

Azimuthal modulation in diffractive vector meson production in ultraperipheral collisions

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Outline



- Introduction to UPC and linearly polarized photon
- Probe nucleon structure in photon-induced diffractive process by using linearly polarized photon in UPC and EICs

Equivalent photon approximation (EPA)



Over 100 years

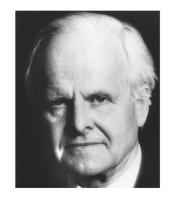
1. 1924, Fermi; "...consider that when a charged particle passes near a point, it produces, at that point, a variable electric field. If we decompose this field, via a Fourier transform, into its harmonic components we find that it is equivalent to the electric field at the same point if it were struck by light with an appropriate continuous distribution of frequencies.



arXiv:hep-th/0205086, Persico remarks that this was one of Fermi's favorite ideas and that he often used it in later life.

2. 1930's, Weizäscker and Williams (individually); developed to relativistic charged particles, method of virtual quanta

photon flux:
$$n(\omega) = \frac{4Z^2 \alpha_e}{\omega} \int \frac{d^2 k_{\perp}}{(2\pi)^2} k_{\perp}^2 \left[\frac{F(k_{\perp}^2 + \omega^2/\gamma^2)}{(k_{\perp}^2 + \omega^2/\gamma^2)} \right]^2$$





Ultraperipheral collision (UPC) in heavy-ion collisions



cross section in $\gamma-\gamma$ processes in heavy-ion collisions:

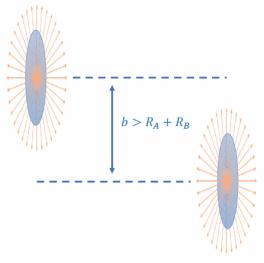
$$\sigma^{WW}_{A_1A_2\to A_1A_2X} = \int d\omega_1 d\omega_2 n_{A_1}(\omega_1) n_{A_2}(\omega_2) \sigma_{\gamma\gamma\to X}(\omega_1,\omega_2)$$

$$\gamma - \gamma$$
: $d\sigma \propto Z^4$ e.g. Au, 79^4=3.9*10^7
 $\gamma - A$: $d\sigma \propto Z^2$

But! strong interaction dominant in center collisions

• UPC

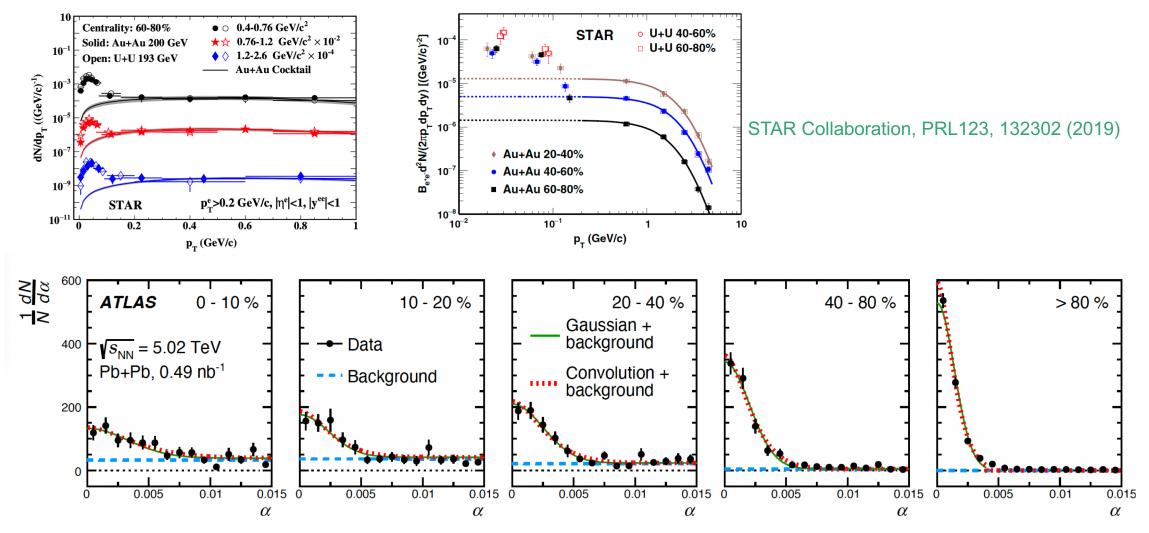
Two nuclei physically miss each other, interact (only) electromagnetically



Clean background

Measurements of dilepton in UPC at STAR and ATLAS





ATLAS Collaboration, PRL 121, 212301 (2018)



Low electron energy, Sommerfeld, 1931

ANNALEN DER PHYSIK

5. FOLGE, 1931, BAND 11, HEFT 3

Über die Beugung und Bremsung der Elektronen Von A. Sommerfeld

(Mit 12 Figuren)

Übersicht: Der I. Teil bildet eine systematische Einleitung zu der Behandlung des kontinuierlichen Röntgenspektrums im II. Teil. Der I. Teil geht nur in der Methode, nicht in den Resultaten über die Arbeiten von Gordon, Mott, Temple hinaus. Der II. Teil setzt, im Gegensatz zu Arbeiten von Oppenheimer und Sugiura den Endzustand des gebremsten Elektrons als ebene, durch Beugung modifizierte Welle an. Polarisation und Intensität im kontinuierlichen Spektrum werden nach der Methode der Matrixelemente berechnet. Um die azimutale Verteilung der Intensität, insbesondere die Voreilung des Maximums zu erhalten, muß die Rechenmethode verfeinert werden durch Berücksichtigung der Retardierung. Die Resultate werden mit Messungen von Kulenkampff verglichen.

relativistic energies, May, Wick, 1951

Detection of Gamma-Ray Polarization by Pair Production*

G. C. WICK Radiation Laboratory, University of Californ December 12, 1950

T has been pointed out by Yang,1 the provide a method for detecting the p the high energy range: $h\nu\gg mc^2$ (m be where the usual Compton recoil method b idea is to utilize the azimuthal dependenc cross section $d\sigma$, the azimuth ϕ being taining k and the electric polarization ve

On the Production of Polarized High Energy X-Rays

M. MAY AND G. C. WICK Department of Physics, University of California, Berkeley, California December 12, 1950

THE purpose of this note is to examine the possibility of experiments with polarized x-rays of high energy, the polarization direction k of the incident quantum an being obtained by using only a portion of the x-ray beam emitted (by a betatron, synchrotron, or linear-accelerator target) at an angle θ to the direction of the electron beam. The optimum angle,

PHYSICAL REVIEW

VOLUME 84. NUMBER 2

OCTOBER 15, 1951

On the Polarization of High Energy Bremsstrahlung and of High Energy Pairs

MICHAEL M. MAY Physics Department, University of California, Berkeley, California (Received July 2, 1951)

The polarization of bremsstrahlung due to electrons with initial energies much larger than 137Z-i mc² is calculated under relativistic, small angles approximations. The cross section for photons polarized normally to the plane containing the initial direction of the electron and the direction of the photon is found to be larger than for photons polarized in that plane. A similar calculation shows that the plane containing one of a pair produced by a polarized photon together with the direction of that photon tends to lie parallel to the plane of polarization rather than normal to it, except for one special case. The effect of the deviation due to multiple scattering of electrons in the target upon the angular dependence of the polarization is considered.



• EPA photons induced by relativistically moving charged particles are linearly polarized due to their transverse momentum

In position space

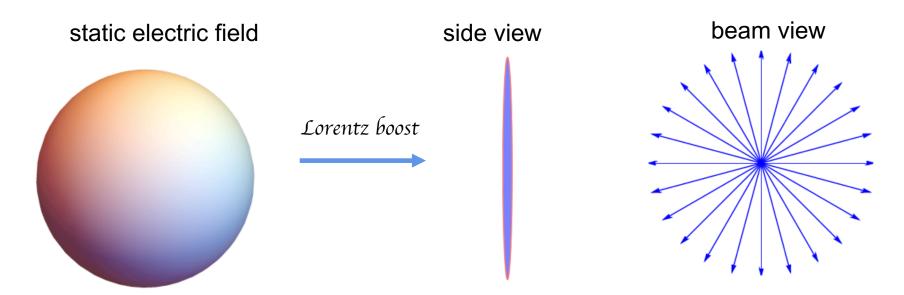
static electric field





• EPA photons induced by relativistically moving charged particles are linearly polarized due to their transverse momentum

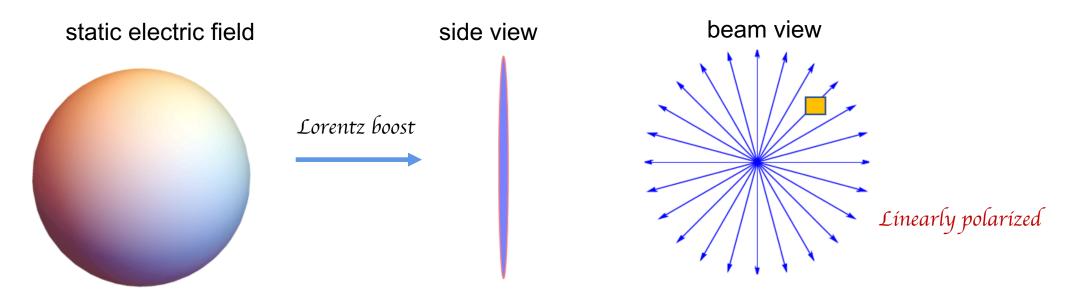
In position space





• EPA photons induced by relativistically moving charged particles are linearly polarized due to their transverse momentum

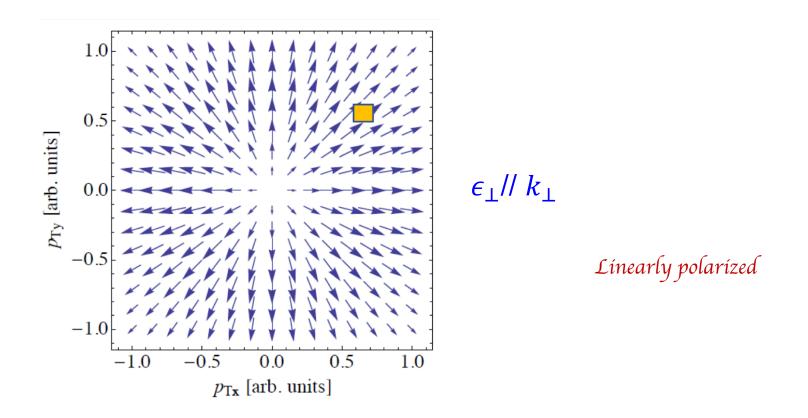
In position space





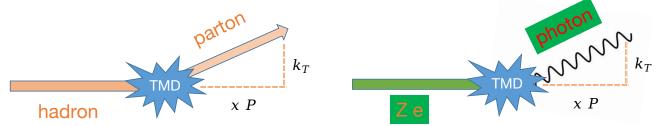
• EPA photons induced by relativistically moving charged particles are linearly polarized due to their transverse momentum

In momentum space



Linearly polarized photon/gluon, formalism in the framework of TMD (transverse-momentum-dependent) factorization

• gluon/photon TMD factorization:



$$\int \frac{2 dy^- d^2 y_\perp}{x P^+ (2\pi)^3} e^{i k \cdot y} \langle P | F_+^\mu(0) F_+^\nu(y) | P \rangle \Big|_{y^+ = 0} = \delta_\perp^{\mu\nu} f_1(x, k_\perp^2) + \left(\frac{2 k_\perp^\mu k_\perp^\nu}{k_\perp^2} - \delta_\perp^{\mu\nu} \right) h_1^\perp(x, k_\perp^2),$$
 P. Mulders, J. Rodrigues, PRD63(2001)

the numbers of gluons with opposite circular polarizations in a longitudinally (transversely) polarized nucleon. The off-diagonal function H^{\perp} also is a difference of densities, but in this case of linearly polarized gluons in an unpolarized hadron. Using the circular polarizations, H^{\perp} flips the polarization.

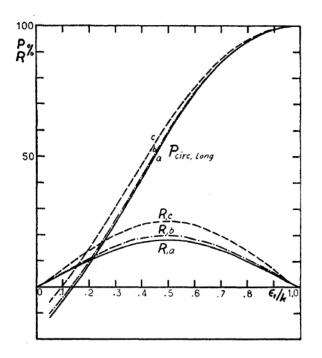
• Small x (dipole) gluons/photons are highly linearly polarized A. Metz, J. Zhou, PRD84(2011) $f_1(x,k_\perp^2) = h_1^\perp(x,k_\perp^2)$ C. Li, J. Zhou, YZ, PLB795(2019)

How to probe linearly polarized photon/gluon, examples



Early studies about linearly polarized photon

$$R = \frac{d\sigma(\hat{\mathbf{u}} = \mathbf{e}) - d\sigma(\hat{\mathbf{u}} \cdot \mathbf{e} = 0)}{d\sigma(\hat{\mathbf{u}} = \mathbf{e}) + d\sigma(\hat{\mathbf{u}} \cdot \mathbf{e} = 0)}$$

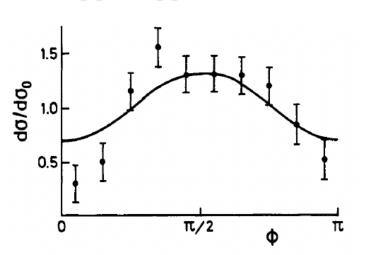


H.Olsen, L.C. Maximon, Phys.Rev. 114 (1959) 887-904

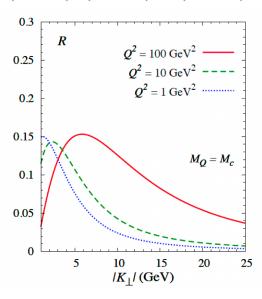
azimuthal modulations induced by linearly polarized gluon

$$pp \rightarrow pp\pi^+\pi^-$$

 $e(\ell)+h(P)\to e(\ell')+Q(K_1)+\bar{Q}(K_2)+X$



T. Jacobsen, H. Olsen, Phys.Scripta 42(1990)



$$R = \left| \frac{\int d^2 \mathbf{q}_T \ \mathbf{q}_T^2 \cos 2(\phi_T - \phi_\perp) \, d\sigma}{\int d^2 \mathbf{q}_T \ \mathbf{q}_T^2 \, d\sigma} \right|$$

D.Boer, S. Brodsky, P. Mulders, C. Pisano, SLAC-PUB-14359 (2010)

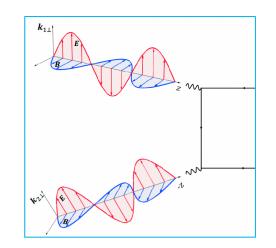
Azimuthal asymmetry in dilepton production in UPC

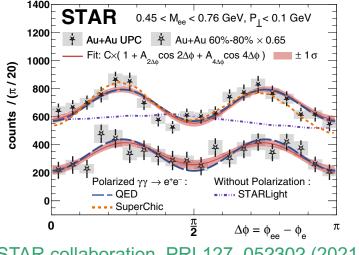


$$\gamma(x_1P + k_{1\perp}) + \gamma(x_2\bar{P} + k_{2\perp}) \rightarrow l^+(p_1) + l^-(p_2)$$

$$\frac{d\sigma}{d^2 \boldsymbol{p}_{1\perp} d^2 \boldsymbol{p}_{2\perp} dy_1 dy_2} = \frac{2\alpha_e^2}{Q^4} \left[\mathcal{A} + \mathcal{B} \cos 2\phi + \mathcal{C} \cos 4\phi \right]$$

$$f_1^{\gamma}(x_1, k_{1\perp}^2) h_1^{\perp \gamma}(x_2, k_{2\perp}^2)$$
 $h_1^{\perp \gamma}(x_1, k_{1\perp}^2) h_1^{\perp \gamma}(x_2, k_{2\perp}^2)$





STAR collaboration, PRL127, 052302 (2021)

	Measured	QED calculation
Tagged UPC	$16.8\% \pm 2.5\%$	16.5%
60%-80%	$27\% \pm 6\%$	34.5%

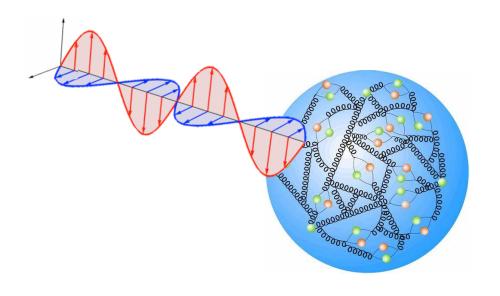
C. Li, J. Zhou and YZ, PLB795, 576(2019)

C. Li, J. Zhou and YZ, PRD101, 034015(2020)

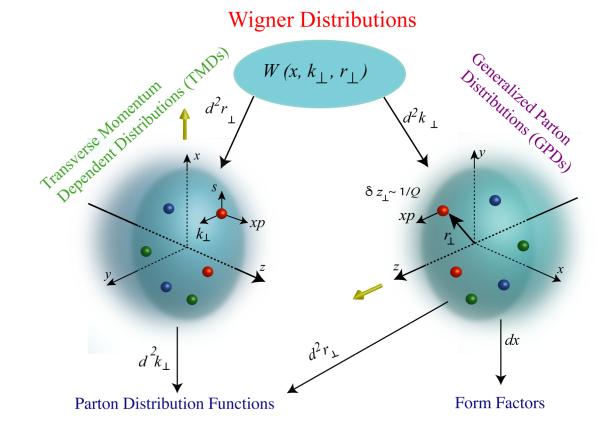
We predicted the azimuthal asymmetries in dilepton@UPC, later verified by STAR

UPC: an ideal platform to "see" nucleus





- √ linearly polarized photon
- √ high luminosity
- √ clean background
- **√** ...



How? photo-nuclear diffractive production of vector mesons, di-jets...

Probing gluon tomography using photon

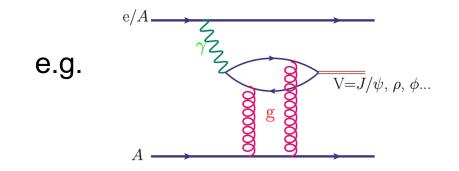


• semi-inclusive processes

e.g.

exclusive processes

Probe gluon TMD (transverse momentum dependent distributions)

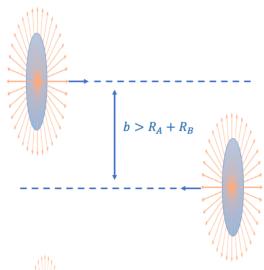


Probe gluon Wigner distributions, GPD (transverse spatial distributions)

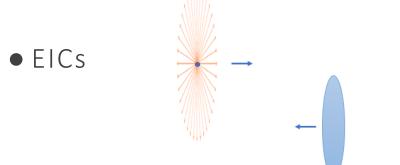
Two platforms to probe gluon tomography in diffractive photoproduction processes



Ultra-peripheral collisions (UPCs)

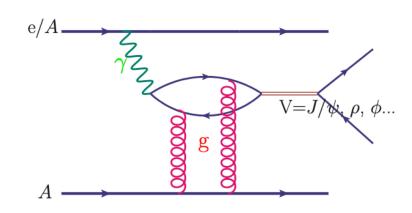


Double-slit interference

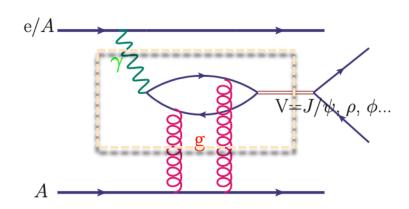


One-slit interference





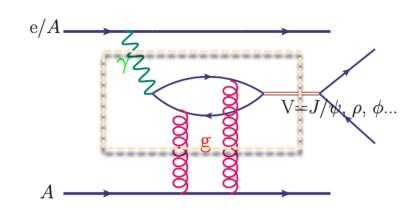




$$\mathcal{A}(\Delta_{\perp}) = i \int d^2b_{\perp}e^{i\Delta_{\perp}\cdot b_{\perp}} \int \frac{d^2r_{\perp}}{4\pi} \int_0^1 dz \, \Psi^{\gamma \to q\bar{q}}(r_{\perp}, z, \epsilon_{\perp}^{\gamma}) N(r_{\perp}, b_{\perp}) \Psi^{V \to q\bar{q}*}(r_{\perp}, z, \epsilon_{\perp}^{V}),$$

For polarization averaged calculation, see: M. G. Ryskin, 93; S. J. Brodsky, L. Frankfurt, J. F. Gunion, A. H. Mueller and M. Strikman, 94





$$\epsilon_{\perp}^{\gamma}
ightarrow \epsilon_{\perp}^{V},$$
 unique observables :

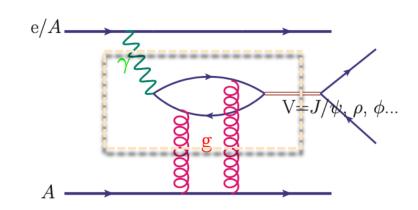
$$\langle \cos(n\phi) \rangle = \frac{\int \frac{d\sigma}{d\mathcal{P}.\mathcal{S}.} \cos(n\phi) d\mathcal{P}.\mathcal{S}.}{\int \frac{d\sigma}{d\mathcal{P}.\mathcal{S}.} d\mathcal{P}.\mathcal{S}.}$$

where
$$\phi = q_{\perp} \wedge p_{\perp}^{l}$$

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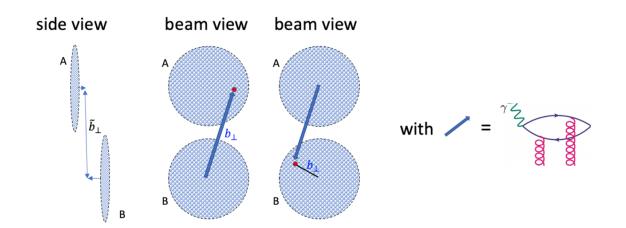
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For polarization averaged calculation, see: M. G. Ryskin, 93; S. J. Brodsky, L. Frankfurt, J. F. Gurlion, A. H. Mueller and M. Strikman, 94

dipole amplitude

Joint \widetilde{b}_{\perp} and q_{\perp} picture





A,B take turns to be the source of color dipole

 \tilde{b}_{\perp} : impact parameter

 b_{\perp} : the position of the produced V $(\lambda_{J/\psi} \ll R_A)$

 $b_{\perp} \leftrightarrow q_{\perp}$

Coherent cs: summing up amplitudes → squaring it

Incoherent cs: squaring the amplitude → summing up

coherent dominant at low k_{\perp} ($\leq \sim \frac{1}{R_A}$, \sim 30 MeV for Au and Pb)

interference effect



coherent production amplitude:

$$\mathcal{M}(Y, \tilde{b}_{\perp}) \propto \left[F_B(Y, b_{\perp} - \tilde{b}_{\perp}) N_A(Y, b_{\perp}) + N_B(-Y, b_{\perp} - \tilde{b}_{\perp}) F_A(-Y, b_{\perp}) \right]$$

Fourier transform $b_{\perp} \rightarrow q_{\perp}$,

$$\mathcal{M}(Y, \tilde{b}_{\perp}) \propto \int d^2k_{\perp} d^2\Delta_{\perp} \delta^2(q_{\perp} - \Delta_{\perp} - k_{\perp})$$

$$\left\{ F_B(Y, k_{\perp}) N_A(Y, \Delta_{\perp}) e^{-i\tilde{b}_{\perp} \cdot k_{\perp}} + F_A(-Y, k_{\perp}) N_B(-Y, \Delta_{\perp}) e^{-i\tilde{b}_{\perp} \cdot \Delta_{\perp}} \right\},$$

Classical:

Light
Source

Source

Min

Max

(n = 1)

Min

Max

(n = 1)

Min

Max

(n = 2)

Min

Max

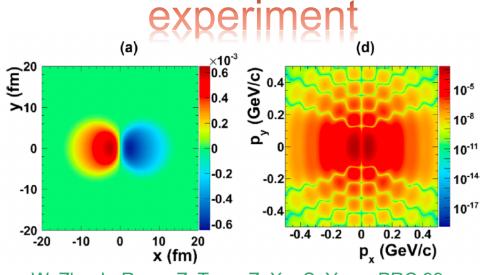
(n = 2)

Screen

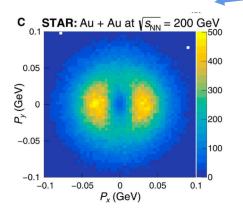
Double slit like interference effect

interference effect

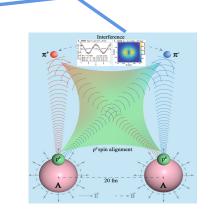




W. Zha, L. Ruan, Z. Tang, Z. Xu, S. Yang, PRC 99, 061901 (2019)



STAR collaboration, Sci.Adv. 9, eabq3903 (2023)



Y.G. Ma, Nucl. Sci. Tech. 34, 16 (2023)

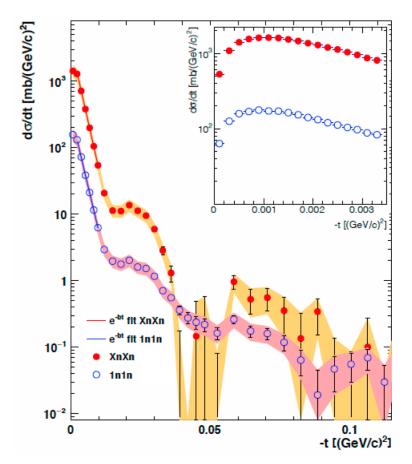
theory

$$\frac{d\sigma}{d^{2}q_{\perp}dYd^{2}\tilde{b}_{\perp}} = \frac{1}{(2\pi)^{4}} \int d^{2}\Delta_{\perp}d^{2}k_{\perp}d^{2}k'_{\perp}\delta^{2}(k_{\perp} + \Delta_{\perp} - q_{\perp})(\epsilon_{\perp}^{V*} \cdot \hat{k}_{\perp})(\epsilon_{\perp}^{V} \cdot \hat{k}'_{\perp}) \left\{ \int d^{2}b_{\perp} \times e^{i\tilde{b}_{\perp} \cdot (k'_{\perp} - k_{\perp})} \left[T_{A}(b_{\perp})\mathcal{A}_{in}(Y, \Delta_{\perp})\mathcal{A}_{in}^{*}(Y, \Delta'_{\perp})\mathcal{F}(Y, k_{\perp})\mathcal{F}(Y, k'_{\perp}) + (A \leftrightarrow B) \right] \right. \\
\left. \times e^{i\tilde{b}_{\perp} \cdot (k'_{\perp} - k_{\perp})} \mathcal{A}_{co}(Y, \Delta_{\perp})\mathcal{A}_{in}^{*}(Y, \Delta'_{\perp})\mathcal{F}(Y, k_{\perp})\mathcal{F}(Y, k'_{\perp}) \right] \\
+ \left[e^{i\tilde{b}_{\perp} \cdot (\Delta'_{\perp} - \Delta_{\perp})} \mathcal{A}_{co}(-Y, \Delta_{\perp})\mathcal{A}_{co}^{*}(-Y, \Delta'_{\perp})\mathcal{F}(-Y, k_{\perp})\mathcal{F}(-Y, k'_{\perp}) \right] \\
+ \left[e^{i\tilde{b}_{\perp} \cdot (\Delta'_{\perp} - k_{\perp})} \mathcal{A}_{co}(Y, \Delta_{\perp})\mathcal{A}_{co}^{*}(-Y, \Delta'_{\perp})\mathcal{F}(Y, k_{\perp})\mathcal{F}(-Y, k'_{\perp}) \right] \\
+ \left[e^{i\tilde{b}_{\perp} \cdot (k'_{\perp} - \Delta_{\perp})} \mathcal{A}_{co}(-Y, \Delta_{\perp})\mathcal{A}_{co}^{*}(Y, \Delta'_{\perp})\mathcal{F}(-Y, k_{\perp})\mathcal{F}(Y, k'_{\perp}) \right] \right\}, \tag{2.14}$$

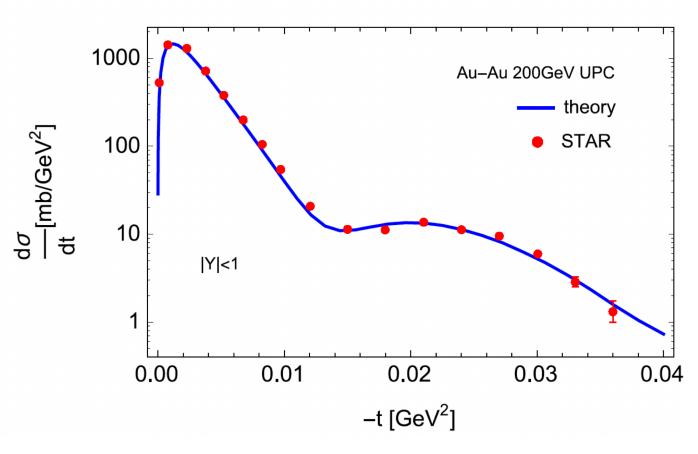
H.X. Xing, C. Zhang, J. Zhou and YZ, JHEP10(2020)064

see also W. Zha, J. D. Brandenburg, L.J. Ruan and Z.B. Tang PRD103, 033007(2021)





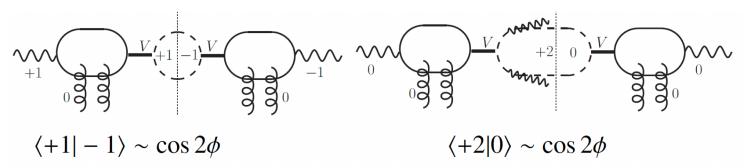
STAR, Phys.Rev.C 96 (2017) 5, 054904

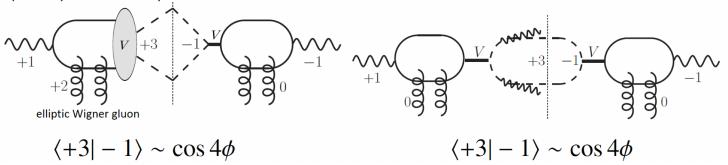


H.X. Xing, C. Zhang, J. Zhou and YZ, JHEP10(2020)064

Azimuthal modulations in diffractive vector meson production in UPC





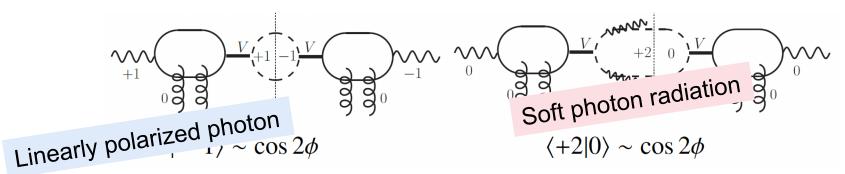


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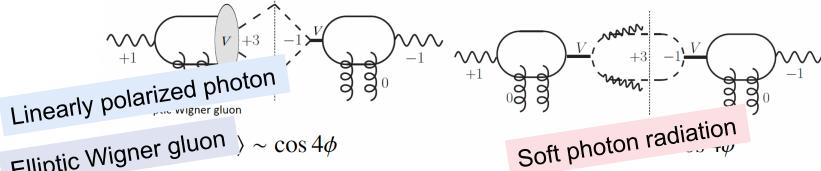
Azimuthal modulations in diffractive vector meson production in UPC



Cos2 asymmetry

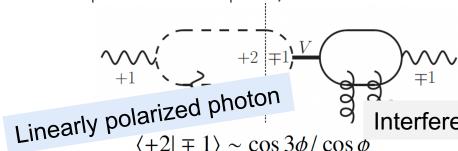


Cos4 asymmetry



Elliptic Wigner gluon $\rangle \sim \cos 4\phi$

Cos
 o and Cos 3
 o asymmetries

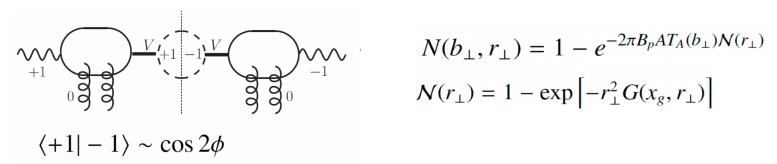


Interference between diffractive $\rho^0 \to \pi\pi$ and direct $\pi\pi$ production

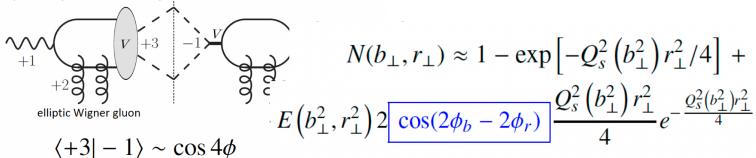
 $\langle +2| \mp 1 \rangle \sim \cos 3\phi / \cos \phi$

Azimuthal modulations in diffractive vector meson production in UPC



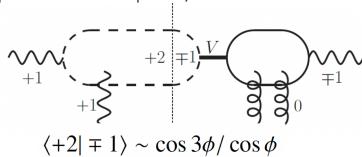


Cos4 asymmetry



Elliptic Wigner gluon

Cosφ and Cos3φ asymmetries

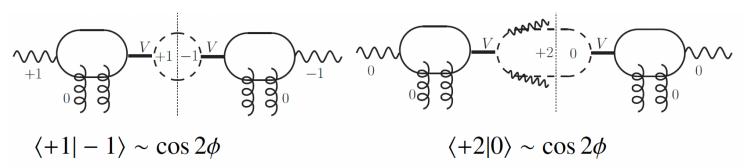


sensitive to nuclear geometry, provide an alternative method to extract transverse spatial gluon distribution.

Azimuthal modulations in diffractive vector meson production in UPC



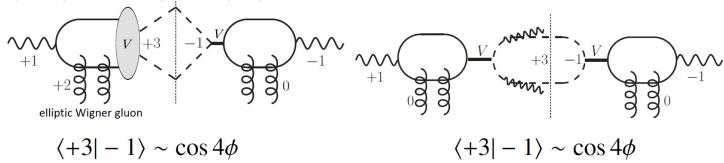
• Cos2 ϕ asymmetry, in ρ^0 production, and J/ ψ production



H.X. Xing, C. Zhang, J. Zhou and YZ, 2020,JHEP

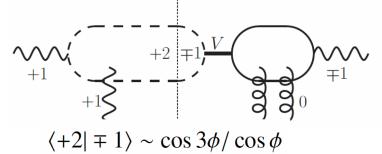
J. D. Brandenburg, Z. Xu, W. Zha, C. Zhang, J. Zhou, YZ, PRD 106, 074008 (2022)

Cos4φ asymmetry, in ρ⁰ production



Y. Hagiwara, C. Zhang, J. Zhou and YZ, PRD.104, 094021(2021)

 \bullet Cos φ and Cos3 φ asymmetries, , in diffractive ρ^0 and direct $\pi\pi$ production

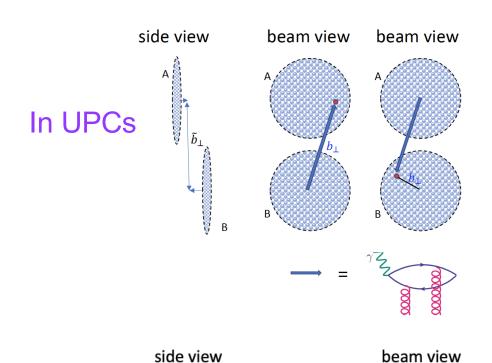


Y. Hagiwara, C. Zhang, J. Zhou and YZ, PRD103.074013(2021)

sensitive to nuclear geometry, provide an alternative method to extract transverse spatial gluon distribution.

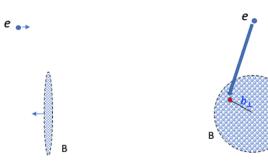
Difference between UPCs and EICs





A,B take turns to be the source of color dipole double-slit interference in UPCs

In EICs



electron provide the photon, one-slit interference



In UPCs

$$\begin{split} &\frac{d\sigma}{d^2p_{1\perp}d^2p_{2\perp}dy_1dy_2d^2\tilde{b}_\perp} \\ &= \frac{\mathcal{C}}{2(2\pi)^7} \frac{24e^4e_q^2}{(Q^2-M^2)^2+M^2\Gamma^2} \frac{|\phi(0)|^2}{M} \int d^2\Delta_\perp d^2k_\perp d^2k'_\perp \delta^2(k_\perp + \Delta_\perp - q_\perp) \left[\hat{k}'_\perp \cdot \hat{k}_\perp - \frac{4(P_\perp \cdot \hat{k}_\perp)(P_\perp \cdot \hat{k}'_\perp)}{M^2}\right] \\ &\times \left\{ \int d^2b_\perp e^{i\tilde{b}_\perp \cdot (k'_\perp - k_\perp)} [T_A(b_\perp)\mathcal{A}_{\rm in}(x_2, \Delta_\perp)\mathcal{A}_{\rm in}^*(x_2, \Delta'_\perp)\mathcal{F}(x_1, k_\perp)\mathcal{F}(x_1, k'_\perp) + (A \leftrightarrow B)] \right. \\ &\quad \left. + \left[e^{i\tilde{b}_\perp \cdot (k'_\perp - k_\perp)} \mathcal{A}_{\rm co}(x_2, \Delta_\perp) \mathcal{A}_{\rm co}^*(x_2, \Delta'_\perp) \mathcal{F}(x_1, k_\perp) \mathcal{F}(x_1, k'_\perp) \right] + \left[e^{i\tilde{b}_\perp \cdot (\Delta'_\perp - \Delta_\perp)} \mathcal{A}_{\rm co}(x_1, \Delta_\perp) \mathcal{A}_{\rm co}^*(x_1, \Delta'_\perp) \mathcal{F}(x_2, k'_\perp) \right] \\ &\quad \left. + \left[e^{i\tilde{b}_\perp \cdot (\Delta'_\perp - k_\perp)} \mathcal{A}_{\rm co}(x_2, \Delta_\perp) \mathcal{A}_{\rm co}^*(x_1, \Delta'_\perp) \mathcal{F}(x_1, k_\perp) \mathcal{F}(x_2, k'_\perp) \right] + \left[e^{i\tilde{b}_\perp \cdot (k'_\perp - \Delta_\perp)} \mathcal{A}_{\rm co}(x_1, \Delta_\perp) \mathcal{A}_{\rm co}^*(x_2, \Delta'_\perp) \mathcal{F}(x_2, k_\perp) \mathcal{F}(x_1, k'_\perp) \right] \right\} \end{split}$$



In UPCs

$$\frac{d\sigma}{d^2p_{1\perp}d^2p_{2\perp}dy_1dy_2d^2\tilde{b}_\perp} \\ = \frac{\mathcal{C}}{2(2\pi)^7} \frac{24e^4e_q^2}{(Q^2-M^2)^2+M^2\Gamma^2} \frac{|\phi(0)|^2}{M} \int d^2\Delta_\perp d^2k_\perp d^2k'_\perp \delta^2(k_\perp + \Delta_\perp - q_\perp) \left[\hat{k}'_\perp \cdot \hat{k}_\perp - \frac{4(P_\perp \cdot \hat{k}_\perp)(P_\perp \cdot \hat{k}'_\perp)}{M^2}\right] \\ \times \left\{ \int d^2b_\perp e^{i\tilde{b}_\perp \cdot (k'_\perp - k_\perp)} [T_A(b_\perp) \mathcal{A}_{\text{in}}(x_2, \Delta_\perp) \mathcal{A}_{\text{in}}^*(x_2, \Delta'_\perp) \mathcal{F}(x_1, k_\perp) \mathcal{F}(x_1, k'_\perp) + (A \leftrightarrow B)] \right. \\ \left. + \left[e^{i\tilde{b}_\perp \cdot (k'_\perp - k_\perp)} \mathcal{A}_{\text{co}}(x_2, \Delta_\perp) \mathcal{A}_{\text{co}}^*(x_2, \Delta'_\perp) \mathcal{F}(x_1, k_\perp) \mathcal{F}(x_1, k'_\perp) \right] + \left[e^{i\tilde{b}_\perp \cdot (\Delta'_\perp - \Delta_\perp)} \mathcal{A}_{\text{co}}(x_1, \Delta'_\perp) \mathcal{F}(x_2, k_\perp) \mathcal{F}(x_2, k'_\perp) \right] \\ \left. + \left[e^{i\tilde{b}_\perp \cdot (\Delta'_\perp - k_\perp)} \mathcal{A}_{\text{co}}(x_2, \Delta_\perp) \mathcal{A}_{\text{co}}^*(x_1, \Delta'_\perp) \mathcal{F}(x_1, k_\perp) \mathcal{F}(x_2, k'_\perp) \right] + \left[e^{i\tilde{b}_\perp \cdot (k'_\perp - \Delta_\perp)} \mathcal{A}_{\text{co}}(x_1, \Delta_\perp) \mathcal{A}_{\text{co}}^*(x_2, \Delta'_\perp) \mathcal{F}(x_2, k_\perp) \mathcal{F}(x_1, k'_\perp) \right] \right\}$$



In UPCs

$$\frac{d\sigma}{d^2p_{1\perp}d^2p_{2\perp}dy_1dy_2d^2\tilde{b}_\perp} \\ = \frac{\mathcal{C}}{2(2\pi)^7} \frac{24e^4e_q^2}{(Q^2-M^2)^2+M^2\Gamma^2} \frac{|\phi(0)|^2}{M} \int d^2\Delta_\perp d^2k_\perp d^2k'_\perp \delta^2(k_\perp + \Delta_\perp - q_\perp) \left[\hat{k}'_\perp \cdot \hat{k}_\perp - \frac{4(P_\perp \cdot \hat{k}_\perp)(P_\perp \cdot \hat{k}'_\perp)}{M^2}\right] \\ \times \left\{ \int d^2b_\perp e^{i\tilde{b}_\perp \cdot (k'_\perp - k_\perp)} [T_A(b_\perp) \mathcal{A}_{\rm in}(x_2, \Delta_\perp) \mathcal{A}_{\rm in}^*(x_2, \Delta'_\perp) \mathcal{F}(x_1, k_\perp) \mathcal{F}(x_1, k'_\perp) + (A \Leftrightarrow B)] \right. \\ \left. + \left[e^{i\tilde{b}_\perp \cdot (k'_\perp - k_\perp)} \mathcal{A}_{\rm co}(x_2, \Delta_\perp) \mathcal{A}_{\rm co}^*(x_2, \Delta'_\perp) \mathcal{F}(x_1, k_\perp) \mathcal{F}(x_1, k'_\perp) \right] + \left[e^{i\tilde{b}_\perp \cdot (\Delta'_\perp - \Delta_\perp)} \mathcal{A}_{\rm co}(x_1, \Delta_\perp) \mathcal{A}_{\rm co}^*(x_1, \Delta'_\perp) \mathcal{F}(x_2, k'_\perp) \right] \\ \left. + \left[e^{i\tilde{b}_\perp \cdot (\Delta'_\perp - k_\perp)} \mathcal{A}_{\rm co}(x_2, \Delta_\perp) \mathcal{A}_{\rm co}^*(x_1, \Delta'_\perp) \mathcal{F}(x_1, k_\perp) \mathcal{F}(x_2, k'_\perp) \right] + \left[e^{i\tilde{b}_\perp \cdot (\Delta'_\perp - \Delta_\perp)} \mathcal{A}_{\rm co}(x_1, \Delta_\perp) \mathcal{A}_{\rm co}^*(x_2, \Delta'_\perp) \mathcal{F}(x_2, k'_\perp) \right] \right\} \\ \left. + \left[e^{i\tilde{b}_\perp \cdot (\Delta'_\perp - k_\perp)} \mathcal{A}_{\rm co}(x_2, \Delta_\perp) \mathcal{A}_{\rm co}^*(x_1, \Delta'_\perp) \mathcal{F}(x_1, k_\perp) \mathcal{F}(x_2, k'_\perp) \right] + \left[e^{i\tilde{b}_\perp \cdot (\Delta'_\perp - \Delta_\perp)} \mathcal{A}_{\rm co}(x_1, \Delta_\perp) \mathcal{A}_{\rm co}^*(x_2, \Delta'_\perp) \mathcal{F}(x_2, k_\perp) \mathcal{F}(x_1, k'_\perp) \right] \right\} \\ \left. + \left[e^{i\tilde{b}_\perp \cdot (\Delta'_\perp - k_\perp)} \mathcal{A}_{\rm co}(x_2, \Delta_\perp) \mathcal{A}_{\rm co}^*(x_1, \Delta'_\perp) \mathcal{F}(x_1, k_\perp) \mathcal{F}(x_2, k'_\perp) \right] + \left[e^{i\tilde{b}_\perp \cdot (\Delta'_\perp - \Delta_\perp)} \mathcal{A}_{\rm co}(x_1, \Delta_\perp) \mathcal{A}_{\rm co}^*(x_2, \Delta'_\perp) \mathcal{F}(x_1, k'_\perp) \right] \right\} \\ \left. + \left[e^{i\tilde{b}_\perp \cdot (\Delta'_\perp - k_\perp)} \mathcal{A}_{\rm co}(x_2, \Delta_\perp) \mathcal{A}_{\rm co}^*(x_1, \Delta'_\perp) \mathcal{F}(x_1, k_\perp) \mathcal{F}(x_2, k'_\perp) \right] + \left[e^{i\tilde{b}_\perp \cdot (\Delta'_\perp - \Delta_\perp)} \mathcal{A}_{\rm co}(x_1, \Delta_\perp) \mathcal{A}_{\rm co}^*(x_2, \Delta'_\perp) \mathcal{F}(x_1, k'_\perp) \right] \right\} \\ \left. + \left[e^{i\tilde{b}_\perp \cdot (\Delta'_\perp - k_\perp)} \mathcal{A}_{\rm co}(x_2, \Delta_\perp) \mathcal{A}_{\rm co}^*(x_1, \Delta'_\perp) \mathcal{F}(x_1, k'_\perp) \mathcal{F}(x_2, k'_\perp) \right] \right] \\ \left. + \left[e^{i\tilde{b}_\perp \cdot (\Delta'_\perp - k_\perp)} \mathcal{A}_{\rm co}(x_2, \Delta_\perp) \mathcal{A}_{\rm co}^*(x_1, \lambda'_\perp) \mathcal{F}(x_1, k'_\perp) \mathcal{F}(x_2, k'_\perp) \right] \right] \right\} \\ \left. \left[e^{i\tilde{b}_\perp \cdot (\Delta'_\perp - k_\perp)} \mathcal{A}_{\rm co}(x_2, \Delta_\perp) \mathcal{A}_{\rm co}^*(x_1, \lambda'_\perp) \mathcal{F}(x_1, k'_\perp) \mathcal{F}(x_2, k'_\perp) \right] \right] \\ \left. + \left[e^{i\tilde{b}_\perp \cdot (\Delta'_\perp - k_\perp)} \mathcal{A}_{\rm co}(x_1, \Delta'_\perp) \mathcal{A}_{\rm co}^*(x_1, \lambda'_\perp) \mathcal{F}(x_1, k'_\perp) \right] \right] \right] \right] \\ \left. \left[e^{i\tilde{b}_\perp \cdot (\Delta'_\perp - k_\perp)} \mathcal{A}_{\rm co}(x_1, \lambda'_\perp) \mathcal{A}_{\rm co}^*(x_1, \lambda'_\perp) \mathcal{F}(x_1,$$

the interference terms ensure the perfect peak and valley structure



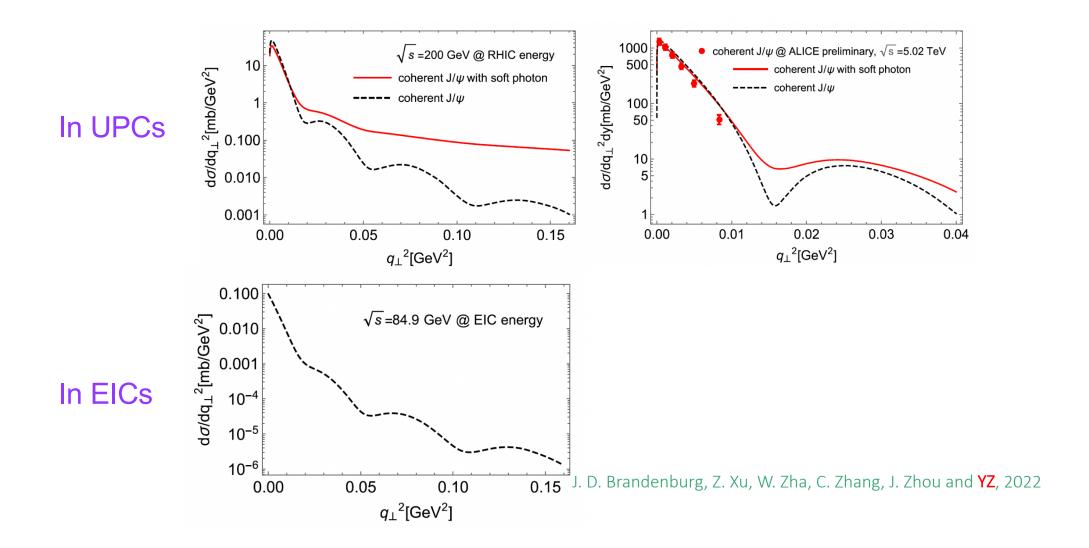
In EICs

$$\frac{d\sigma}{d^2p_{1\perp}d^2p_{2\perp}dy_1dy_2d^2\tilde{b}_\perp} \\ = \frac{\mathcal{C}}{2(2\pi)^7} \frac{24e^4e_q^2}{(Q^2-M^2)^2+M^2\Gamma^2} \frac{|\phi(0)|^2}{M} \int d^2\Delta_\perp d^2k_\perp d^2k'_\perp \delta^2(k_\perp + \Delta_\perp - q_\perp) \left[\hat{k}'_\perp \cdot \hat{k}_\perp - \frac{4(P_\perp \cdot \hat{k}_\perp)(P_\perp \cdot \hat{k}'_\perp)}{M^2}\right] \\ \times \left\{ \int d^2b_\perp e^{i\tilde{b}_\perp \cdot (k'_\perp - k_\perp)} [T_A(b_\perp) \mathcal{A}_{\text{in}}(x_2, \Delta_\perp) \mathcal{A}^*_{\text{in}}(x_2, \Delta'_\perp) \mathcal{F}(x_1, k'_\perp) + (A \leftrightarrow B)] \right. \\ \left. + \left[e^{i\tilde{b}_\perp \cdot (k'_\perp - k_\perp)} \mathcal{A}_{\text{co}}(x_2, \Delta_\perp) \mathcal{A}^*_{\text{co}}(x_2, \Delta'_\perp) \mathcal{F}(x_1, k'_\perp) \right] + \left[e^{i\tilde{b}_\perp \cdot (\Delta'_\perp - \Delta_\perp)} \mathcal{A}_{\text{co}}(x_1, \Delta'_\perp) \mathcal{F}(x_2, k'_\perp) \mathcal{F}(x_2, k'_\perp) \right] \\ \left. + \left[e^{i\tilde{b}_\perp \cdot (\Delta'_\perp - k_\perp)} \mathcal{A}_{\text{co}}(x_2, \Delta_\perp) \mathcal{A}^*_{\text{co}}(x_1, \Delta'_\perp) \mathcal{F}(x_1, k_\perp) \mathcal{F}(x_2, k'_\perp) \right] + \left[e^{i\tilde{b}_\perp \cdot (\Delta'_\perp - \Delta_\perp)} \mathcal{A}_{\text{co}}(x_1, \Delta_\perp) \mathcal{A}^*_{\text{co}}(x_2, \Delta'_\perp) \mathcal{F}(x_1, k'_\perp) \right] \right\} \\ \left. + \left[e^{i\tilde{b}_\perp \cdot (\Delta'_\perp - k_\perp)} \mathcal{A}_{\text{co}}(x_2, \Delta_\perp) \mathcal{A}^*_{\text{co}}(x_1, \Delta'_\perp) \mathcal{F}(x_1, k_\perp) \mathcal{F}(x_2, k'_\perp) \right] + \left[e^{i\tilde{b}_\perp \cdot (\Delta'_\perp - k_\perp)} \mathcal{A}_{\text{co}}(x_1, \Delta'_\perp) \mathcal{F}(x_2, k_\perp) \mathcal{F}(x_1, k'_\perp) \right] \right\}$$

the behavior will differ from that in UPC

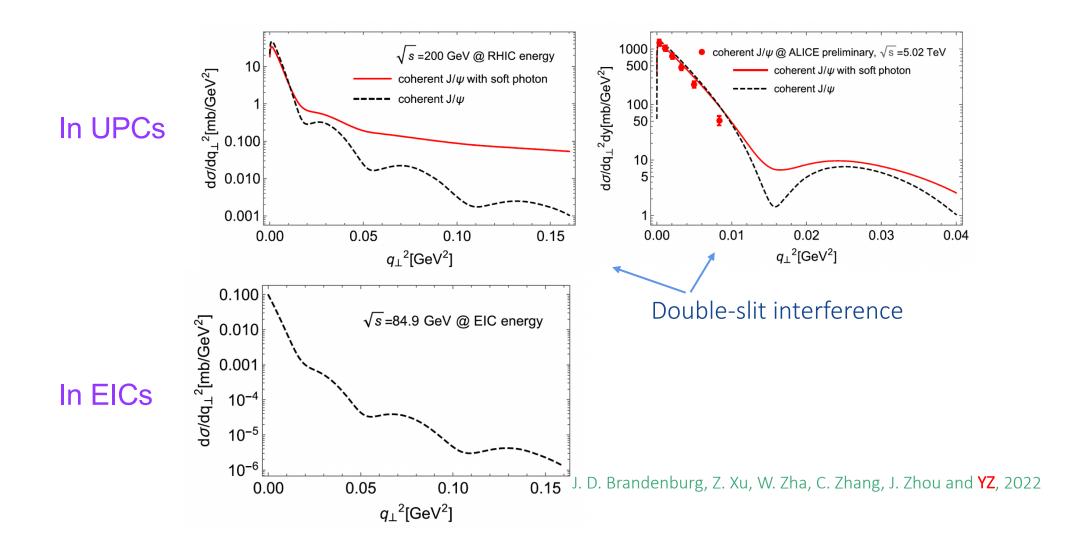
Cross section in J/ψ production





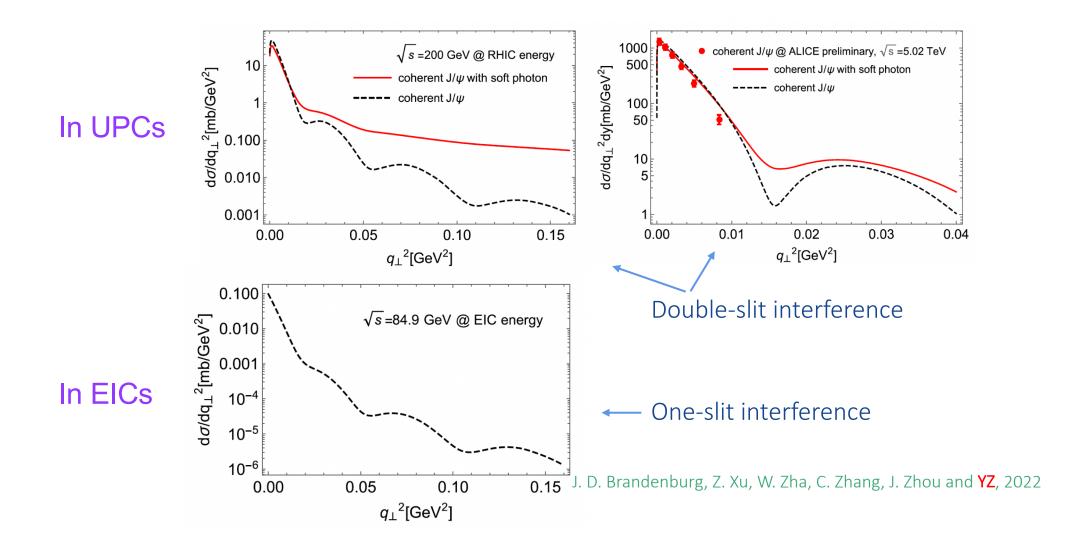
Cross section in J/ψ production



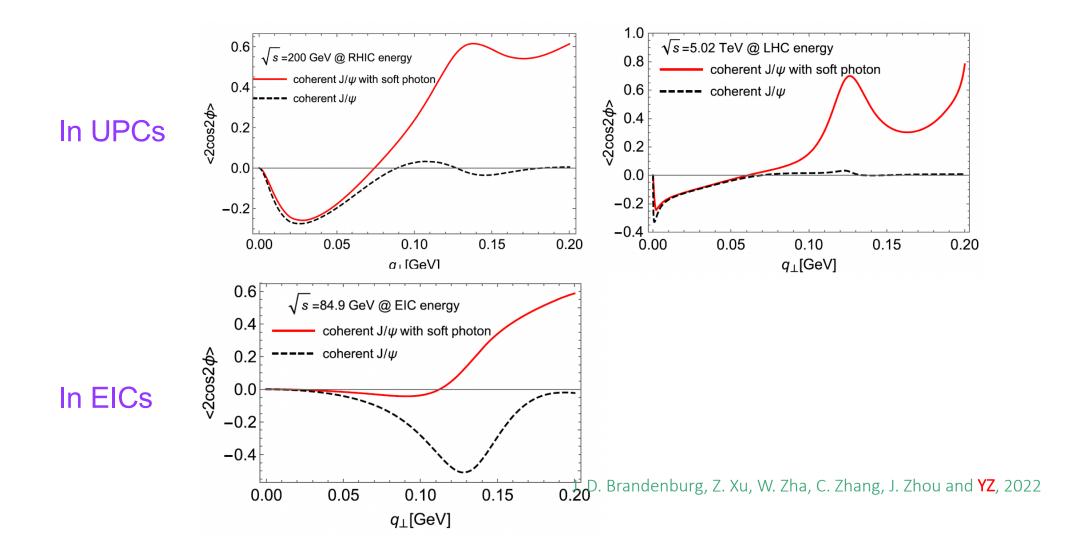


Cross section in J/ψ production

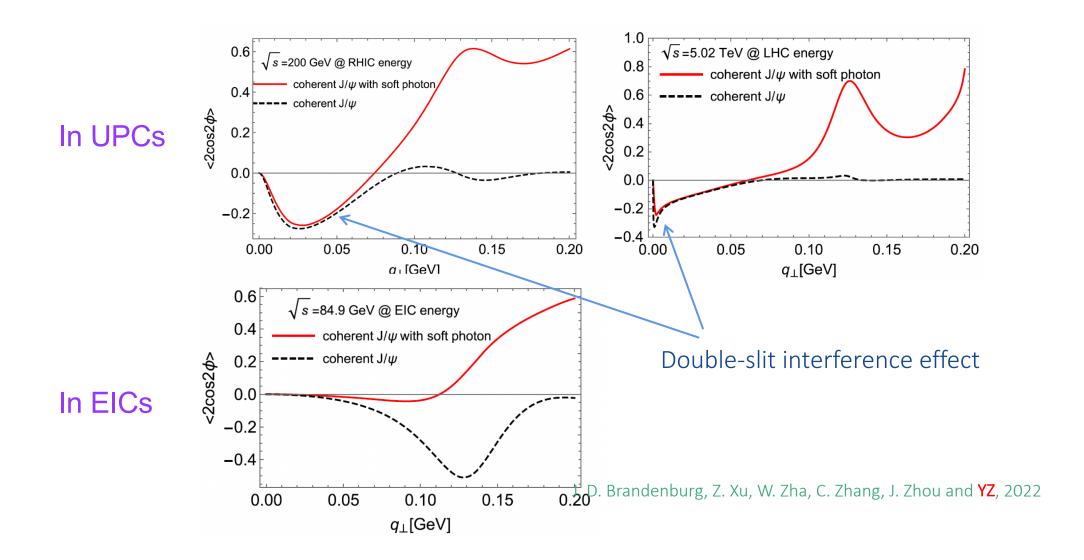




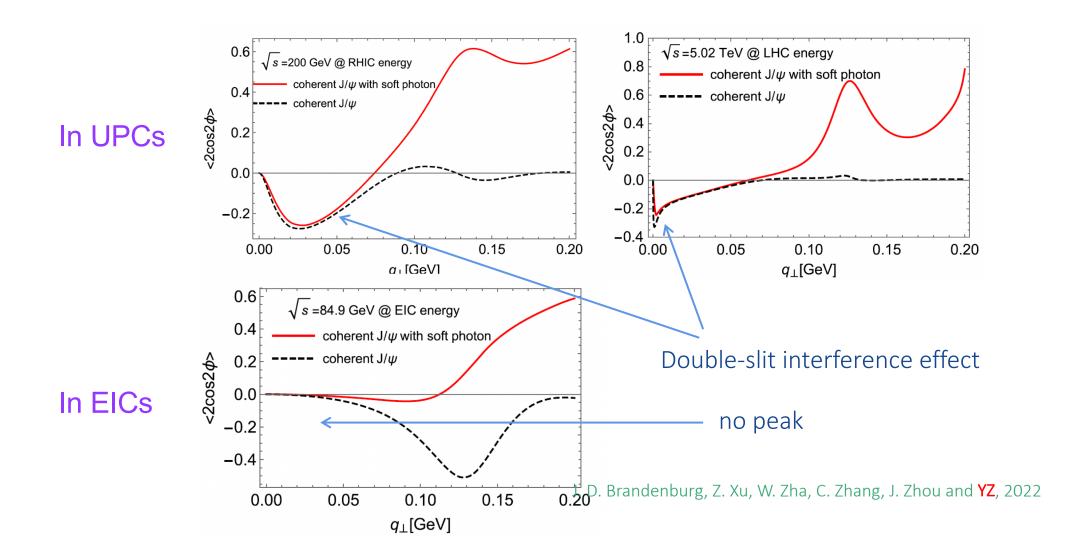






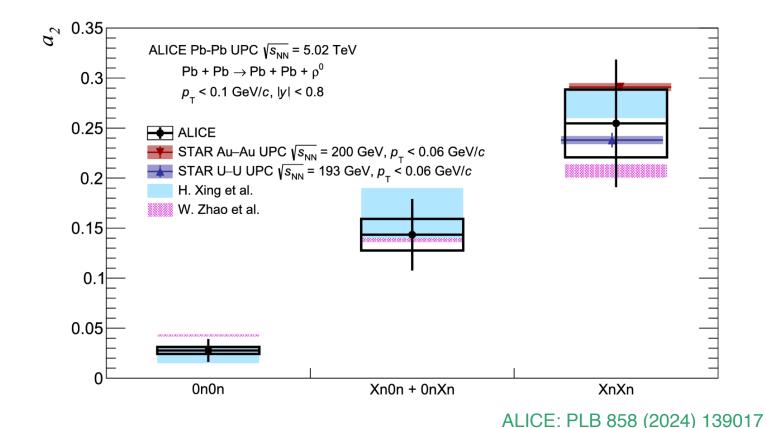






$cos2\phi$ asymmetry in ρ production, ALICE measurement vs. theory



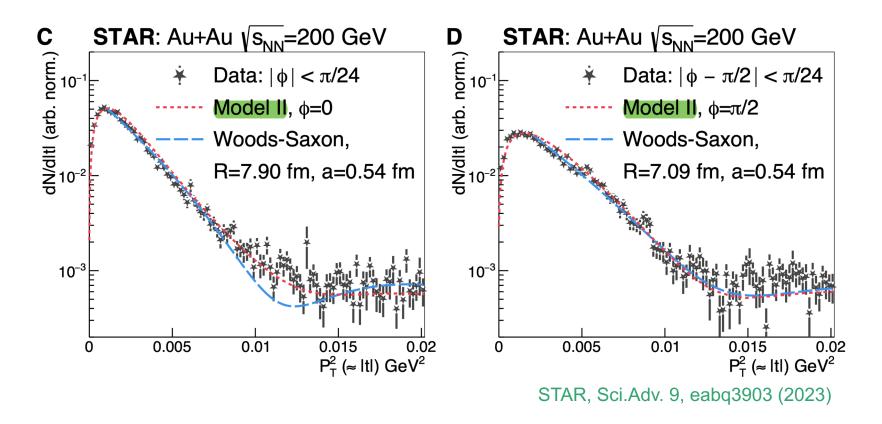


SDU-SCNU group: Hongxi Xing, Cheng Zhang, Jian Zhou, Ya-Jin Zhou JHEP 10 (2020) 064

BNL group: Heikki Mäntysaari, Farid Salazar, Björn Schenke, Chun Shen, Wenbin Zhao Phys. Rev. C 109 (2024) 2, 024908

$cos2\phi$ asymmetry in ρ production, STAR measurement vs. theory



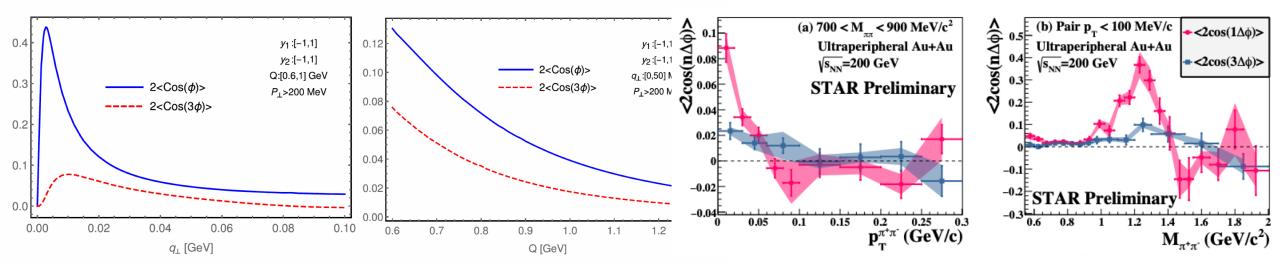


H.X. Xing, C. Zhang, J. Zhou and YZ, 2020, JHEP

cos φ and cos 3φ asymmetry in ρ production, STAR measurement vs. theory



• interference between diffractive $\rho^0 \to \pi\pi$ and direct $\pi\pi$ production

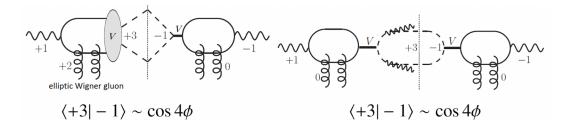


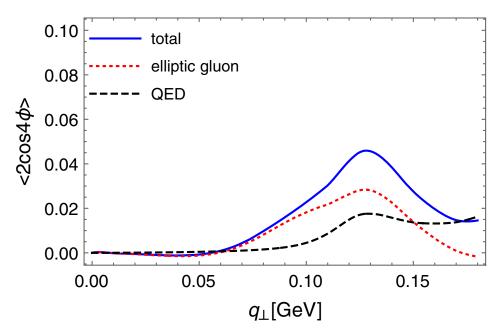
Y. Hagiwara, C. Zhang, J. Zhou and YZ, PRD103.074013(2021)

Chi Yang and Samuel's talk on UPC2025 in Finland

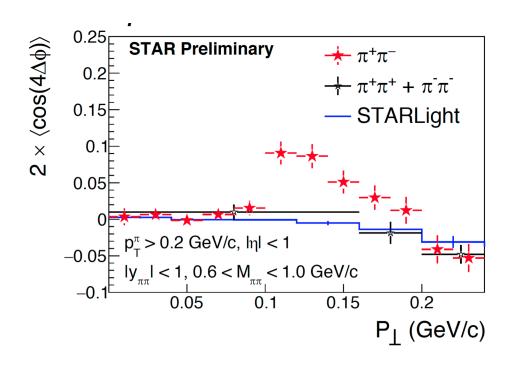
cos4 φ asymmetry in ρ production, STAR measurement vs. theory







• Both elliptic gluon Wigner distribution and final-state soft photon radiation contribute to cos4φ asymmetry.



Summary



- The EPA photons are linearly polarized, which can be used to probe nuclear structure in diffractive photo-nuclear processes in UPCs and EICs, and provide a method to extract spatial gluon distribution.
- Quite a few measurements at LHC and RHIC have been made, awaiting for the extraction of corresponding gluon distributions.
- The diffractive patterns predicted in UPCs and EICs differ significantly, both in their cross sections and azimuthal asymmetries. Measuring and comparing these observables in UPCs and EICs can provide deeper insights into gluon tomography.
 Thank you for your attention!

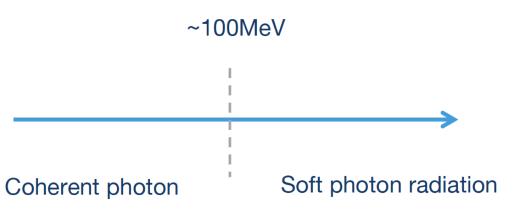


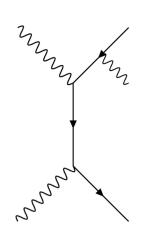
backups

Soft photon radiation



the recoiled momentum of the lepton also cause azimuthal anisotropy





$$\operatorname{Sud}_{1-\operatorname{loop}}(r_{\perp}) = \frac{\alpha_e}{\pi} \ln \frac{Q^2}{m^2} \ln \frac{P_{\perp}^2}{\mu_r^2}$$

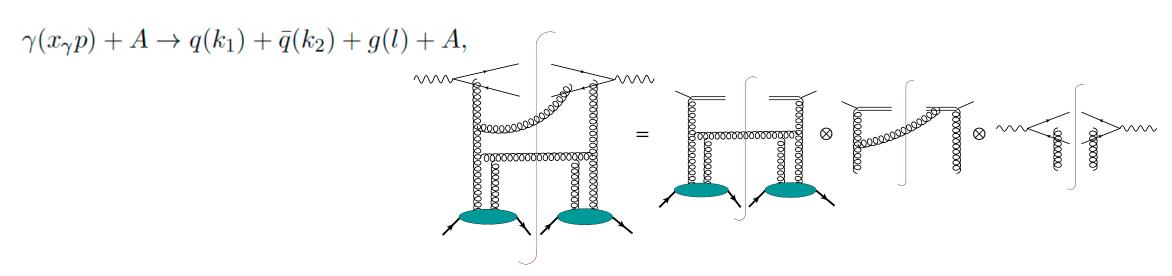
$$\frac{d\sigma(q_{\perp})}{d\mathcal{P}.\mathcal{S}.} = \int d^2q'_{\perp} \frac{d\sigma_0(q'_{\perp})}{d\mathcal{P}.\mathcal{S}.} S(q_{\perp} - q'_{\perp})$$

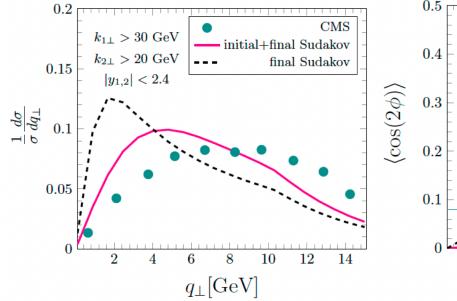
$$S(l_{\perp}) = \delta(l_{\perp}) + \frac{\alpha_e}{\pi^2 l_{\perp}^2} \left\{ c_0 + 2c_2 \cos 2\phi \right\} + 2c_4 \cos 4\phi + \dots \right\}$$

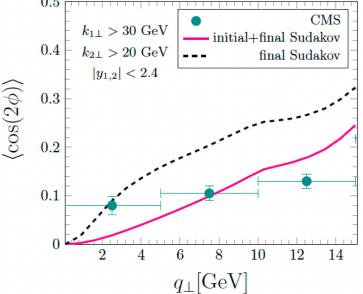
Y. Hatta, B.W. Xiao, F. Yuan and J. Zhou, PRL126, 142001(2021) and PRD104, 054037(2021)

Diffractive di-jet production in UPC









D.Y. Shao, Y. Shi, C. Zhang, J. Zhou and YZ, JHEP07(2024)189

Initial state radiation reduce the azimuthal asymmetry, could provide novel insights into the mechanisms of diffractive di-jet production