Gravitational formfactors, equivalence principle and shear viscosity XXXVI International Workshop on High Energy Physics

"Strong Interactions: Experiment, Theory, Phenomenology

Logunov IHEP, July 23, 2024

Oleg Teryaev JINR, Dubna Outline Gravitational formfactors and hadron spin structure External gravitational field Spacelike vs timelike formfactors Viscosity in hadrons Space ->Time: T-odd->exotics Holographic bounds -> smallness of DA

Gravitational Formfactors (spin ¹/₂)

 $\langle p'|T^{\mu\nu}_{q,g}|p\rangle = \bar{u}(p') \Big[A_{q,g}(\Delta^2) \gamma^{(\mu} p^{\nu)} + B_{q,g}(\Delta^2) P^{(\mu} i \sigma^{\nu)\alpha} \Delta_{\alpha}/2M] u(p)$

Conservation laws - zero Anomalous Gravitomagnetic Moment : $\mu_G = J$ (g=2)

 $P_{q,g} = A_{q,g}(0) \qquad A_q(0) + A_g(0) = 1$

 $J_{q,g} = \frac{1}{2} \left[A_{q,g}(0) + B_{q,g}(0) \right] \qquad A_q(0) + B_q(0) + A_g(0) + B_g(0) = 1$

- May be extracted from high-energy experiments/NPQCD calculations
- Describe the partition of angular momentum between quarks and gluons
- Describe interaction with scalar and tensor particles, with both classical and "TeV" gravity

Gravity and hadron structure: (OT'99)

- Interaction field vs metric deviation
- $M = \langle P' | J_q^{\mu} | P \rangle A_{\mu}(q) \qquad M = \frac{1}{2} \sum_{q,G} \langle P' | T_{q,G}^{\mu\nu} | P \rangle h_{\mu\nu}(q)$ Static limit
- $\langle P|J^{\mu}_{q}|P\rangle = 2e_{q}P^{\mu} \qquad \qquad \sum_{q,G} \langle P|T^{\mu\nu}_{i}|P\rangle = 2P^{\mu}P^{\nu} \\ h_{00} = 2\phi(x)$

$$M_0 = \langle P | J^{\mu}_q | P \rangle A_{\mu} = 2e_q M \phi(q) \qquad M_0 = \frac{1}{2} \sum_{q,G} \langle P | T^{\mu\nu}_i | P \rangle h_{\mu\nu} = 2M \cdot M \phi(q)$$

Mass as charge – equivalence principle

EP and hadron structure

"Microscopic" EP (coupling of gravity to EMT)

Conservation law (Momentum SR to get local from LC:∫dx x (Σ q(x) + G(x))=1)

=

+

"Macroscopic" EP (universal falling) : Tested VERY precisely

Gravitomagnetism

• Gravitomagnetic field (weak, except in gravity waves) – action on spin from $M = \frac{1}{2} \sum_{q,G} \langle P' | T_{q,G}^{\mu\nu} | P \rangle h_{\mu\nu}(q)$

$$\vec{H}_J = \frac{1}{2} rot \vec{g}; \ \vec{g}_i \equiv g_{0i}$$

spin dragging twice smaller than EM

• Lorentz force – similar to EM case: factor $\frac{1}{2}$ cancelled with 2 from $h_{00} = 2\phi(x)$ Larmor frequency same as EM

$$\omega_J = \frac{\mu_G}{J} H_J = \frac{H_L}{2} = \omega_L \ \vec{H}_L = rot \vec{g}$$

 Orbital and Spin momenta dragging – the same -Equivalence principle

Experimental test of PNEP

Reinterpretation of the data on G(EDM) search

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NUMBER 2

Search for a Coupling of the Earth's Gravitational Field to Nuclear Spins in Atomic Mercury

B. J. Venema, P. K. Majumder, S. K. Lamoreaux, B. R. Heckel, and E. N. Fortson Physics Department, FM-15, University of Washington, Seattle, Washington 98195 (Received 25 September 1991)

If (CP-odd!) GEDM=0 -> constraint for AGM (Silenko, OT'07) from Earth rotation – was considered as obvious (but it is just EP!) background

 $\mathcal{H} = -g\mu_N \boldsymbol{B} \cdot \boldsymbol{S} - \zeta \hbar \boldsymbol{\omega} \cdot \boldsymbol{S}, \quad \zeta = 1 + \chi$

 $|\chi(^{201}\text{Hg}) + 0.369\chi(^{199}\text{Hg})| < 0.042 \quad (95\%\text{C.L.})$

Quantum measurement and EP

If spin is just a (pseudo) vector : EP due to Earth rotation is trivial

Crucial if measured by a device in rotating frame

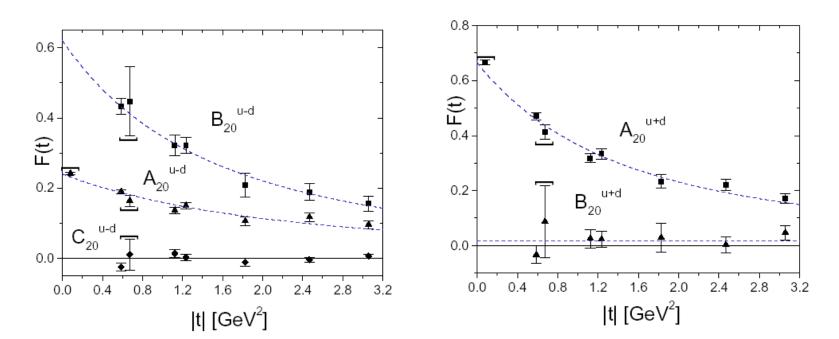
Quantum measurement problem becomes practical

Cf Unruh effect in HIC (Prokhorov, OT, Zakharov'19,23 and in progress)

Measurement problem in QM and GR

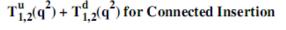
Generalization of Equivalence principle

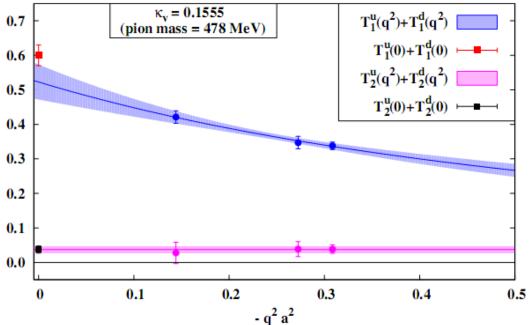
Various arguments: AGM ≈0 separately for quarks and gluons – most clear from the lattice (LHPC/SESAM)



Recent lattice study (M. Deka et al. Phys.Rev. D91 (2015) no.1, 014505)

Sum of u and d for Dirac (T1) and Pauli (T2) FFs





Extended Equivalence Principle=Exact EquiPartition

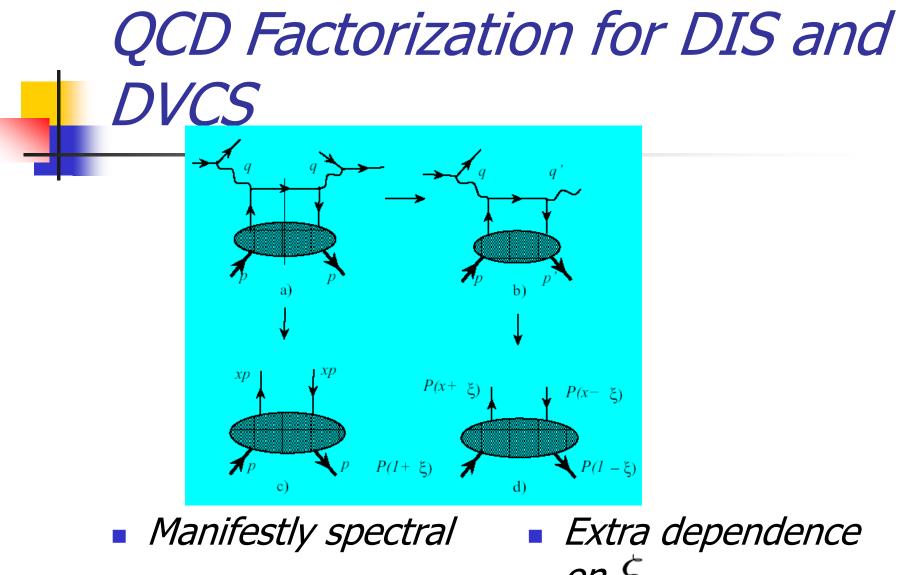
- In QED, pQCD violated (Brodsky et al)
- Reason in the case of ExEP- no smooth transition for zero fermion mass limit (Milton, 73)
- Conjecture (O.T., 2001 prior to lattice data) – valid in NP QCD – zero quark mass limit is safe due to chiral symmetry breaking
- Gravityproof confinement? Nucleons do not break even by black holes?
- Support by recent observation of smalness of (nucleon "cosmological constant") Cbar

One more gravitational formfactor (related to "D-term" of Maxim Polyakov and Christian Weiss)

• Quadrupole

 $\langle P + q/2 | T^{\mu\nu} | P - q/2 \rangle = C(q^2)(g^{\mu\nu}q^2 - q^{\mu}q^{\nu}) + \dots$

- Cf vacuum matrix element cosmological constant $\langle 0|T^{\mu\nu}|0\rangle = \Lambda g^{\mu\nu}$ $\Lambda = C(q^2)q^2$
- NO "vacuum-like" term EP, Smallness -ExEP
- How to measure experimentally DVCS (and DVMP?)



$$\mathcal{H}(x_B) = \int_{-1}^{1} dx \frac{H(x)}{x - x_B + i\epsilon}$$

 $\begin{array}{l} & \text{on } \xi \\ \mathcal{H}(\xi) = \int_{-1}^{1} dx \frac{H(x,\xi)}{x - \xi + i\epsilon}, \end{array} \end{array}$

Unphysical regions

DIS : Analytical function – polynomial in $1/x_B$ if $1 \le |X_B|$

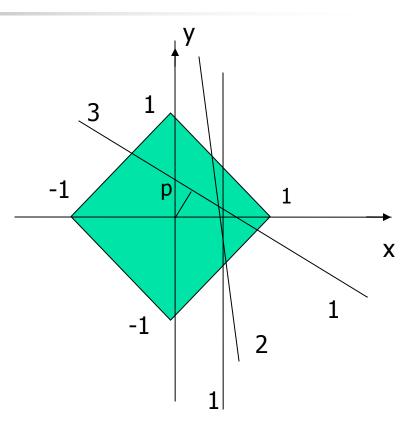
$$H(x_B) = -\int_{-1}^{1} dx \sum_{n=0}^{\infty} H(x) \frac{x^n}{x_B^{n+1}}$$

- DVCS additional problem of analytical continuation of H(x,ξ)
- Solved by using of Double Distributions Radon transform

$$H(z,\xi) = \int_{-1}^{1} dx \int_{|x|-1}^{1-|x|} dy (F(x,y) + \xi G(x,y)) \delta(z-x-\xi y)$$

Double distributions and their integration

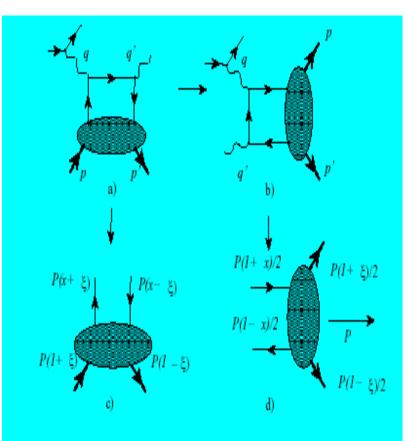
- Slope of the integration lineskewness
- Kinematics of DIS: ξ = 0
 ("forward") vertical line (1)
- Kinematics of DVCS: ξ <1
 line 2
- Line 3: ξ > 1 unphysical region - required to restore DD by inverse Radon transform: tomography



$$\begin{split} f(x,y) &= -\frac{1}{2\pi^2} \int_0^\infty \frac{dp}{p^2} \int_0^{2\pi} d\phi |\cos\phi| (H(p/\cos\phi + x + ytg\phi, tg\phi) - H(x + ytg\phi, tg\phi)) = \\ &= -\frac{1}{2\pi^2} \int_{-\infty}^\infty \frac{dz}{z^2} \int_{-\infty}^\infty d\xi (H(z + x + y\xi, \xi) - H(x + y\xi, \xi)) \end{split}$$

Crossing for DVCS and GPD

- DVCS -> hadron pair production in the collisions of real and virtual photons
- GPD -> Generalized
 Distribution Amplitudes
- Duality between s and t channels (Polyakov,Shuvaev, Guzey, Vanderhaeghen)



GDA -> back to unphysical regions for DIS and DVCS

Recall DIS

$$H(x_B) = -\int_{-1}^{1} dx \sum_{n=0}^{\infty} H(x) \frac{x^n}{x_B^{n+1}}$$

 Non-positive powers of X_B

$$H(\xi) = -\int_{-1}^{1} dx \sum_{n=0}^{\infty} H(x,\xi) \frac{x^{n}}{\xi^{n+1}}$$

DVCS

- Polynomiality (general property of Radon transforms): moments integrals in x weighted with xⁿ - are polynomials in 1/ ξ of power n+1
- As a result, analyticity is preserved: only non-positive powers of $\,\xi\,$ appear

->

Formula

$$\mathcal{H}(\xi) = \int_{-1}^{1} dx \frac{H(x,\xi)}{x-\xi+i\epsilon}$$

$$\mathcal{H}(\xi) = \int_{-1}^{1} dx \frac{H(x,x)}{x - \xi + i\epsilon}$$

$$\Delta \mathcal{H}(\xi) \equiv \int_{-1}^{1} dx \frac{H(x,x) - H(x,\xi)}{x - \xi + i\epsilon}$$

$$=\sum_{n=1}^{\infty}\frac{1}{n!}\frac{\partial^n}{\partial\xi^n}\int_{-1}^1H(x,\xi)dx(x-\xi)^{n-1}=const$$

Holographic property - II

Directly follows from double distributions

$$H(z,\xi) = \int_{-1}^{1} dx \int_{|x|-1}^{1-|x|} dy (F(x,y) + \xi G(x,y)) \delta(z-x-\xi y)$$

 Constant is the SUBTRACTION one - due to the (generalized) Polyakov-Weiss term G(x,y)

$$\Delta \mathcal{H}(\xi) = \int_{-1}^{1} dx \int_{|x|-1}^{1-|x|} dy \frac{G(x,y)}{1-y}$$
$$= \int_{-\xi}^{\xi} dx \frac{D(x/\xi)}{x-\xi+i\epsilon} = \int_{-1}^{1} dz \frac{D(z)}{z-1} = const$$

Holographic property - III

- 2-dimensional space -> 1-dimensional section!
- Momentum space: any relation to holography in coordinate space ?!

• Strategy (now adopted) of GPD's studies: start at diagonals (through SSA due to imaginary part of DVCS $x = -\xi$ amplitude) and restore by making use of dispersion relations + subtraction constants

x= *E*

Analyticity of Compton amplitudes in energy plane (Anikin,OT'07)

Finite subtraction implied

$$\operatorname{Re}\mathcal{A}(\nu, Q^{2}) = \frac{\nu^{2}}{\pi} \mathcal{P} \int_{\nu_{0}}^{\infty} \frac{d\nu'^{2}}{\nu'^{2}} \frac{\operatorname{Im}\mathcal{A}(\nu', Q^{2})}{(\nu'^{2} - \nu^{2})} + \Delta \qquad \Delta = 2 \int_{-1}^{1} d\beta \frac{D(\beta)}{\beta - 1}$$
$$\Delta_{\operatorname{CQM}}^{p}(2) = \Delta_{\operatorname{CQM}}^{n}(2) \approx 4.4, \qquad \Delta_{\operatorname{latt}}^{p} \approx \Delta_{\operatorname{latt}}^{n} \approx 1.1$$

- Numerically close to Thomson term for real proton (but NOT neutron) Compton Scattering!
- Duality (sum of squares vs square of sum; proton: 4/9+4/9+1/9=1)?!

From D-term to pressure

- Inverse -> 1st moment (model)
- Kinematical factor moment of pressure D~-4</sup>> (2</sup>> =0) M.Polyakov (2003)

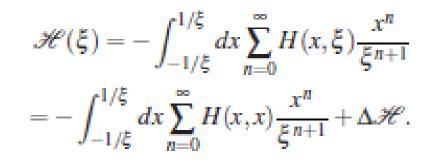
$$T^{Q}_{\mu\nu}(\vec{r},\vec{s}) = \frac{1}{2E} \int \frac{d^{3}\Delta}{(2\pi)^{3}} e^{i\vec{r}\cdot\vec{\Delta}} \langle p', S' | \hat{T}^{Q}_{\mu\nu}(0) | p, S \rangle$$

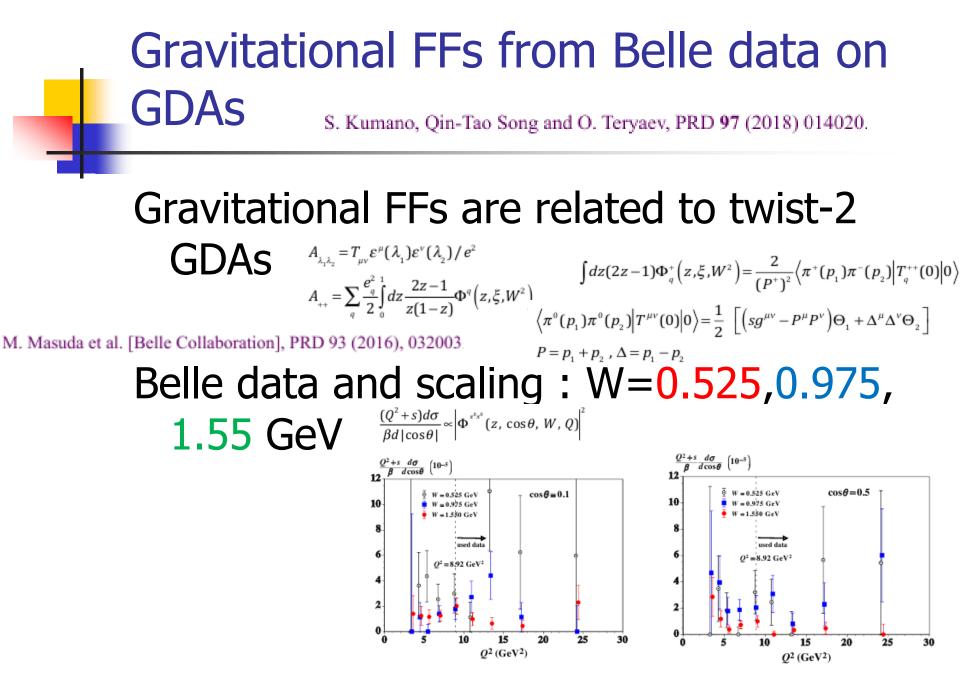
$$T_{ij}(\vec{r}) = s(r) \left(\frac{r_i r_j}{r^2} - \frac{1}{3} \,\delta_{ij}\right) + p(r)\delta_{ij}$$

- Possible justification: Born gravitational scattering
- Stable equilibrium D<0: Holds for quarks (or leptons) in photon

Pressure in hadron pairs production

- Back to GDA region
- -> moments of H(x,x) define the coefficients of powers of cosine!- 1/ξ
- Higher powers of cosine in t-channel – threshold in s -channel
- Larger for pion than for nucleon pairs because of less fast decrease at x ->1
- Large ξ limit access to D-term





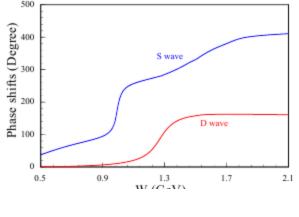
Phase shifts and resonances

Leading harmonics

 $\sum_{q} \Phi_{q}^{+}(z,\xi,W^{2}) = 18n_{f}z(1-z)(2z-1)[B_{10}(W) + B_{12}(W)P_{2}(2\xi-1)]$ $= 18n_{f}z(1-z)(2z-1)[\tilde{B}_{10}(W) + \tilde{B}_{12}(W)P_{2}(\cos\theta)]$

$$\tilde{B}_{10}(W) = \overline{B}_{10}(W)e^{i\delta_0}$$
, $\tilde{B}_{12}(W) = \overline{B}_{12}(W)e^{i\delta_2}$

S/D shifts



$$\overline{B}_{12}(W) = \beta^2 \frac{10g_{f_2\pi\pi}f_{f_2}M_{f_2}^2}{9\sqrt{2}\sqrt{(M_{f_2}^2 - W^2)^2 - \Gamma_{f_2}^2M_{f_2}^2}}$$
$$\overline{B}_{10}(W) = \frac{5g_{f_0\pi\pi}f_{f_0}}{3\sqrt{2}\sqrt{(M_{f_0}^2 - W^2)^2 - \Gamma_{f_0}^2M_{f_0}^2}}$$

Fits and results

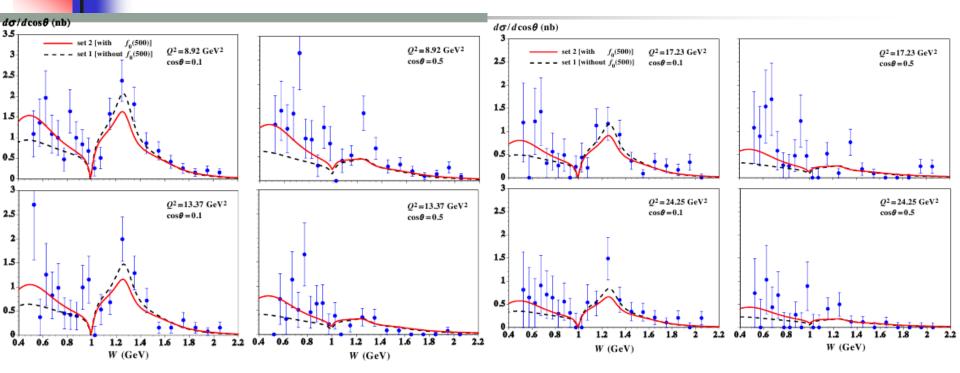
Collection

$$\begin{split} \Phi_{q}^{+}\left(z,\xi,W^{2}\right) &= N_{h}z^{\alpha}(1-z)^{\alpha}(2z-1)[\tilde{B}_{10}(W) + \tilde{B}_{12}(W)P_{2}(\cos\theta)]\\ \tilde{B}_{10}(W) &= \left[\frac{-3+\beta^{2}}{2}\frac{5R_{\pi}}{9}F_{h}(W^{2}) + \frac{5g_{f_{0}\pi\pi}f_{f_{0}}}{3\sqrt{2}\sqrt{\left(M_{f_{0}}^{2}-W^{2}\right)^{2}-\Gamma_{f_{0}}^{2}M_{f_{0}}^{2}}}\right]e^{i\delta_{0}}\\ \tilde{B}_{12}(W) &= \left[\beta^{2}\frac{5R_{\pi}}{9}F_{h}(W^{2}) + \beta^{2}\frac{10g_{f_{2}\pi\pi}f_{f_{2}}M_{f_{2}}^{2}}{9\sqrt{2}\sqrt{\left(M_{f_{2}}^{2}-W^{2}\right)^{2}-\Gamma_{f_{2}}^{2}M_{f_{2}}^{2}}}\right]e^{i\delta_{2}}\\ F_{h}(W^{2}) &= \frac{1}{\left[1+\frac{W^{2}-4m_{\pi}^{2}}{\Lambda^{2}}\right]^{n-1}} \end{split}$$

Best fit with (2) and without (1) f_{0}

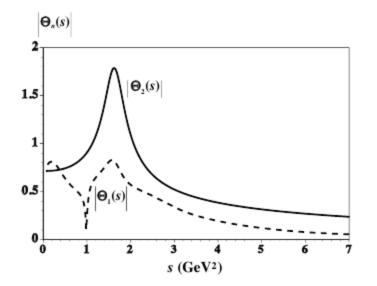
	Set 1	Set 2
α	0.801±0.042	1.157± 0.132
Λ	1.602±0.109	1.928±0.213
а	3.878± 0.165	3.800± 0.170
b	0.382± 0.040	0.407± 0.041
f _{f0}		0.0184± 0.034
	$\chi^{2} = 1.22$	$\chi^2 = 1.09$
	NOF	NOF

Description of data



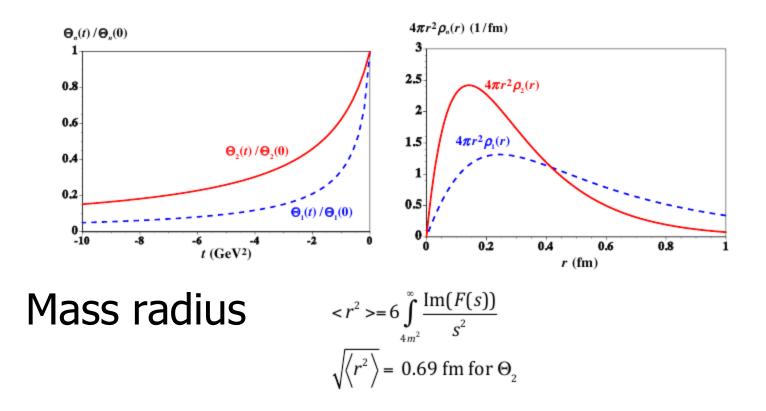


Resonance structure in pressure –related Θ_1



Time-like -> space-like

Dispersion relation and Fourier transform



Shear – natural counterpart of pressure

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Forces inside the nucleon on the light front from 3D Breit frame force distributions: Abel tomography case

Julia Yu. Panteleeva¹ and Maxim V. Polyakov^{1,2} ¹Ruhr University Bochum, Faculty of Physics and Astronomy, Institute for Theoretical Physics II, D-44870 Bochum, Germany ²Petersburg Nuclear Physics Institute, Gatchina, 188300 St. Petersburg, Russia

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3D <->2D relations

Shear viscosity

From spherically symmetric object to fluid (EoS!)

$$T^{\mu\lambda} = (e+p) v^{\mu}v^{\lambda} - p g^{\mu\lambda}$$

 $V^{\mu} = P^{\mu}/M$: correct normalization but no coordinate dependence Another suggestion:

$$V^{\mu} = (P^{\mu} + a(t) k_{T}^{\mu}) / (M^{2} + a^{2}(t) k_{T}^{2})^{\frac{1}{2}}$$

Viscosity: ~ E $_{\eta} p^{[\mu} \Delta^{\lambda]}$

Naïve T-oddness: phases

NO such term in total EMT (but can be for quarks separately)

Phases <-> dissipation: polarization in pionic superfluidity model (V. I. Zakharov, OT' 17)

Viscosity in GDA channel

- Viscosity:will correspond to Exotic J^{PC}=1⁻⁺ meson (already studied without reference to viscosity: Anikin, Pire, Szymanowski,OT, Wallon'06)
- Spin: related to structure of matrix element: One index of EMT (0th in rest frame) is carried by momentum and other by polarization vector- just what we need for viscosity
- No zero-momentum (classical) limit -> quantum
- NO for conserved EMT (zero coupling!): violated ExEP
- **π**η pairs observation instead of π π required
- Smallness of viscosity: related to smallness of exotic GDAs and ExEP violation?!

Exotic hybrid meson production

On exotic hybrid meson production in $\gamma^*\gamma$ collisions

I.V. Anikin¹, B. Pire^{2,a}, L. Szymanowski^{3,4,5}, O.V. Teryaev¹, S. Wallon⁵

Eur. Phys. J. C 47, 71–79 (2006) Digital Object Identifier (DOI) 10.1140/epjc/s2006-02533-7

Possible candidate Π_1 (1400)

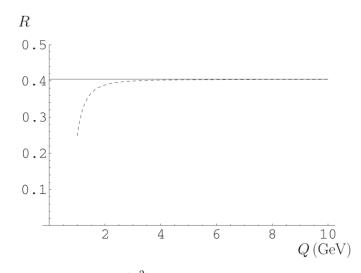


Fig. 2. The ratio $R(Q^2)$ of the squared amplitudes for H and π^0 production in $\gamma^* \gamma$ collisions at leading twist and zero-th order in α_s (solid line) and including twist three contributions in the numerator (dashed line)

Estimate of viscosity

Terms in EMT: (e+p) $v^{\mu}v^{\lambda} \sim A P^{\mu}P^{\lambda}$ $\eta dv^{\mu}/d x_{T}^{\lambda} \sim E_{n} p^{[\mu} \Delta^{\lambda]}$ TD: $e+p \sim Ts$ η/s (> 1/(4π) ~ E _nT /AM Correct dependence on Planck constant recovered via Δ^{λ} (cf K. Trachenko et al.)

DA vs holographic bound

$$\eta \frac{\partial v^{\nu}}{\partial x_{\mu}} \to \frac{P^{\nu} \Delta^{\mu}}{M} \sim E(t) P_{\nu} \Delta_{\mu} \qquad v^{\mu} = \frac{P^{\mu} + a(t) \Delta^{\mu}}{\sqrt{M^2 - a^2(t)t}}, \quad \frac{\partial}{\partial x_{\mu}} \to i \Delta^{\mu}$$
$$(e+p) v^{\nu} v^{\mu} \to T s \frac{P^{\nu} P^{\mu}}{M^2} \sim A(t) P^{\nu} P^{\mu} \qquad \qquad \frac{\eta}{s} \sim \frac{E(t)}{A(t)} \cdot \frac{T}{M} \quad \mathsf{T} \sim \langle \mathsf{K}_{\mathsf{T}} \rangle$$
$$\mathsf{Time-like}$$

 $\langle \pi \eta(P,\Delta) | T_i^{\alpha\nu} | 0 \rangle_{\mu^2} = E_i(s,\mu^2) P^\alpha \Delta^\nu$

Dimensionful $\frac{\eta}{s} \sim \hbar \frac{E(t)}{A(t)} \cdot \frac{T}{M} \sim \frac{\hbar}{k_B} \cdot \frac{E(t)}{A(t)} \cdot \frac{k_B T}{M}$ $\hbar \frac{\partial}{\partial x_{\mu}} \rightarrow i \Delta^{\mu}$

Small bound => small exotic DA, small ExEP violation

Conclusions/Outlook

- Time-like Gravitational FFs: may be studied in meson pairs production
- Exotic hybrid mesons: access to shear viscosity and interplay between hadronic and heavy-ion physics
- Holographic bound: related to smallness of exotic GDA and violation of ExEP?
- Shear from asymptotic transition gravitational FFs (Q.-T. Song, OT, work in progress)
- Medium viscosity from GrFFs?