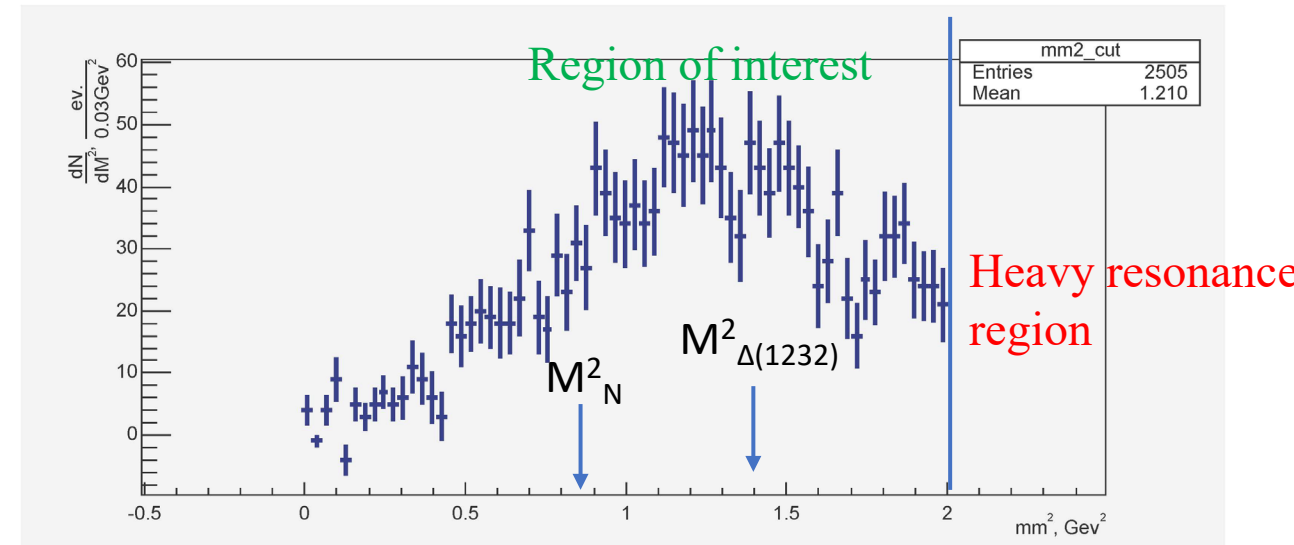
$a_2(1320)$?

Characteristics of the selected sample (3)

Momentum spectrum of the system



Missing mass squared distribution

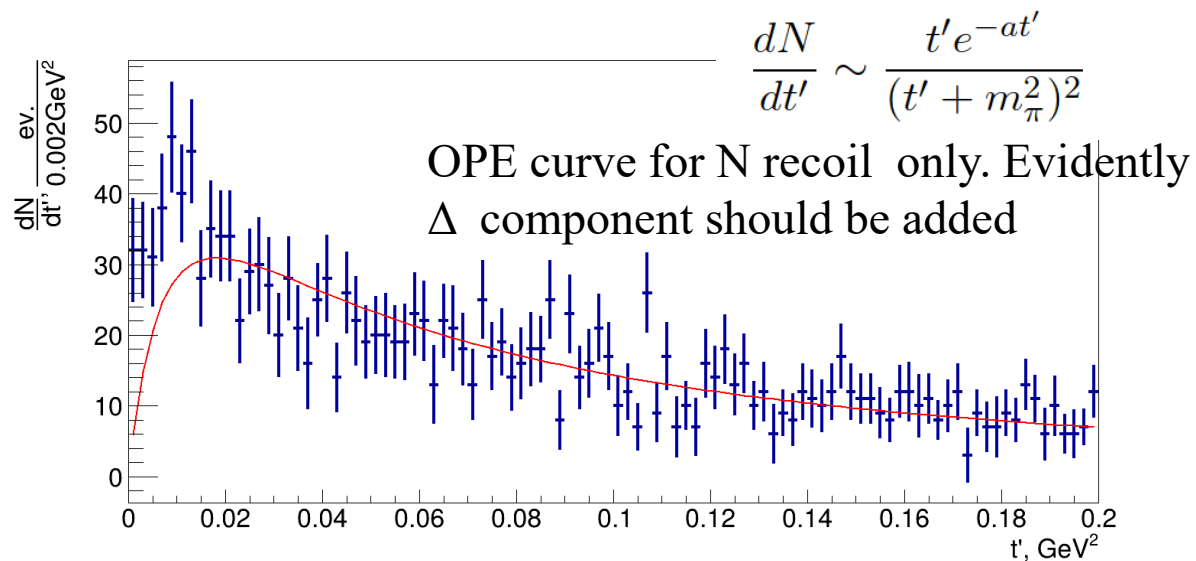


Exclusivity:

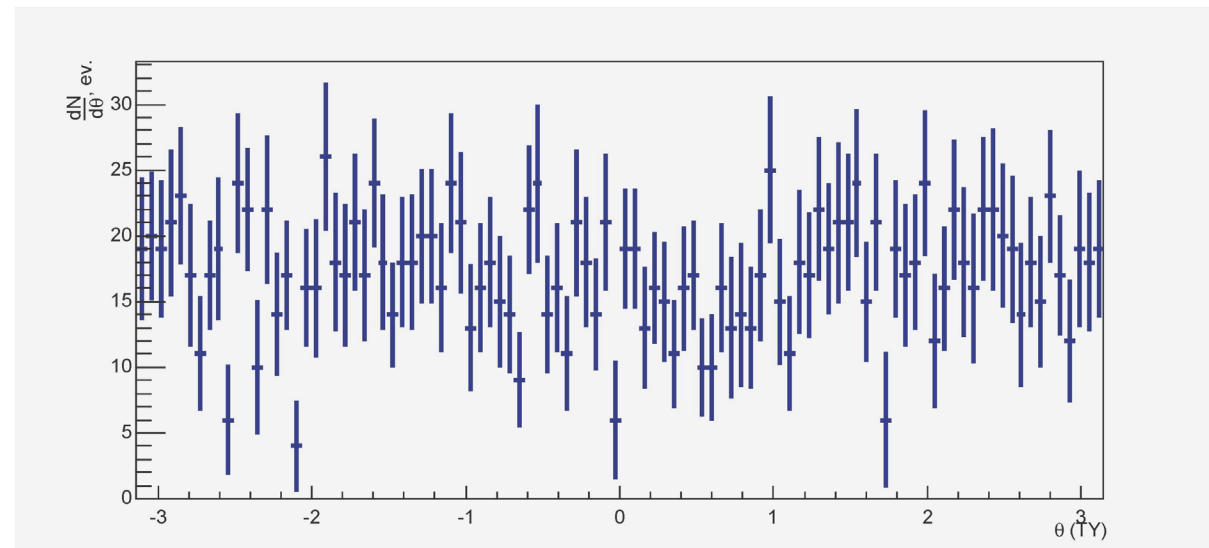
- no missed “fast” particles from beam fragmentation.
- target fragmentation dominates over nucleon recoil

Characteristics of the selected sample $\eta' \pi^+ \pi^-$ (4)

t' distribution



Treiman – Yang angle spectrum for η'



Narrow t' – distribution and uniformity over ϕ_{TY} are in accordance with OPE hypothesis

A «standard» region $t' < 0.2 \text{ GeV}^2$ is further analysed

X-section. Model for efficiency

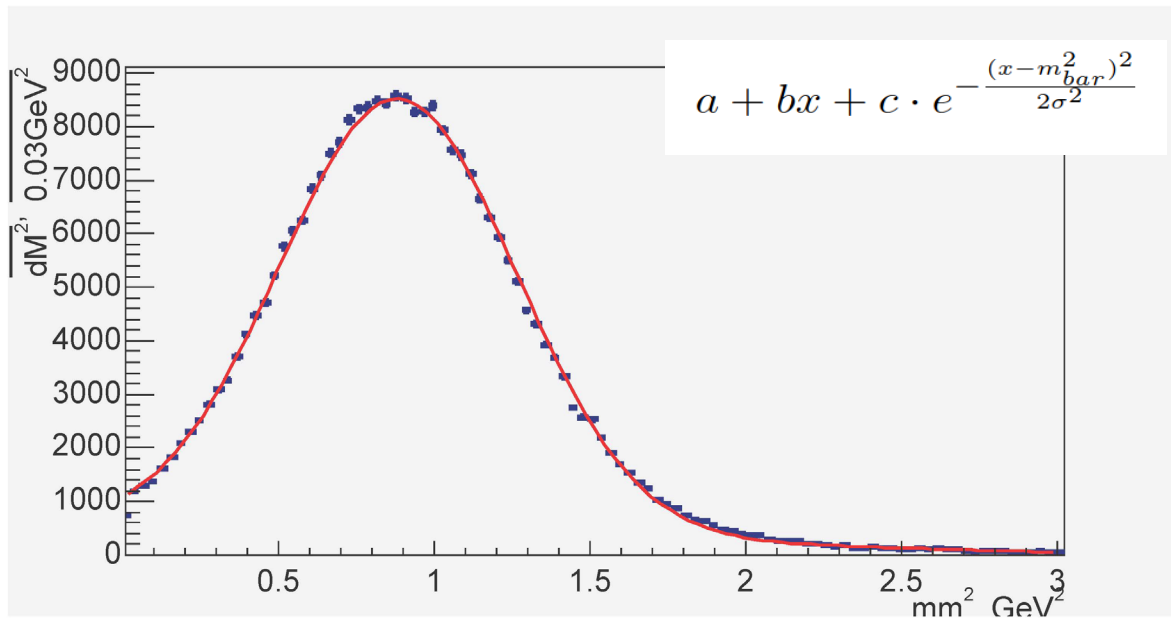
- Detailed setup model
- Detailed model (generators) for particles passage through the matter
- Simplified model for the reaction
 - realistic beam and scattering vertex
 - t –spectrum – according to OPE with N (J =1/2) or Δ (J =3/2)
 - System X of mass m_s decays to eta' 2pi according to phase space
 - **Recoil:** free mixture of n, $\Delta(1232) \rightarrow N \pi$, “ $\Delta(1600)$ ” $\rightarrow \Delta \pi$
 - Input channels according to ^9Be composition p:n = 4:5.
 - Isotopic states and decay modes according to Clebsh coefficients

$$\frac{dN}{dt'} \sim \frac{t' e^{-at'}}{(t' + m_\pi^2)^2}$$

$$\frac{dN}{dt'} \sim \frac{e^{-at'}}{(t' + m_\pi^2)^2}$$

X-section. Model for efficiency (2)

Recoil composition



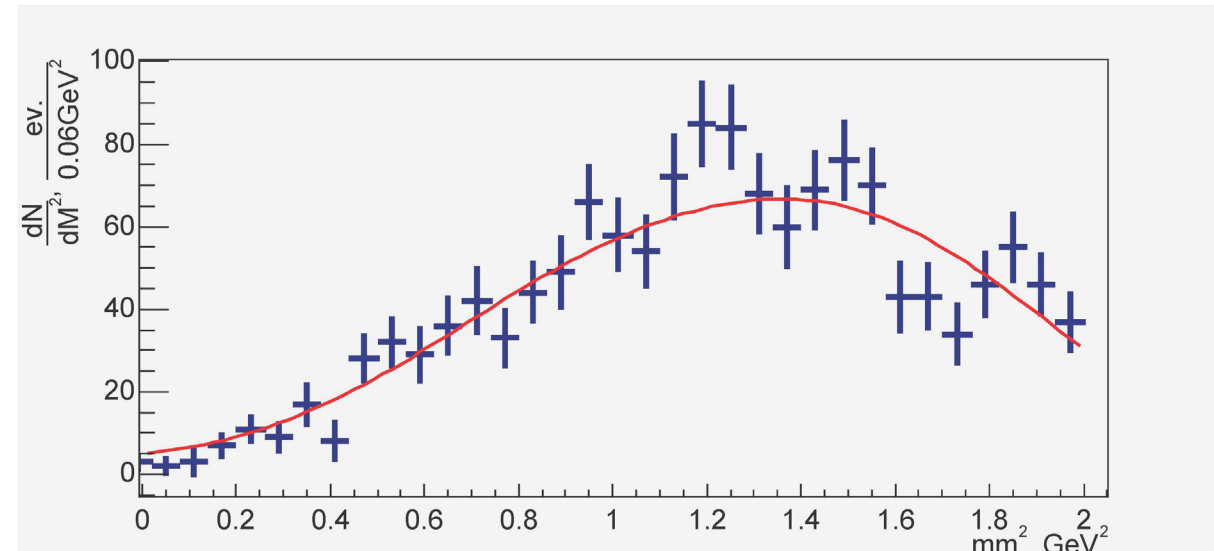
← Model function $f_1(\text{mm}^2)$ for neutron component

PRELIMINARY

Data fit with 3 model functions →

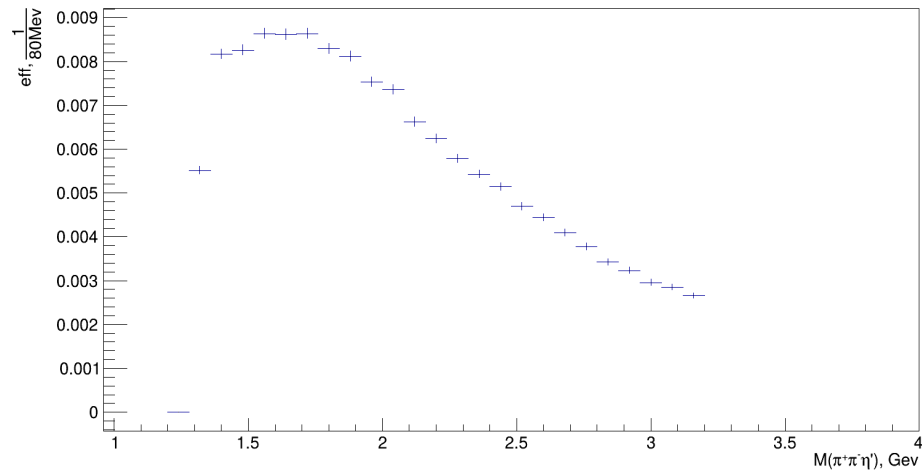
$$f(x) = n_1 f_1(x) + n_2 f_2(x) + n_3 f_3(x)$$

Resulting ratio of components in initial mixture
 $n : \Delta(1232) = 0.14$

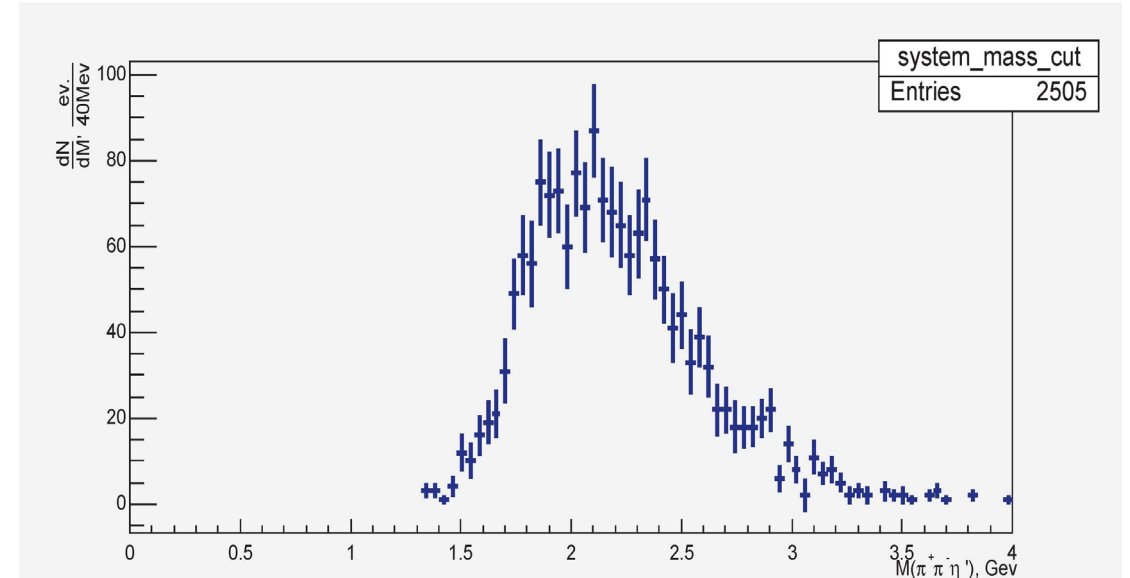


Efficiency and mass spectra

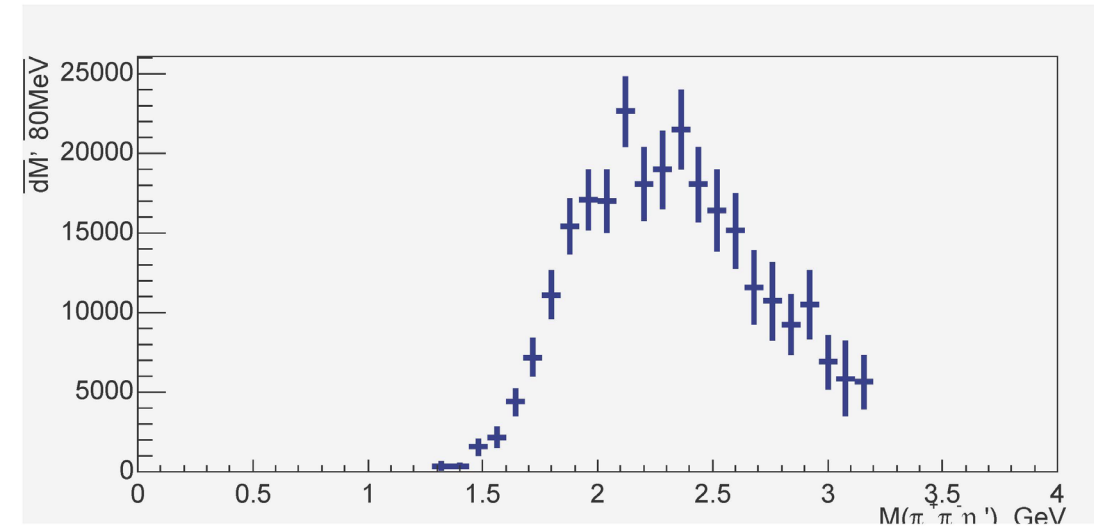
Efficiency vs $M(\eta' \pi^+ \pi^-)$



Observed $M(\eta' \pi^+ \pi^-)$ spectrum



$M(\eta' \pi^+ \pi^-)$ spectrum corrected by efficiency



Resulting X-section on ${}^9\text{Be}$

Run#	X-section, μBn
run44	1.92 ± 0.11
run45	1.80 ± 0.16
run47	1.55 ± 0.22
run48	2.29 ± 0.22
run59	1.32 ± 0.17
run60	1.96 ± 0.47
run62	1.55 ± 0.27

$\approx 2 \cdot 10^3$ events in Trig=MAIN

Topology with Br=16.8%

PRELIMINARY

$$\sigma(\pi^- p \rightarrow n \ \eta' \pi^+ \pi^-, t' < 0.2 \text{ GeV}^2, P=29 \text{ GeV}, {}^9\text{Be}) = 1.78 \pm 0.07 \mu\text{Bn}$$

Only Stat. uncertainty!

Syst. uncertainty is factor ~ 1.5 (expert guess)

Results discussion

- $\eta' \pi^+ \pi^-$ Ch-Ex production with $I=1$ $\rho \eta'$
- compatible with **OPE**
- process with $\Delta(1232)$ dominates, with n significant.
- $\sigma(\pi^- p \rightarrow n \eta' \pi^+ \pi^-, t' < 0.2 \text{ GeV}^2, \text{ target} = {}^9\text{Be}) = 1.78 \pm 0.07 \text{ (stat)} \mu\text{Bn}$

➤ Let's reduce to proton target :

$$\sigma(\pi^- p \rightarrow n X, Z) = \sigma(\pi^- p \rightarrow n X, p) * Z^{2/3} \rightarrow$$

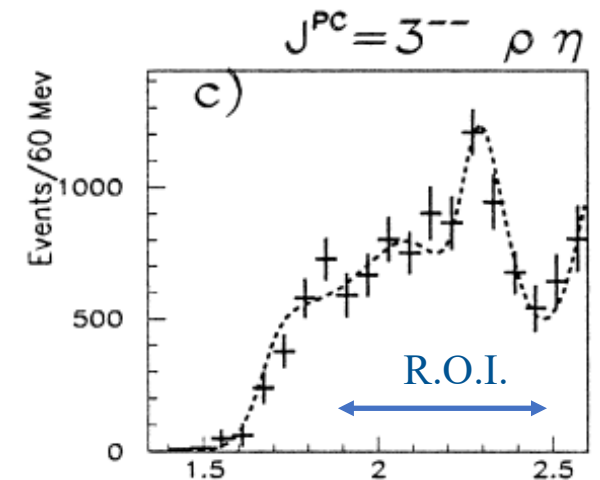
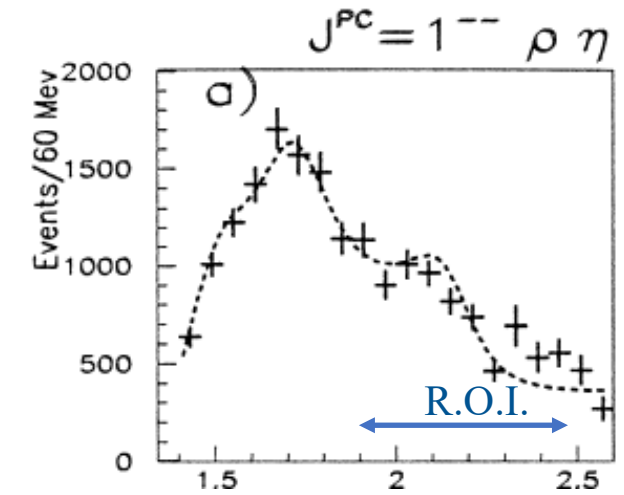
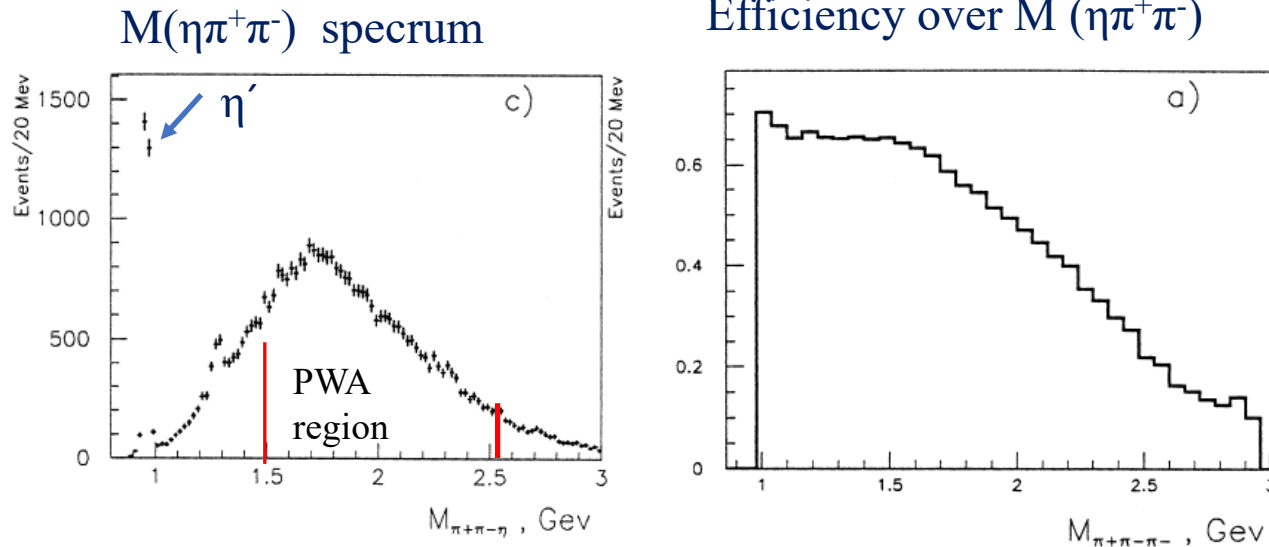
$$\sigma(\pi^- p \rightarrow n \eta' \pi^+ \pi^-, t' < 0.2 \text{ GeV}^2, P=29 \text{ GeV}, \text{ target} = p) \approx 0.7 \mu\text{Bn} \text{ (VES, 2025)}$$

Results discussion (2)

What object(s) could be here ? **Natural** hypothesis for $\pi\pi \rightarrow R$ with $I=1$: $J^{PC} = 1^-, 3^-, \dots$

PWA of similar system $\eta \pi^+ \pi^-$ (VES, Nuclear Physics A 668 (2000) 83-96):

major waves intensities



No X-section in VES-2000. Estimation with:

- normalization to $\eta' \rightarrow \eta \pi^+ \pi^-$
- known $\sigma(\pi p \rightarrow \eta' (\rightarrow 2\gamma) n, |t| < 1.5 \text{ GeV}^2, P = 15 - 40 \text{ GeV})$ Phys.Let. 83B (1979) 1
- given intensities for $1^-, 3^-$
- given efficiency
- reduction of X-sec to unified P beam and t range

Results discussion (3)

- Estimate result:

$$\sigma(\pi^- p \rightarrow \rho\eta \ 1^{--} ; 1.9\text{--}2.3 \text{ GeV}; |t| < 0.2 \text{ GeV}^2; P=27 \text{ GeV}; \text{target} = p) \approx 0.6 \text{ } \mu\text{Bn}$$

$$\sigma(\pi^- p \rightarrow \rho\eta \ {1^{--} + 3^{--}} ; 1.9\text{--}2.5 \text{ GeV}) \approx 1.8 \text{ } \mu\text{Bn}$$

- New measurement VES-2025 for $\rho\eta'$ is in this range
- is compatible with both $\rho\eta$ values within large uncertainty

➤ A good object to consider: $\rho(2150)$

Results discussion (4)

$\rho(2150)$ observations: e^+e^- $\pi^-\pi^+$ $p\bar{p}$

$\rho(2150)$

$$J^{PC} = 1^{++}(1^{--})$$

OMITTED FROM SUMMARY TABLE

This entry was previously called $T_1(2190)$. See the review on "Spectroscopy of Light Meson Resonances."

$\rho(2150)$ MASS

e^+e^- PRODUCED

VALUE (MeV)	EVTS	DOCUMENT ID	TECN	COMMENT
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
2034 ± 13 ± 9		1 ABLIKIM	21A BES3	$e^+e^- \rightarrow \omega\pi^0$
2111 ± 43 ± 25		2 ABLIKIM	21X BES3	$e^+e^- \rightarrow \eta'\pi^+\pi^-$
2255 $+17$ $+50$ -18 -41	1.8k	3 ABLIKIM	20F BES3	$\psi(2S) \rightarrow K^+K^-\eta$
2201 ± 19		4 LEES	20 BABR	$e^+e^- \rightarrow K^+K^-\gamma$
2227 ± 9 ± 9		5 LEES	20 RVUE	$e^+e^- \rightarrow K^+K^-$
2039 ± 8 $+36$ -18		6 ABLIKIM	19AQ BES	$J/\psi \rightarrow K^+K^-\pi^0$
2239.2 ± 7.1 ± 11.3		7 ABLIKIM	19L BES3	$e^+e^- \rightarrow K^+K^-$
2254 ± 22		8 LEES	12G BABR	$e^+e^- \rightarrow \pi^+\pi^-\gamma$
2150 ± 40 ± 50		AUBERT	07AU BABR	10.6 $e^+e^- \rightarrow f_1(1285)\pi^+\pi^-\gamma$
1990 ± 80		AUBERT	07AU BABR	10.6 $e^+e^- \rightarrow \eta'\pi^+\pi^-\gamma$
2153 ± 37		BIAGINI	91 RVUE	$e^+e^- \rightarrow \pi^+\pi^-$, K^+K^-
2110 ± 50		9 CLEGG	90 RVUE	$e^+e^- \rightarrow 3(\pi^+\pi^-)$, $2(\pi^+\pi^-\pi^0)$

$\rho(2150)$ DECAY MODES

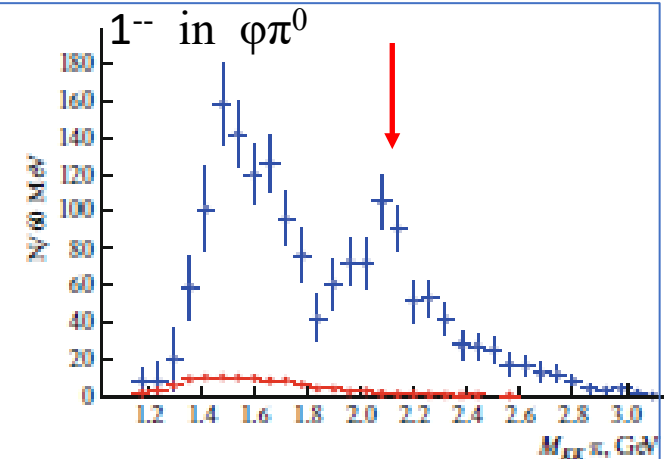
Mode	Fraction (Γ_i/Γ)
Γ_1 e^+e^-	
Γ_2 $\pi^+\pi^-$	seen
Γ_3 K^+K^-	seen
Γ_4 $3(\pi^+\pi^-)$	seen
Γ_5 $2(\pi^+\pi^-\pi^0)$	seen
Γ_6 $\eta'\pi^+\pi^-$	seen
Γ_7 $f_1(1285)\pi^+\pi^-$	seen
Γ_8 $\omega\pi^0$	seen
Γ_9 $\omega\pi^0\eta$	seen
Γ_{10} $p\bar{p}$	

also in $\eta\phi$ (VES, 2000)

possibly in
 $\eta'\phi$ (VES, 2025)

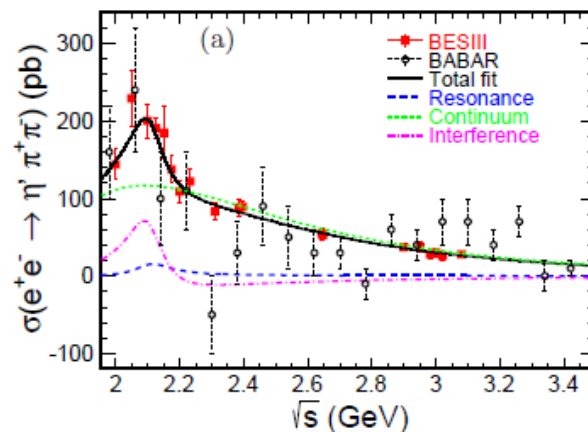
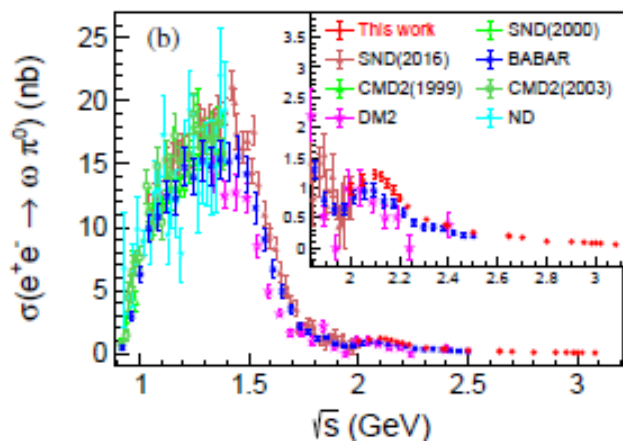
and in $\phi\pi^0$ (VES, 2024)

Physics of Particles and Nuclei Letters v.22 (2025) 1, p.131–136



Results discussion (5)

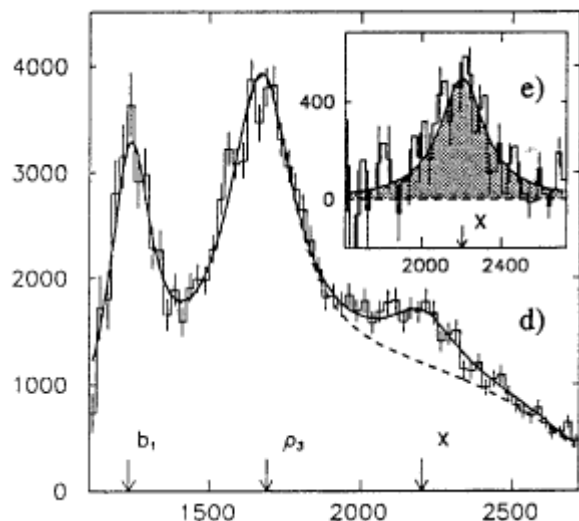
Comparison of branchings for $\rho/X(2150)$



a) e^+e^- (BESIII): two fit models

$$R_1 = \Gamma(\rho\eta') : \Gamma(\omega\pi) = 0.69 \pm 0.4$$

$$R_2 = \Gamma(\rho\eta') : \Gamma(\omega\pi) = 0.019 \pm 0.020$$



b) $\pi^- p$

$$\sigma(X, P=27 \text{ GeV}) \cdot \text{BR}(\omega\pi) \approx 0.24 \text{ uBn}$$

(GAMS – IHEP and GAMS – CERN)

$$\sigma(\pi^- p \rightarrow Xn) \cdot \text{BR}(X \rightarrow \omega\pi^0) = \begin{cases} 120 \pm 25 \text{ nb} & \text{at } 38 \text{ GeV/c} \\ 20 \pm 6 \text{ nb} & \text{at } 100 \text{ GeV/c} \end{cases}$$

$$\sigma(X) \cdot \text{BR}(\rho\eta') \approx \begin{cases} 0.7 \text{ uBn} & \text{(if } 1^- \text{ dominates)} \\ 0.3 \text{ uBn} & \text{(if } 1^- \text{ и } 3^- \text{ are comparable)} \end{cases}$$

(VES, 2025)

$$R = \text{Br}(\rho\eta') : \text{Br}(\omega\pi) \approx 1. -- 2.9$$

Conclusion

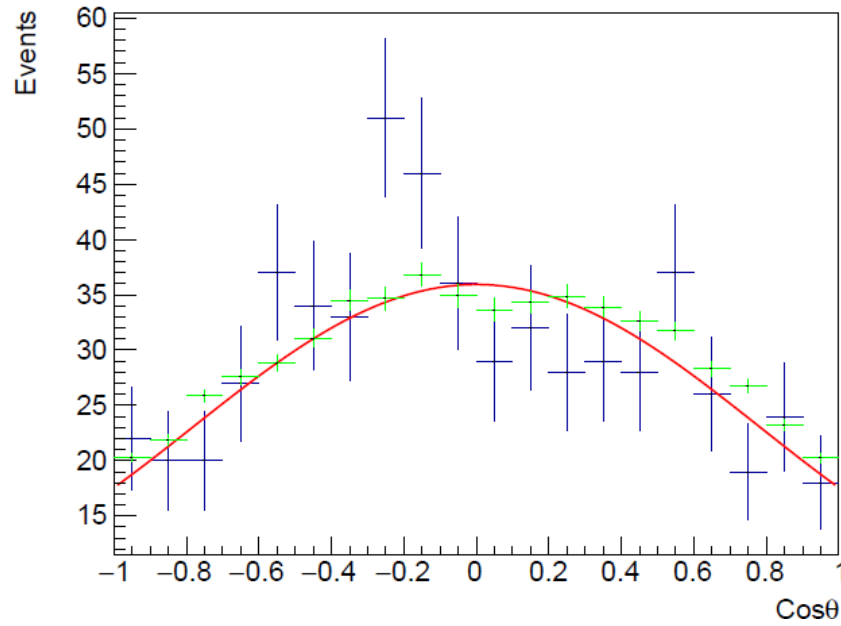
- ✓ VES (U-70): first observation of $\eta'\pi\pi$ in ChEx
- ✓ Compatible with OPE
- ✓ $\sigma(\pi^- p \rightarrow n \eta'\pi^+\pi^-, t' < 0.2 \text{ GeV}^2, P=29 \text{ GeV}, \text{target} = {}^9\text{Be}) = 1.78 \pm 0.07 \text{ (stat.) } \mu\text{Bn}$
- ✓ Mass spectrum with maximum @2.2 GeV and dominance of $\rho\eta'$
- ✓ Assuming $\rho(2150) \rightarrow \rho\eta'$ and using data available:
$$R = \text{Br}(\rho(2150) \rightarrow \rho\eta') : \text{Br}(\rho(2150) \rightarrow \omega\pi) \approx 1. - 2.9$$

not far from BESIII in one model and excludes another one
- ✓ PWA of $\eta'\pi\pi$ could confirm $\rho(2150)$ and looks feasible.

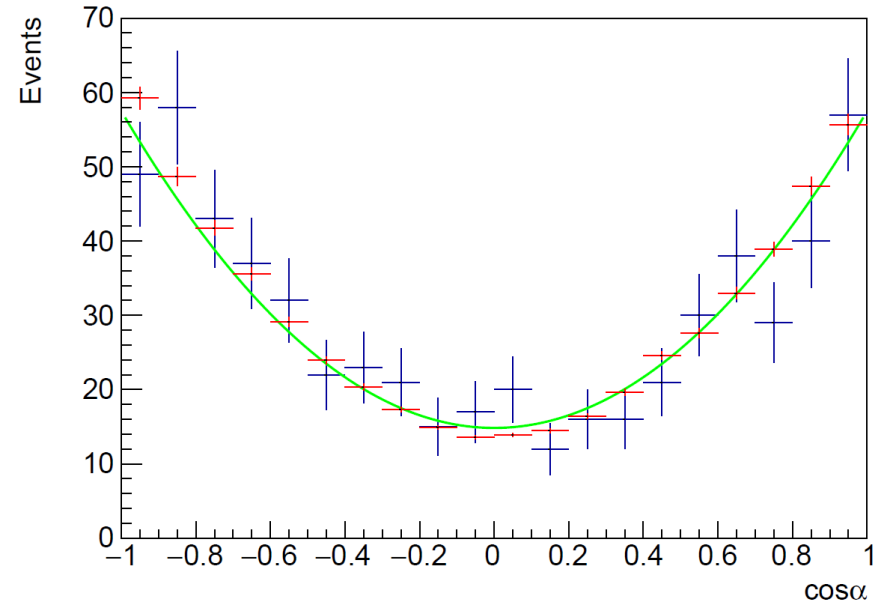
Thank You for Attention

Extra materials

Some features of $\omega\omega$ events (4)



$\theta = \angle (\mathbf{p}(\phi), \mathbf{p}(K))$
(spin alignment of ϕ)



$\alpha = \angle (\mathbf{n}(\omega), \mathbf{p}(K))$
 $\mathbf{n}$ - normal to decay plane
(significant contribution of LS=00)

large errors: data
small errors: PWA model
line: $p_1 + p_2 \cos^2\theta$ function

PWA model for $\omega\phi$

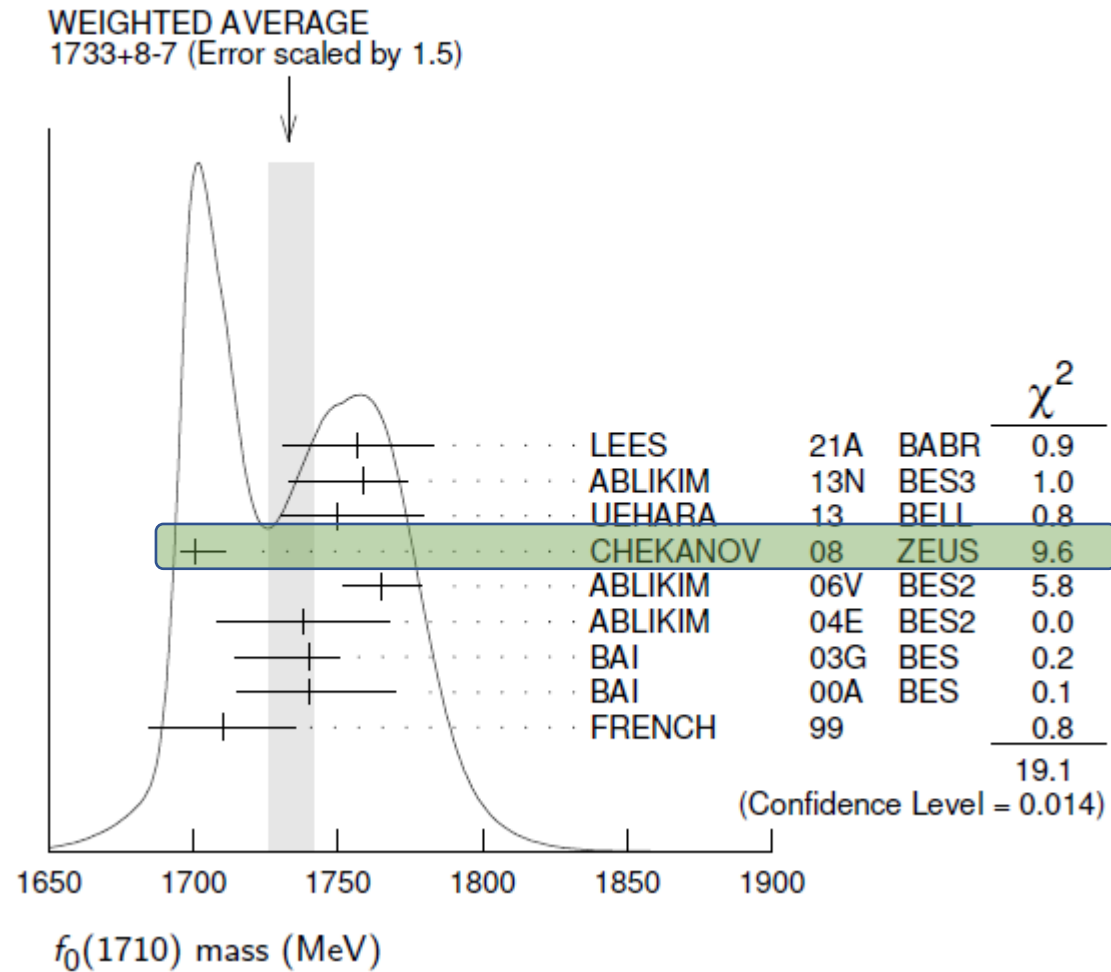
$$\ln\mathcal{L} = \sum_k \ln \sum_{\eta=\pm 1} \left| \sum_i T_i^\eta A_i^\eta(\tau_k) \right|^2 - \sum_{\eta=\pm 1} \sum_{i,j} T_i^\eta T_j^{\eta*} \int A_i^\eta(\tau) A_j^{\eta*}(\tau) \zeta(\tau) d\tau$$

ev.
ph. sp.
prod. ampl.
dec. ampl.
acc. fun.

- ❖ Results: waves intensities (in number of produced events) and phases
- ❖ Set of significant waves $J^{PC}M^\eta$ LS:
 - $0^{++}0-00$, $2^{++}0-02$, $0^{-+}0^+00$, Flat (pseudo wave with uniform population of 5-particle phase space)
- ❖ Efficiency (M) is a weak function, 5.1 – 6.7% including $\varepsilon(\text{PID}) \approx 0.3$

Mass of $f_0(1710)$ in PDG

Citation: R.L. Workman *et al.* (Particle Data Group), Prog.Theor.Exp.Phys. **2022**, 083C01 (2022)

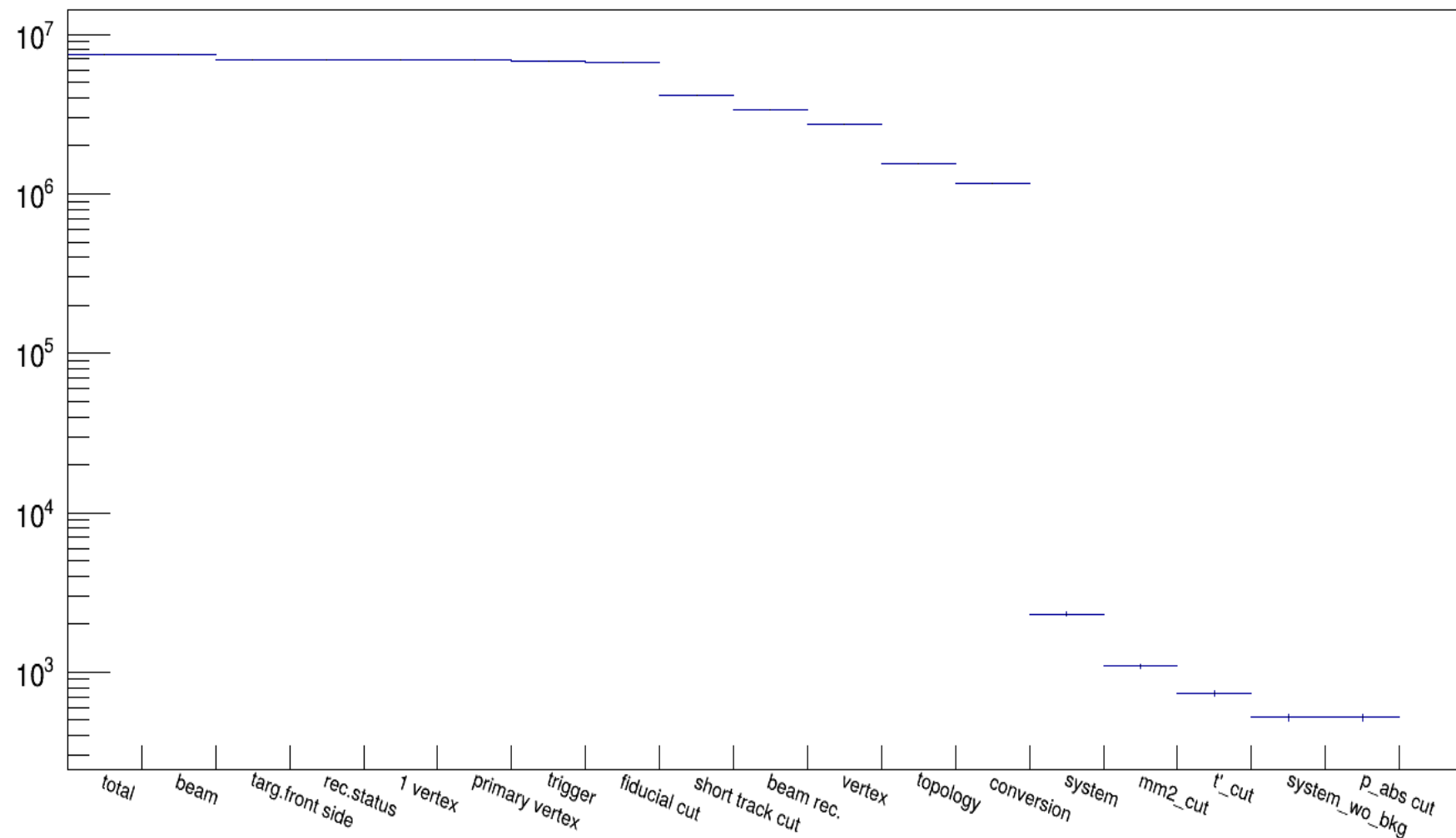


Mass of $gg\ 0^{++}$ in Lattice

TABLE I: Scalar glueball masses (in units of MeV) in quenched (top) and unquenched (bottom) lattice QCD.

Bali <i>et al.</i> (1993) [34]	1550 ± 50
H. Chen <i>et al.</i> (1994) [37]	1740 ± 71
Morningstar, Peardon (1999) [38]	$1730 \pm 50 \pm 80$
Vaccarino, Weingarten (1999) [39]	1648 ± 58
Loan <i>et al.</i> (2005) [40]	1654 ± 83
Y. Chen <i>et al.</i> (2006) [33]	$1710 \pm 50 \pm 80$
Gregory <i>et al.</i> (2012) [41]	1795 ± 60

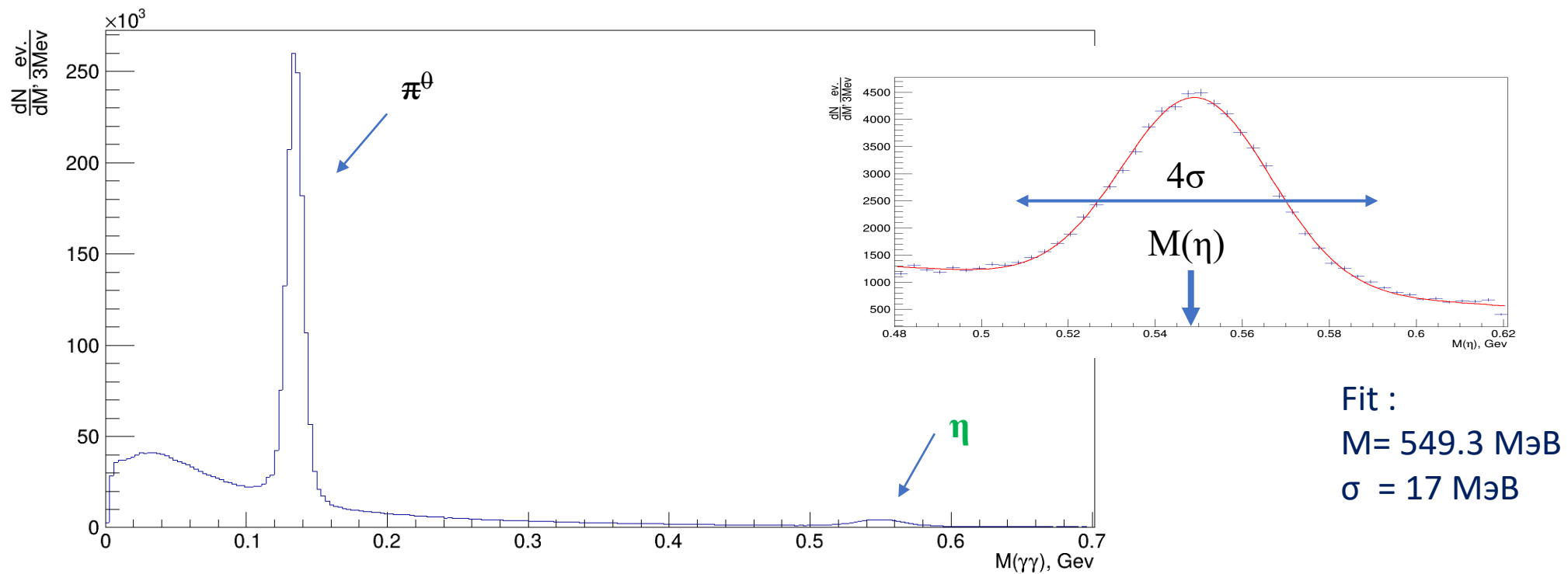
Прохождение отборов $\eta' \pi \pi$



Иллюстрации к отборам

$$\eta' \rightarrow \pi^+ \pi^- \eta \rightarrow \pi^+ \pi^- 2\gamma$$

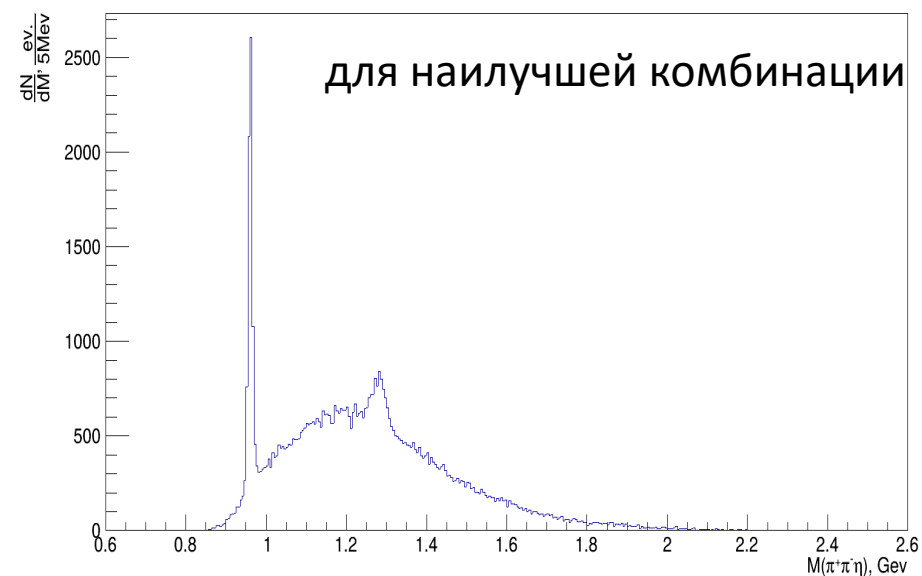
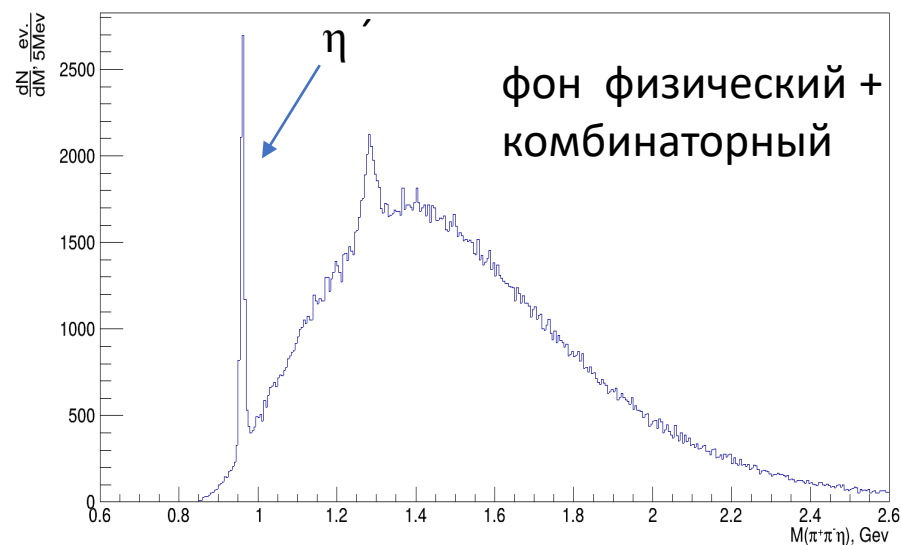
Спектр инв. масс 2γ



Иллюстрации к отборам (2)

$$\eta' \rightarrow \pi^+ \pi^- \eta \rightarrow \pi^+ \pi^- 2\gamma \quad (\text{Мода 2TPL})$$

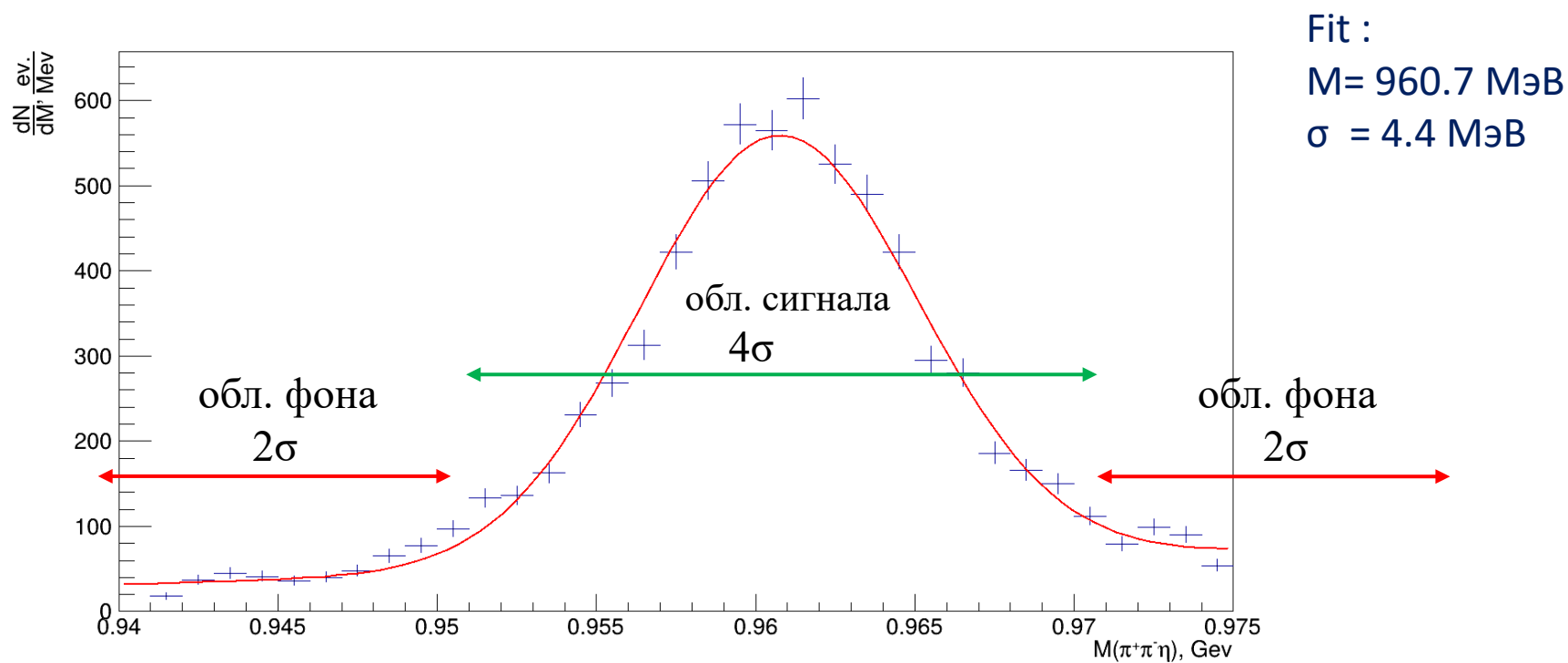
Спектр инв. масс $\pi\pi\eta$



Иллюстрации к отборам (3)

$$\eta' \rightarrow \pi^+ \pi^- \eta \rightarrow \pi^+ \pi^- 2\gamma \quad (\text{Мода 2TPL})$$

Спектр инв. масс $\pi\pi\eta$ (область η')



Об эффективности

- Усредненно по всем переменным системы «верхней» вершины, кроме m_s — массы $\eta' \pi^+ \pi^-$
- Наблюдается факторизация эффективности по «верхней» и «нижней» вершинам
- Для нижней вершины аргумент mm^2 включает (квадрат) массу отдачи **и характер распада**

$$\epsilon_{tot}(m_s, mm^2) = \epsilon_1(m_s) \cdot \epsilon_2(mm^2)$$

$$\epsilon_{tot}(m_s) = \int \epsilon_1(m_s) \cdot \epsilon_2(mm^2) d(mm^2) = \epsilon_2 \cdot \epsilon_1(m_s)$$

$$\epsilon_{tot}(m_s, n) = \epsilon_2(n) \cdot \epsilon_1(m_s)$$

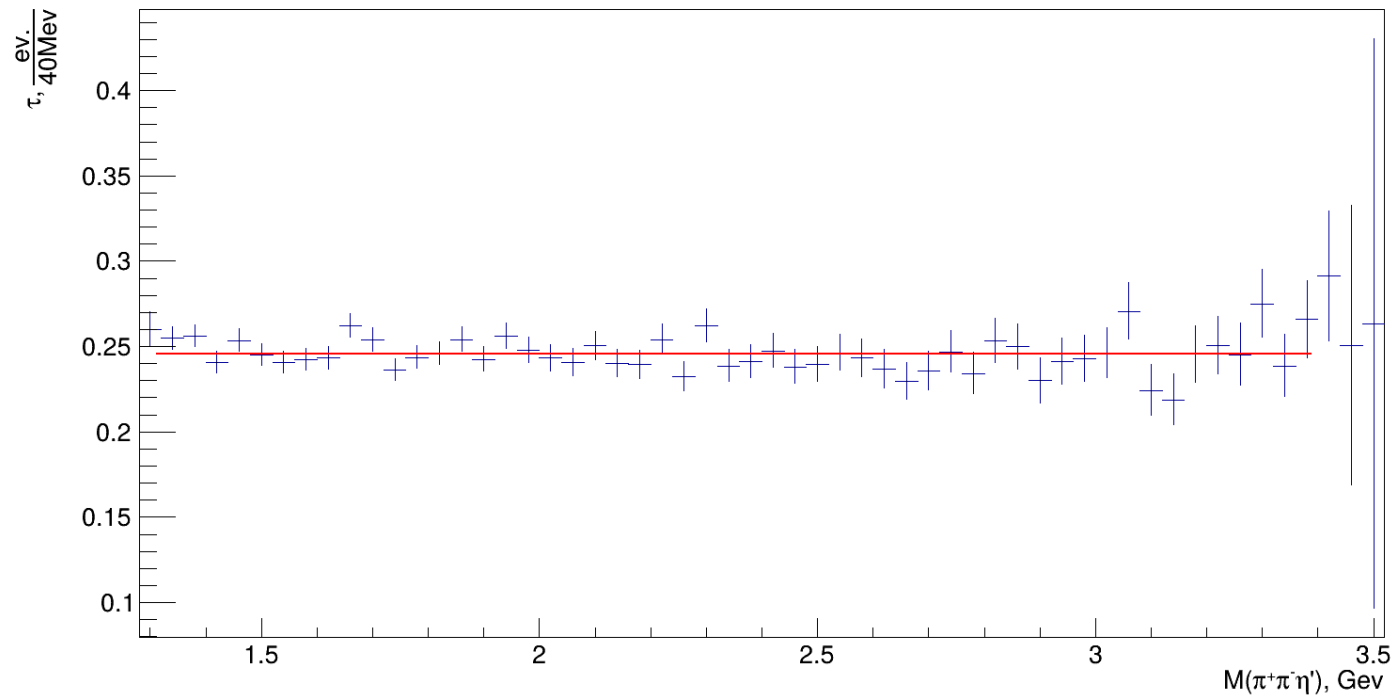
$$\epsilon_{tot}(m_s, \Delta) = \epsilon_2(\Delta) \cdot \epsilon_1(m_s)$$

$$\tau = \epsilon_{tot}(m_s, \Delta) / \epsilon_{tot}(m_s, n) = \epsilon_2(\Delta) / \epsilon_2(n)$$

Об эффективности (2)

Отношение τ эффективностей в триггере MAIN

для реакций $\pi^- p \rightarrow n \eta' \pi^+ \pi^-$ и $\pi^- N \rightarrow \Delta \eta' \pi^+ \pi^-$

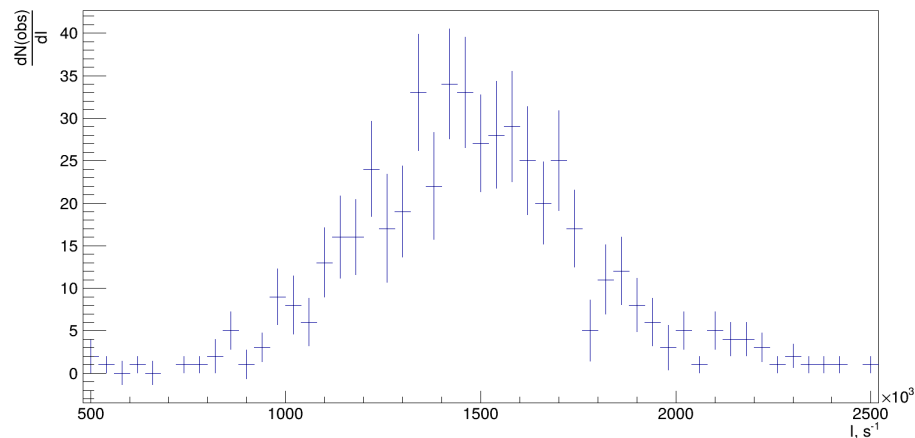


$$\tau = \text{const}(m_s)$$

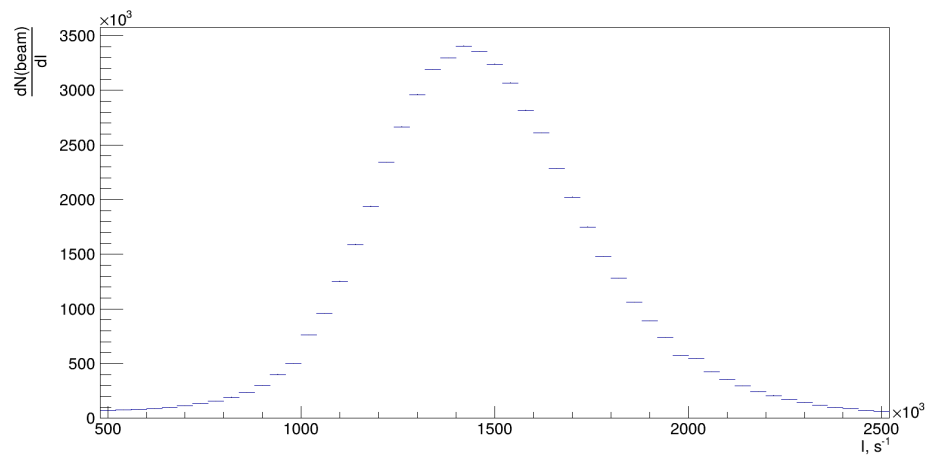
$$\tau(\text{Trig=MWG}) \sim 0.9$$

$$\tau(\text{Trig=MAIN}) \ll 1 \quad \text{из-за VETO}$$

Об эффективности (3)



Распределение по интенсивности пучка для событий изучаемой реакции



Распределение по интенсивности пучка для пучковых событий

X-section. Recoil model

$\Delta(1232)$

$$p\pi^- \rightarrow \Delta^0 \rightarrow p\pi^- \quad 4 \cdot 1 \cdot 1/3 = 4/3$$

$$p\pi^- \rightarrow \Delta^- \rightarrow n\pi^0 \quad 4 \cdot 1 \cdot 2/3 = 8/3$$

$$n\pi^- \rightarrow \Delta^- \rightarrow n\pi^- \quad 5 \cdot 3 \cdot 1 = 15$$

$$p\pi^- \rightarrow \Delta^0 \rightarrow \Delta^0\pi^0 \rightarrow p\pi^-\pi^0 \quad 4 \cdot 1 \cdot 1/15 \cdot 1/3 = 4/45$$

$$p\pi^- \rightarrow \Delta^0 \rightarrow \Delta^0\pi^0 \rightarrow n\pi^0\pi^0 \quad 4 \cdot 1 \cdot 1/15 \cdot 2/3 = 8/45$$

$$p\pi^- \rightarrow \Delta^0 \rightarrow \Delta^-\pi^+ \rightarrow n\pi^-\pi^+ \quad 4 \cdot 1 \cdot 2/5 \cdot 1 = 8/5$$

$$p\pi^- \rightarrow \Delta^0 \rightarrow \Delta^+\pi^- \rightarrow p\pi^0\pi^- \quad 4 \cdot 1 \cdot 8/15 \cdot 2/3 = 64/45$$

$$p\pi^- \rightarrow \Delta^0 \rightarrow \Delta^+\pi^- \rightarrow n\pi^+\pi^- \quad 4 \cdot 1 \cdot 8/15 \cdot 1/3 = 32/45$$

$$n\pi^- \rightarrow \Delta^- \rightarrow \Delta^-\pi^0 \rightarrow n\pi^-\pi^0 \quad 5 \cdot 3 \cdot 3/5 \cdot 1 = 9$$

$$n\pi^- \rightarrow \Delta^- \rightarrow \Delta^0\pi^- \rightarrow p\pi^-\pi^- \quad 5 \cdot 3 \cdot 2/5 \cdot 1/3 = 2$$

$$n\pi^- \rightarrow \Delta^- \rightarrow \Delta^0\pi^- \rightarrow n\pi^0\pi^- \quad 5 \cdot 3 \cdot 2/5 \cdot 2/3 = 4$$

« $\Delta(1600)$ »

Effective description for high-end tail
in mm²

$\rho(2150)$ REFERENCES

ABLIKIM 21A PL B813 136059 M. Ablikim et al. (BESIII Collab.)

ABLIKIM 21X PR D103 072007 M. Ablikim et al. (BESIII Collab.)