D-wave B_c meson production at LHC XXXIII International Workshop on High energy Physics, Protvino

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B_c properties

- All excitations below the threshold decay into the ground state 1¹S₀.
- 2 The absence of strong annihilation channels ⇒ the very narrow ground state (practically as *B*-meson).
- Spectroscopy can be investigated within the same frame work as for cc
 and bb
 quarkoniums.
- The small total yield comparing to the cc and bb quarkonia case.
- The small relative yield of P-wave excitations comparing to the cc
 and bb
 quarkonia case.

 B_c family has a spectroscopy similar to $c\bar{c}$ or $b\bar{b}$ quarkonium spectroscopy and decays like B meson

- The main difference in decays (comparing to *B* meson): the both quarks in *B_c* are heavy.
- The main difference in spectroscopy (comparing to $c\bar{c}$ and $b\bar{b}$ quarkonia): charge parity can not be determined.

$$n_Q \chi_{1Q} \xrightarrow{\text{mixing}} 1^+ 1^{+'}$$

$$\begin{aligned} |2P, 1'^+\rangle &= 0.294|S=1\rangle + 0.956|S=0\rangle \\ |2P, 1^+\rangle &= 0.956|S=1\rangle - 0.294|S=0\rangle \\ |3P, 1'^+\rangle &= 0.371|S=1\rangle + 0.929|S=0\rangle \\ |3P, 1^+\rangle &= 0.929|S=1\rangle - 0.371|S=0\rangle \end{aligned}$$

[Kiselev et al.(1995)Kiselev, Likhoded, and Tkabladze, Gershtein et al.(1995)Gershtein, Kiselev, Likhoded, and Tkabladze]

Spectroscopy

All excitations decay into 1^1S_0 .



Figure 1: The mass spectrum of $(\bar{b}c)$ with account for the spin-dependent splittings.

[Gouz et al.(2004)Gouz, Kiselev, Likhoded, Romanovsky, and Yushchenko]

$$\begin{split} M_{B_c} &= 6274.9 \pm 0.8 \ {\rm MeV}, \\ \tau_{B_c} &= 0.507 \pm 0.009 \ {\rm ps.} \\ \tau_{B_c}$$

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$B_c(2S)$ observed in $B_c^{(*)} + \pi\pi$ spectrum





CMS results (reasonable agreement with predictions!)

$$\frac{\sigma(B_c(2S) \to B_c(1S) + \pi^+\pi^-)}{\sigma(B_c)} = (8.2 \pm 1.1) \%$$

$$\frac{\sigma(B_c^*(2S))}{\sigma(B_c(2S))} = 1.35 \pm 0.33$$

CMS [Sirunyan et al.(2019)] LHCb [Aaij et al.(2019)] CMS[Sirunyan et al.(2020), CMS(2020)]

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What was expected for $B_c^{(*)}(2S) \rightarrow B_c^{(*)} + \pi\pi$

$$\begin{split} B_c(2S) & \frac{\pi^+\pi^-}{\sim 50\%} B_c \\ B_c^*(2S) & \frac{\pi^+\pi^-}{\sim 40\%} B_c^* \\ \sigma^{2S}/\sigma^{\rm total} \sim 25~\% \end{split}$$

~ 10 % of B_c come from $B_c(2S) \rightarrow B_c(1S) + \pi^+\pi^-$

Under assumption that $\begin{aligned} |R(B_c^*(2S))(0)| &\approx |R(B_c(2S))(0)| \\ &\sigma(B_c^*(2S))/\sigma(B_c(2S)) \sim 2.6 \end{aligned}$

Relativistic corrections

 $|R(B_c^*(2S))(0)|/|R(B_c(2S))(0)| = 0.87$ [Martynenko(2019)]

$$\begin{split} |R(B_c^*(2S))(0)| / |R(B_c(2S))(0)| &= 0.567\\ \text{[Galkin(2019),}\\ \text{Ebert et al.(2011)Ebert, Faustov, and Galkin]} \end{split}$$

$$\sigma(B_c^*(2S))/\sigma(B_c(2S)) \sim 1 \div 2$$



where $x = m_{\pi\pi}/2m_{\pi}$ and $\mathbf{k}_{\pi\pi}$ is the momentum of $\pi\pi$ -pair in the initial quarkonium rest frame. [Brown and Cahn(1975), Novikov and Shifman(1981), Voloshin(1975), Voloshin and Zakharov(1980)]

Table: The experimental data on $B_c(2S)$

	experiment	ATLAS	CMS	LHCb
	luminosity (energy)	24.1 fb ⁻¹ (7, 8 TeV)	140 fb ⁻¹ (13 TeV)	8.7 fb ⁻¹ (7, 8, 13 TeV)
mass, MeV	2^3S_1 , shifted	6842 + 6	6842 ± 2	6841 ± 1
	$2^{1}S_{0}$	0342 ± 0	6871.0 ± 1.6	6872.1 ± 1.6
row relative yield	$2^{3}S_{1}$		0.0088 ± 0.0014	0.0136 ± 0.0027
	$2^{1}S_{0}$		0.0068 ± 0.0014	0.0063 ± 0.0024
	total	0.18 ± 0.05	0.0156 ± 0.0019	0.0198 ± 0.0036
	$2^{3}S_{1}$		(4.69 ± 0.90) %	
real relative yield	$2^{1}S_{0}$		(3.47 ± 0.71) %	
	total		(8.16 ± 1.1) %	
$N(2^{3}S_{1})/N(2^{1}S_{0})$			1.35 ± 0.33	2.1 ± 0.9

• The registration efficiencies for $\pi^+\pi^-$ are published only by CMS Collaboration, thus the relative yields can not be accurately compared.

• Unexpectedly large yield at ATLAS.

ATLAS [Aad et al.(2014)], CMS [Sirunyan et al.(2019)], LHCb [Aaij et al.(2019)] See also later CMS publications: [Sirunyan et al.(2020), CMS(2020)]

D-wave states of B_c -mesons

Π	State	EQ	GKLT	ZVR	FUI	EFG	GI	MBV	SJSCP	LLLGZ
Π	$1^{3}D_{1}$	7012	7008	7010	7024	7072	7028	6973	6998	7020
	$1D'_2$		7016			7079	7036	7003		7032
	$1D_{2}^{-}$		7001			7077	7041	6974		7024
	$1^{1}D_{2}$	7009		7020	7023				6994	
	$1^{3}D_{2}$	7012		7030	7025				6997	
	$1^{3}D_{3}$	7005	7007	7040	7022	7081	7045	7004	6990	7030

Predictions for masses of D-wave states of B_c -mesons (MeV):

 $\sim 20\%~D$ could radiate $\pi\pi$ [Eichten and Quigg(1994)] (see also

[Asghar et al.(2019)Asghar, Åkram, Masud, and Sultan]), and therefore one can expect peak in the same mass distribution as for $B_c(2S)$

$B_c\pi\pi$ -peaks from D states

- one narrow peak at ~ 7000 MeV from 1^1D_2 state;
- one broad peak at ~ 6930 MeV form shifted and broadened 1^3D_1 , 1^3D_2 , 1^3D_3 states.

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D-wave B_c calculation in hadronic interaction



LO: 36 diagrams of the order of $\mathcal{O}(\alpha_S^4 \; v^4)$

$$A \sim \int d^3 q \Psi^*(\mathbf{q}) \left\{ T(p_i, \mathbf{q}) \Big|_{\mathbf{q}=0} + q^{\alpha} \frac{\partial}{\partial q^{\alpha}} T(p_i, \mathbf{q}) \Big|_{\mathbf{q}=0} + \frac{1}{2} q^{\alpha} q^{\beta} \frac{\partial^2}{\partial q^{\alpha} \partial q^{\beta}} T(p_i, \mathbf{q}) \Big|_{\mathbf{q}=0} + \cdots \right\}$$

q is quark three momentum in B_c -meson, $\Psi^*(q)$ is B_c -meson wave function, and T is the amplitude of four heavy quark gluonic production with momenta p_i . For D wave state an amplitude is proportional to R''(0) and second derivatives of T over q. Spin singlet $(J = 2, j_z = l_z)$:

$$A^{jz} = \frac{1}{2} \sqrt{\frac{15}{8\pi}} R_D^{\prime\prime}(0) \epsilon^{\alpha\beta}(j_z) \left. \frac{\partial^2 M(\boldsymbol{q})}{\partial q^\alpha \partial q^\beta} \right|_{\boldsymbol{q}=0}$$

Spin triplet $(J = 1, 2, 3; j_z = s_z + l_z)$:

$$A^{Jjz} = \frac{1}{2} \sqrt{\frac{15}{8\pi}} R_D^{\prime\prime}(0) \Pi^{J, \ \alpha\beta\rho}(j_z) \left. \frac{\partial^2 M_\rho(q)}{\partial q^\alpha \partial q^\beta} \right|_{q=0}$$

$$\Pi^{J, \ \alpha\beta\rho}(j_z) = \sum_{l_z, s_z} \epsilon^{\alpha\beta}(l_z) \epsilon^{\rho}(s_z) \cdot C^{Jj_z}_{s_z l_z},$$

where $C_{s_{z_{z_{z_{z_{z_{z_{z_{z_{z_{z_{z_{z_{c_{z_{l_{z_{c_{z_{l_{z_{c_{z_{l_{z_{c_{l}}}}}}}}}}}}}}}$ are Clebsch-Gordan coefficients.

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Amplitude derivatives

$$\mathcal{P}(0,0) = \frac{1}{\sqrt{2}} \{ v_+ (p_{\bar{b}} + k) \bar{u}_+ (p_c - k) - v_- (p_{\bar{b}} + k) \bar{u}_- (p_c - k) \},$$

$$\mathcal{P}(1, S_z) = \begin{cases} \mathcal{P}(1, 1) = v_-(p_{\bar{b}} + k)\bar{u}_+(p_c - k) \\ \mathcal{P}(1, 0) = \frac{1}{\sqrt{2}} \{v_+(p_{\bar{b}} + k)\bar{u}_+(p_c - k) + v_-(p_{\bar{b}} + k)\bar{u}_-(p_c - k)\} \\ \mathcal{P}(1, -1) = v_+(p_{\bar{b}} + k)\bar{u}_-(p_c - k) \end{cases}$$

$$\begin{split} v_{\lambda_1}(p_{\bar{b}}+k) &= (1-\frac{\hat{k}}{2m_b})v_{\lambda_1}(p_{\bar{b}}), \\ \bar{u}_{\lambda_2}(p_c-k) &= (1-\frac{\hat{k}}{2m_c})\bar{u}_{\lambda_2}(p_c), \end{split}$$

where $p_{\bar{b}} = \frac{m_b}{m_b + m_c} P_{B_c}$, $p_{\bar{c}} = \frac{m_c}{m_b + m_c} P_{B_c}$ and $k(\vec{q})$ ia a Lorentz boost of $(0, \vec{q})$ to the system where B_c momentum is P_{B_c} .

Amplitudes and there derivatives have been calculated numerically as follows:

$$\begin{split} \frac{\partial^2 M}{\partial q_x^2} &= \frac{M(p_i, \vec{q}_x) + M(p_i, -\vec{q}_x) - 2M(p_i, 0)}{\Delta_x^2} \\ \frac{\partial^2 M}{\partial q_x \partial q_y} &= \frac{M(p_i, \vec{q}_x + \vec{q}_y) + M(p_i, 0) - M(p_i, \vec{q}_x) - M(p_i, \vec{q}_y)}{\Delta_x \Delta_y} \end{split}$$

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Amplitude squared

 $\text{Matrix elements are summed over } J \text{ and } j_z \colon \ \mathbb{P} = \sum_{\substack{j_z \ j_z'}} A^{j_z} A^* \frac{j_z'}{2} \text{ and } \mathbb{V} = \sum_{\substack{J \ J' \ j_z \ j_z'}} \sum_{\substack{j_z \ j_z'}} \mathcal{A}^{Jj_z} \mathcal{A}^* \frac{J'j_z'}{2}.$

• The amplitude squared for the spin-singlet state with S = 0 (1¹ D_2):

$$\begin{split} \mathbb{P} &= \left(\frac{5}{16\pi}\right) |R_D^{\prime\prime}(0)|^2 \times \\ &\left[\left(\left| \frac{\partial^2 M}{\partial k_x^2} \right|^2 + \left| \frac{\partial^2 M}{\partial k_y^2} \right|^2 + \left| \frac{\partial^2 M}{\partial k_z^2} \right|^2 \right) + 3 \left(\left| \frac{\partial^2 M}{\partial k_x \partial k_y} \right|^2 + \left| \frac{\partial^2 M}{\partial k_x \partial k_z} \right|^2 + \left| \frac{\partial^2 M}{\partial k_y \partial k_z} \right|^2 \right) \\ &- \operatorname{Re} \left(\frac{\partial^2 M}{\partial k_x^2} \frac{\partial^2 M^*}{\partial k_y^2} + \frac{\partial^2 M}{\partial k_x^2} \frac{\partial^2 M^*}{\partial k_z^2} + \frac{\partial^2 M}{\partial k_y^2} \frac{\partial^2 M^*}{\partial k_z^2} \right) \right] \end{split}$$

• The sum of amplitudes squared for the spin-triplet states with S = 1 (1^3D_1 , 1^3D_2 , 1^3D_3):

$$\begin{split} \mathbb{V} &= |\mathcal{A}(J=1)|^2 + |\mathcal{A}(J=2)|^2 + |\mathcal{A}(J=3)|^2 = \left(\frac{5}{16\pi}\right) |\mathcal{R}_D^{\prime\prime}(0)|^2 \times \\ &\sum_{s_z}^{-1,0,1} \left[\left(\left| \frac{\partial^2 \mathcal{M}_{s_z}}{\partial k_x^2} \right|^2 + \left| \frac{\partial^2 \mathcal{M}_{s_z}}{\partial k_y^2} \right|^2 + \left| \frac{\partial^2 \mathcal{M}_{s_z}}{\partial k_z^2} \right|^2 \right) + 3 \left(\left| \frac{\partial^2 \mathcal{M}_{s_z}}{\partial k_x \partial k_y} \right|^2 + \left| \frac{\partial^2 \mathcal{M}_{s_z}}{\partial k_x \partial k_z} \right|^2 + \left| \frac{\partial^2 \mathcal{M}_{s_z}}{\partial k_y \partial k_z} \right|^2 \right) \\ &- \operatorname{Re} \left(\frac{\partial^2 \mathcal{M}_{s_z}}{\partial k_x^2} \frac{\partial^2 \mathcal{M}_{s_z}^*}{\partial k_y^2} + \frac{\partial^2 \mathcal{M}_{s_z}}{\partial k_x^2} \frac{\partial^2 \mathcal{M}_{s_z}^*}{\partial k_x^2} + \frac{\partial^2 \mathcal{M}_{s_z}}{\partial k_z^2} + \frac{\partial^2 \mathcal{M}_{s_z}}{\partial k_y^2} \frac{\partial^2 \mathcal{M}_{s_z}^*}{\partial k_z^2} \right) \right] \end{split}$$

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Color octet (singlet) NRQCD contributions

The final B_c meson is a superposition of Fock states:

$$|B_{c}(1^{1}D_{2})\rangle = O(1)|\bar{b}c(^{1}D_{2},\mathbf{1})\rangle + O(v)|\bar{b}c(^{1}P_{1},\mathbf{8})g\rangle + O(v^{2})|\bar{b}c(^{1}S_{0},\mathbf{8} \text{ or } \mathbf{1})gg\rangle + \cdots$$
(1)

$$|B_{c}(1^{3}D_{j})\rangle = O(1)|\bar{b}c(^{3}D_{j},1)\rangle + O(v)|\bar{b}c(^{3}P_{j'},8)g\rangle + O(v^{2})|\bar{b}c(^{3}S_{1},8 \text{ or } 1)gg\rangle + \cdots$$
(2)

- All NRQCD states in (1),(2) contribute to cross section as O(v⁴)
- The O(1) terms in (1),(2) are well defined:

$$\begin{split} \langle \mathcal{O}^{B_c(1^1D_2)}_{\mathbf{1}}(^1D_2) \rangle &\approx \frac{75N_c}{4\pi} |R_D^{\prime\prime}(0)|^2 \\ \langle \mathcal{O}^{B_c(1^3D_j)}_{\mathbf{1}}(^3D_j) \rangle &\approx \frac{15(2j+1)N_c}{4\pi} |R_D^{\prime\prime}(0)|^2 \end{split}$$

• Naive velocity scaling:

$$\mathsf{P}\text{-wave octet} \left\{ \begin{array}{ccc} \frac{\delta_{\overline{b}c}}{\sqrt{3}} & \longrightarrow & \sqrt{2} \; t^a_{\overline{b}c} \\ |R'_P(0)|^2 & \longrightarrow & K_{P\mathbf{8}} \cdot |R'_P(0)|^2 \\ K_{P\mathbf{8}} & = & O(v_{\text{eff}}^2) \end{array} \right.$$

$$v_{\text{eff}}^2 = \frac{\langle E \rangle}{2\mu}$$

$$\begin{array}{ccc} \mathbf{S}\text{-wave octet} \left\{ \begin{array}{ccc} \frac{\delta_{\overline{b}c}}{\sqrt{3}} & \longrightarrow & \sqrt{2} \; t^a_{\overline{b}c} \\ |R_S(0)|^2 & \longrightarrow & K_{S\mathbf{8}} \cdot |R_S(0)|^2 \\ K_{S\mathbf{8}} & = & O(v_{\text{eff}}^4) \end{array} \right. \end{array}$$

$$\begin{array}{c} \text{Effective value} \fbox{v_{\text{eff}}^2 \approx 0.15} \text{ from } \\ \text{Gershtein et al.(1995)Gershtein, Kiselev, Likhoded, and Tkabladze]} \\ \begin{array}{c} \text{S-wave singlet} \left\{ \begin{array}{c} \left|R_S(0)\right|^2 \longrightarrow K_{S1} \cdot \left|R_S(0)\right|^2 \\ K_{S1} &= O(v_{\text{eff}}^4) \\ \end{array} \right. \\ \left. \begin{array}{c} \text{Gershtein et al.(1995)Gershtein, Kiselev, Likhoded, and Tkabladze]} \end{array} \right\} \\ \end{array}$$

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$gg \to B_c(D) + X$ v.s. $gg \to B_c + X$

Wave functions by [Eichten and Quigg(2019)]:

$$|R_D''(0)|^2 = 0.0986 \text{ GeV}^7$$

 $|R_S(0)|^2 = 1.994 \text{ GeV}^3$

Cross sections obtained with $\alpha_s = 0.1$.

energy,	σ_{gg} , pb		
$\sqrt{s_{gg}}$, GeV	1S	1D	
20	1.97	0.009	
30	2.90	0.023	
50	2.64	0.028	
70	1.98	0.024	
100	1.44	0.018	
150	0.90	0.012	



 $\sigma(gg \rightarrow B_c + X)$ at $\sqrt{s_{gg}} = 100$ GeV. Red lines: S = 0, blue lines: S = 1, solid lines: D-waves, dashed lines: S-waves scaled by 0.01

Primary predictions for $B_c(D)$

1 ÷ 2 % of the direct yield of 1S

•
$$\sigma(1^3D_1 + 1^3D_2 + 1^3D_3)/\sigma(1^1D_2) \sim (3+5+7)/5 = 3$$

• p_T distributions are quite similar to ones for S wave states

• $\sigma(1D)/\sigma(1S)$ ratio is sensible to $|R''_D(0)|^2/|R_S(0)|^2$

$pp \rightarrow B_c(D) + X$: cross sections



 $\sigma \ (pp \to B_c + X) \text{ dependence on } p_T \text{ at diff. scales for frontal kinematics: } 2 < \eta < 4.5, \ p_T < 10 \text{ GeV.}$

 $\sigma (pp \rightarrow B_c + X)$ dependence on p_T at diff. scales for central kinematics: $|\eta| < 2.5, \ 10 \text{ GeV} < p_T < 50 \text{ GeV}$

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 Convolution with CT14 PDFs by CTEQ group [Dulat et al.(2016)Dulat, Hou, Gao, Guzzi, Huston, Nadolsky, Pumplin, Schmidt, Stump, and Yuan]

$$\sigma_{pp} = \int \sigma_{gg}(\hat{s}_{gg}, \mu) f_{g1}(x_1, \mu) f_{g2}(x_2, \mu) dx_1 dx_2, \qquad \qquad E_T/2 < \mu < 2E_T$$

RAMBO algorithm for Monte-Carlo integraton [Kleiss et al. (1986)Kleiss, Stirling, and Ellis]

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$pp \to B_c(D) + X$: yields



Relative yields for D-wave B_c mesons for forward and central kinematic regions at LHC.

kinematic region	$\sigma\left(1^{3}S_{1}\right)/\sigma\left(1^{3}S_{0}\right)$	$\sigma \left(1^3 D_j\right) / \sigma \left(1^1 D_2\right)$	$\sigma\left(1D ight)/\sigma\left(1S ight)$, %
$2 < \eta < 4.5, p_T < 10 \text{ GeV}$	2.4	3.0	$0.6 \div 0.7$
$ \eta < 2.5, \ 10 \ \text{GeV} < p_T < 50 \ \text{GeV}$	2.4	2.3	$1.0 \div 1.1$

More optimistic values in the approaches considering relativistic corrections. [Ebert et al.(2011)Ebert, Faustov, and Galkin] $-\sigma(1D)/\sigma(1S)$ is approximately 1.6 times higher, [Martynenko(2019)] $-\sigma(1D)/\sigma(1S)$ is approximately 1.5 times higher.

Color octet (singlet) contributions to $gg \to B_c(D) + X$



 $\sigma \; (gg \rightarrow B_c + X)$ dependence on transverse momentum at $\sqrt{s}_{gg} = 100$ GeV. Solid lines: direct D-wave production; dashed lines: S-wave states, scaled by 0.01; dashed-dotted lines: extra D-wave states. Red lines: states with S=0, blue lines: states with S=1.

 $\sigma~(gg \rightarrow B_c + X)$ dependence on gluon-gluon energy. Black line: direct D-wave production; red line: $|(1P,8)g\rangle$ contribution; blue and green lines: $|(1S,1)gg\rangle$ and $|(1S,8)gg\rangle$ contributions correspondingly.

- p_T distribution shapes for $|\bar{b}c(P, \mathbf{8})g\rangle$, $|\bar{b}c(S, \mathbf{8})gg\rangle$, $|\bar{b}c(S, \mathbf{1})gg\rangle$ states nearly reproduce ones for direct D-wave production
- Color octet contributions decrease faster with energy than color singlet ones
- Seems, that the shape of energy dependence is mostly determined by color state of bc-pair and practically does not depend on its orbital momentum.

Color octet (singlet) contributions to $B_c(D)$ yield



r dependence on p_T at different scales for forward kinematics: $2 < \eta < 4.5, \ p_T < 10$ GeV. The contributions of $|\bar{b}c(P,\mathbf{8})g\rangle, |\bar{b}c(S,\mathbf{8})gg\rangle$ and $|\bar{b}c(S,\mathbf{1})gg\rangle$ states are included.



r dependence on p_T at different scales for central kinematics: $|\eta| < 2.5, \ 10 \ {\rm GeV} < p_T < 50 \ {\rm GeV}.$ The contributions of $|\bar{b}c(P, 8)g\rangle, |\bar{b}c(S, 8)gg\rangle$ and $|\bar{b}c(S, 1)gg\rangle$ states are included.

$$K_{P8} = \mathcal{O}(v_{\text{eff}}^2); \ 0.1 < K_{S8,1} < 0.2$$
 $K_{S8,1} = \mathcal{O}(v_{\text{eff}}^4); \ 0.015 < K_{S8,1} < 0.03$

• The hadronic relative yield $\sigma(1D)/\sigma(1S)$ is increased by an order of magnitude (three contributions, each of which is $\sim \sigma(1D)_{\text{direct}}$)

• The normalization for $|\bar{b}c(P, 8)g\rangle$, $|\bar{b}c(S, 8)gg\rangle$ and $|\bar{b}c(S, 1)gg\rangle$ states is unknown. The naive normalization cannot be regarded as reliable !

Conclusions

- The $B_c(2S)$ excitations have been observed at LHC in the $B_c\pi^+\pi^-$ spectrum.
- At very large statistics it would be possible to distinguish two peaks in the $B_c \pi^+ \pi^-$ mass spectrum: one peak near 7000 MeV formed by 1^1D_2 state and another one near 6930 MeV formed by 1^1D_1 , 1^1D_2 and 1^1D_3 states decaying to $B_c^*\pi^+\pi^-$ with further radiative decay $B_c^* \xrightarrow{\gamma} B_c$.
- Also the *D*-wave B_c excitations could be found in cascade radiative decays $B_c(1D) \xrightarrow{\gamma} B_c(1P) \xrightarrow{\gamma} B_c(1S)$.
- Considering the main color singlet contribution we estimate $B_c(1D)$ states yield in hadronic production as $0.6 \div 1.8\%$ with respect to the direct production of $B_c(1S)$ (approximately $0.4 \div 1.1\%$ with respect to all produced B_c).
- Our estimations for *D*-wave states of B_c in hadronic production do not contradict the estimations [Cheung and Yuan(1996)] for e^+e^- -annihilation.
- The significant experimental excess of the relative yield over the value $0.4 \div 1.1\%$ will indicate an essential contribution of the color octet states to the production.
- We propose to search for *D*-excitations in $B_c \pi^+ \pi^-$ spectrum at LHC at large statics. However we have to conclude that it is quite a challenging experimental task.

Thank for your attention!

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Backup slides

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ATLAS results for $B_c(2S)$



The papers with mass predictions for D-wave states of B_c -mesons

EQ [Eichten and Quigg(1994)] GKLT [Gershtein et al.(1995)Gershtein, Kiselev, Likhoded, and Tkabladze] ZVR [Zeng et al.(1995)Zeng, Van Orden, and Roberts] FUI [Fulcher(1999)] EFG [Ebert et al.(2003)Ebert, Faustov, and Galkin] GI [Godfrey(2004)] MBV [Monteiro et al.(2017)Monteiro, Bhat, and Vijaya Kumar] SJSCP [Soni et al.(2018)Soni, Joshi, Shah, Chauhan, and Pandya] LLLGZ [Li et al.(2019)Li, Liu, Lu, Lü, Gui, and Zhong]

B_c -state	$ R(0) ^2$, $ R''(0) ^2$ [a]	$ R(0) ^2$, $ R''(0) ^2$ [b]
$1^{1}S_{0}$	2.68 GeV^3	$0.97 { m GeV}^3$
$1^{3}S_{1}$	$1.09 \mathrm{GeV}^3$	0.66 GeV^3
1^1D_2	$0.078 { m GeV}^7$	
$1^{3}D_{1}$	$0.314 { m GeV}^7$	$0.055 \text{ C} \cdot 1/3$
$1^{3}D_{2}$	0.098 GeV^7	0.055 GeV
$1^{3}D_{3}$	0.061 GeV^7	

Table: B_c meson wave functions within the quasipotential models.

[a] [Ebert et al.(2011)Ebert, Faustov, and Galkin, Galkin(2019)],
[b] [Berezhnoy et al.(2019)Berezhnoy, Martynenko, Martynenko, and Sukhorukova, Martynenko(2019)].

$$\begin{split} & {R_D^{\prime\prime}(0)|}^2_{\rm eff} = (3|R_{13\,D_1}^{\prime\prime}(0)|^2 + 5|R_{13\,D_2}^{\prime\prime}(0)|^2 + 7|R_{13\,D_3}^{\prime\prime}(0)|^2 + 5|R_{11\,D_2}^{\prime\prime}(0)|^2)/20, \\ & |R_S(0)|^2_{\rm eff} = (|R_{11\,S_0}^{\prime\prime}(0)|^2 + 3|R_{13\,S_1}(0)|^2)/4. \end{split}$$

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Bibliography

A. Berezhnoy , <u>I. Belov</u>, A. Likhoded (S. D-wave B_c meson production at LHC

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```
Relative cross sections of the B_c^+(2S) and B_c^{*+}(2S) states with respect to the B_c^+ state in proton-proton collisions at \sqrt{s} = 13 TeV.
5 2020.
```



Georges Aad et al.

Observation of an Excited B_c^{\pm} Meson State with the ATLAS Detector. *Phys. Rev. Lett.*, 113(21):212004, 2014. doi: 10.1103/PhysRevLett.113.212004.



Roel Aaij et al.

```
Observation of an excited B_c^+ state.
2019.
```



```
Ishrat Asghar, Faisal Akram, Bilal Masud, and M. Atif Sultan.
Properties of excited charmed-bottom mesons.
Phys. Rev. D, 100(9):096002, 2019.
doi: 10.1103/PhysRevD.100.096002.
```

A. V. Berezhnoy, A. P. Martynenko, F. A. Martynenko, and O. S. Sukhorukova. Exclusive double B_c meson production from e^+e^- annihilation into two virtual photons.

Nucl. Phys. A, 986:34-47, 2019.

doi: 10.1016/j.nuclphysa.2019.03.006.

A. Berezhnoy , <u>I. Belov</u>, A. Likhoded (C D-wave B_c meson production at LHC

```
09.11.2021 23 / 23
```

A. V. Berezhnoy, I. N. Belov, and A. K. Likhoded.

Production of *D*-wave states of $\bar{b}c$ quarkonium at the LHC. *Phys. Rev. D*, 103(11):114001, 2021. doi: 10.1103/PhysRevD.103.114001.



Chiral Symmetry and psi-prime — psi + pi + pi Decay. *Phys.Rev.Lett.*, 35:1, 1975. doi: 10.1103/PhysRevLett.35.1.

King-man Cheung and Tzu Chiang Yuan.

Heavy quark fragmentation functions for \boldsymbol{d} wave quarkonium and charmed beauty mesons.

09.11.2021

23 / 23

Phys. Rev., D53:3591–3603, 1996. doi: 10.1103/PhysRevD.53.3591.

S. Dulat, T. J. Hou, J. Gao, M. Guzzi, J. Huston, P. Nadolsky, J. Pumplin, C. Schmidt, D. Stump, and C. P. Yuan.

The structure of the proton: The CT14 QCD global analysis.

EPJ Web Conf., 120:07003, 2016.

doi: 10.1051/epjconf/201612007003.

A. Berezhnoy , I. Belov, A. Likhoded (5 D-wave Bc meson production at LHC

D. Ebert, R. N. Faustov, and V. O. Galkin.

Properties of heavy quarkonia and B_c mesons in the relativistic quark model. *Phys. Rev.*, D67:014027, 2003. doi: 10.1103/PhysRevD.67.014027.



D. Ebert, R. N. Faustov, and V. O. Galkin.

Spectroscopy and Regge trajectories of heavy quarkonia and B_c mesons. *Eur. Phys. J.*, C71:1825, 2011. doi: 10.1140/epjc/s10052-011-1825-9.

Estia J. Eichten and Chris Quigg.
 Mesons with beauty and charm: Spectroscopy.
 Phys. Rev., D49:5845–5856, 1994.
 doi: 10.1103/PhysRevD.49.5845.

Estia J Eichten and Chris Quigg.
Mesons with Beauty and Charm: New Horizons in Spectroscopy. *Phys. Rev.*, D99(5):054025, 2019.
doi: 10.1103/PhysRevD.99.054025.



Lewis P. Fulcher.

Phenomenological predictions of the properties of the B_c system. $E \rightarrow C = P$

A. Berezhnoy , <u>I. Belov</u>, A. Likhoded (S. D-wave B_c meson production at LHC

09.11.2021 23 / 23

Phys. Rev., D60:074006, 1999. doi: 10.1103/PhysRevD.60.074006.



V. O. Galkin.

Private communications: wave functions for bc(2s) states.

Private communications: wave functions for Bc(2S) states, 2019.



S.S. Gershtein, V.V. Kiselev, A.K. Likhoded, and A.V. and Tkabladze. Physics of B(c) mesons. Phys. Usp., 38:1-37, 1995. doi: 10.1070/PU1995v038n01ABEH000063.



Stephen Godfrey.

Spectroscopy of B_c mesons in the relativized quark model. Phys.Rev., D70:054017, 2004. doi: 10.1103/PhysRevD.70.054017.



I.P. Gouz, V.V. Kiselev, A.K. Likhoded, V.I. Romanovsky, and O.P. Yushchenko. Prospects for the B_c studies at LHCb.

23 / 23

Phys.Atom.Nucl., 67:1559-1570, 2004. doi: 10.1134/1.1788046,10.1134/1.1788046.



V. V. Kiselev, A. K. Likhoded, and A. V. Tkabladze. < => < => < => 09.11.2021

A. Berezhnoy , I. Belov, A. Likhoded (5 D-wave Bc meson production at LHC

B(c) spectroscopy.

Phys. Rev., D51:3613–3627, 1995. doi: 10.1103/PhysRevD.51.3613.

R. Kleiss, W. James Stirling, and S. D. Ellis.

A New Monte Carlo Treatment of Multiparticle Phase Space at High-energies. *Comput. Phys. Commun.*, 40:359, 1986. doi: 10.1016/0010-4655(86)90119-0.

Qi Li, Ming-Sheng Liu, Long-Sheng Lu, Qi-Fang Lü, Long-Cheng Gui, and Xian-Hui Zhong.

The excited bottom-charmed mesons in a nonrelativistic quark model. 2019.

A. P. Martynenko.

Private communications: wave functions for bc(2s) states. Private communications: wave functions for Bc(2S) states, 2019.

Antony Prakash Monteiro, Manjunath Bhat, and K. B. Vijaya Kumar.

Mass spectra and decays of ground and orbitally excited $c\bar{b}$ states in nonrelativistic quark model.

Int. J. Mod. Phys., A32(04):1750021, 2017.

doi: 10.1142/S0217751X1750021X.



V.A. Novikov and Mikhail A. Shifman.

Comment on the psi-prime - J/psi pi pi Decay.

Z.Phys., C8:43, 1981. doi: 10.1007/BF01429829.

Albert M Sirunyan et al.

Observation of Two Excited $B_{\rm c}^+$ States and Measurement of the $B_{\rm c}^+(2S)$ Mass in pp Collisions at $\sqrt{s}=13$ TeV.

Phys. Rev. Lett., 122(13):132001, 2019.

doi: 10.1103/PhysRevLett.122.132001.

Albert M Sirunyan et al.

Measurement of $B_c(2S)^+$ and $B_c^*(2S)^+$ cross section ratios in proton-proton collisions at $\sqrt{s} = 13$ TeV.

09.11.2021

23/23

8 2020.



N. R. Soni, B. R. Joshi, R. P. Shah, H. R. Chauhan, and J. N. Pandya. $Q\bar{Q}$ ($Q \in \{b, c\}$) spectroscopy using the Cornell potential. *Eur. Phys. J.*, C78(7):592, 2018. doi: 10.1140/epjc/s10052-018-6068-6.



Mikhail B. Voloshin.

Adler's Selfconsistency Condition in the Decay psi-prime (3700) — psi (3100) pi pi. *JETP Lett.*, 21:347–348, 1975.

- Mikhail B. Voloshin and Valentin I. Zakharov.
 Measuring QCD Anomalies in Hadronic Transitions Between Onium States.
 Phys.Rev.Lett., 45:688, 1980.
 doi: 10.1103/PhysRevLett.45.688.

J. Zeng, J. W. Van Orden, and W. Roberts. Heavy mesons in a relativistic model. *Phys. Rev.*, D52:5229–5241, 1995. doi: 10.1103/PhysRevD.52.5229.