

# Search for the QCD Critical Point in Heavy-ion Collisions at RHIC

---



Xiaofeng Luo

Central China Normal University

November 13, 2020

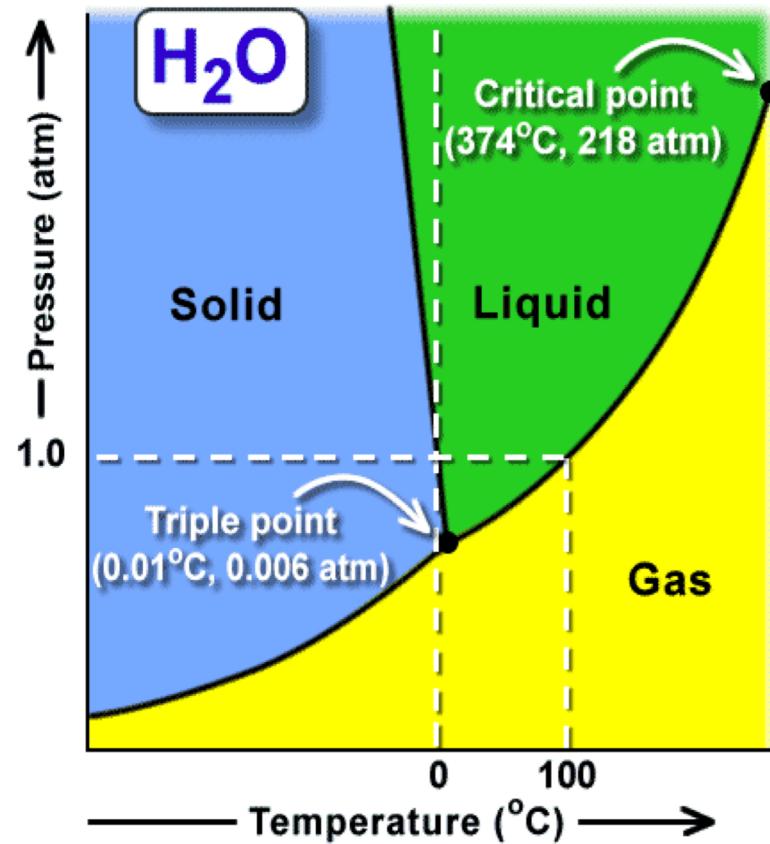




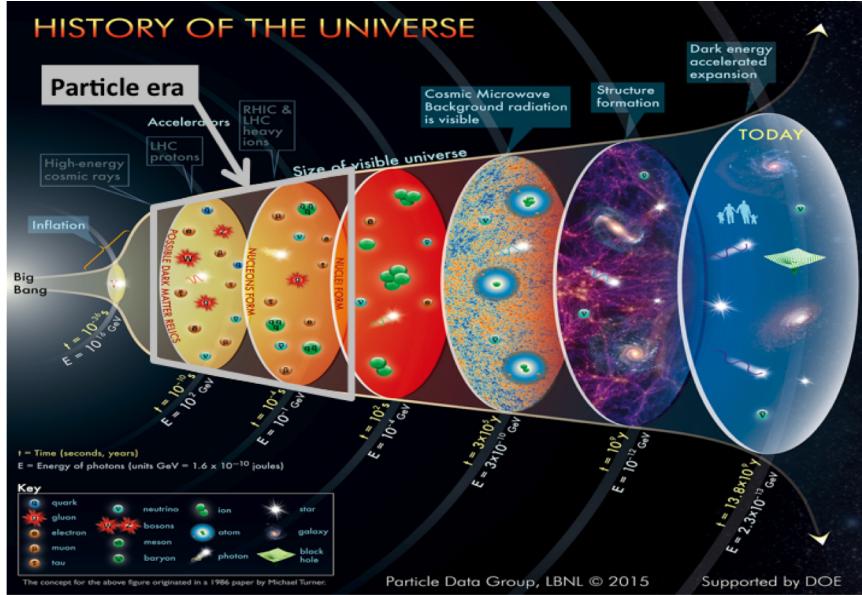
# Phase Diagram: Water



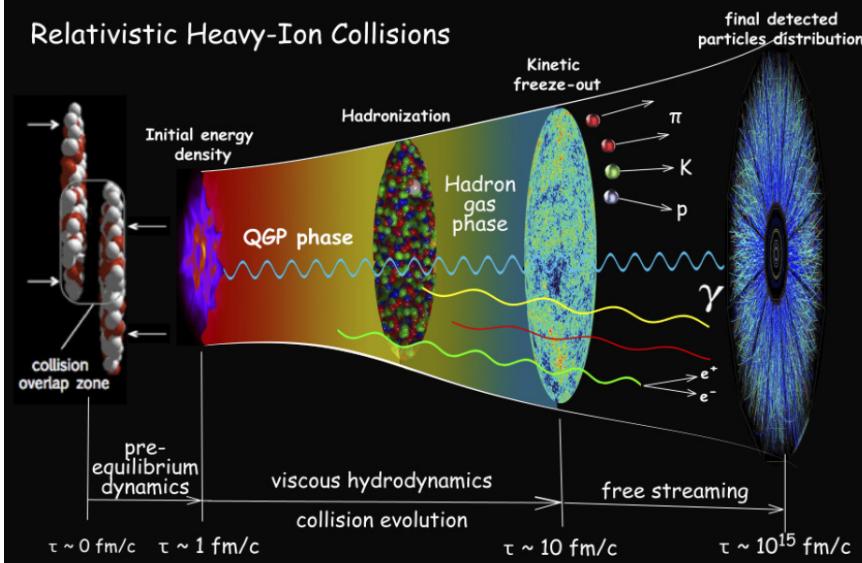
# How matter self-organized by varying external conditions.



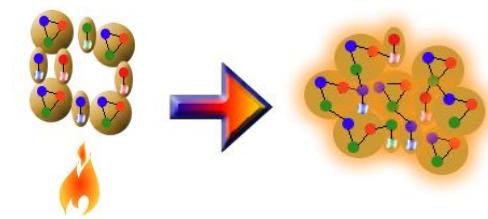
## Big Bang



## Little Bang



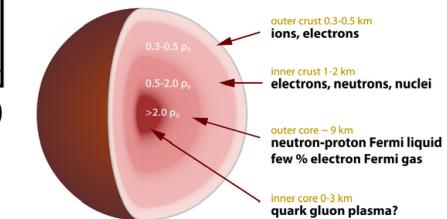
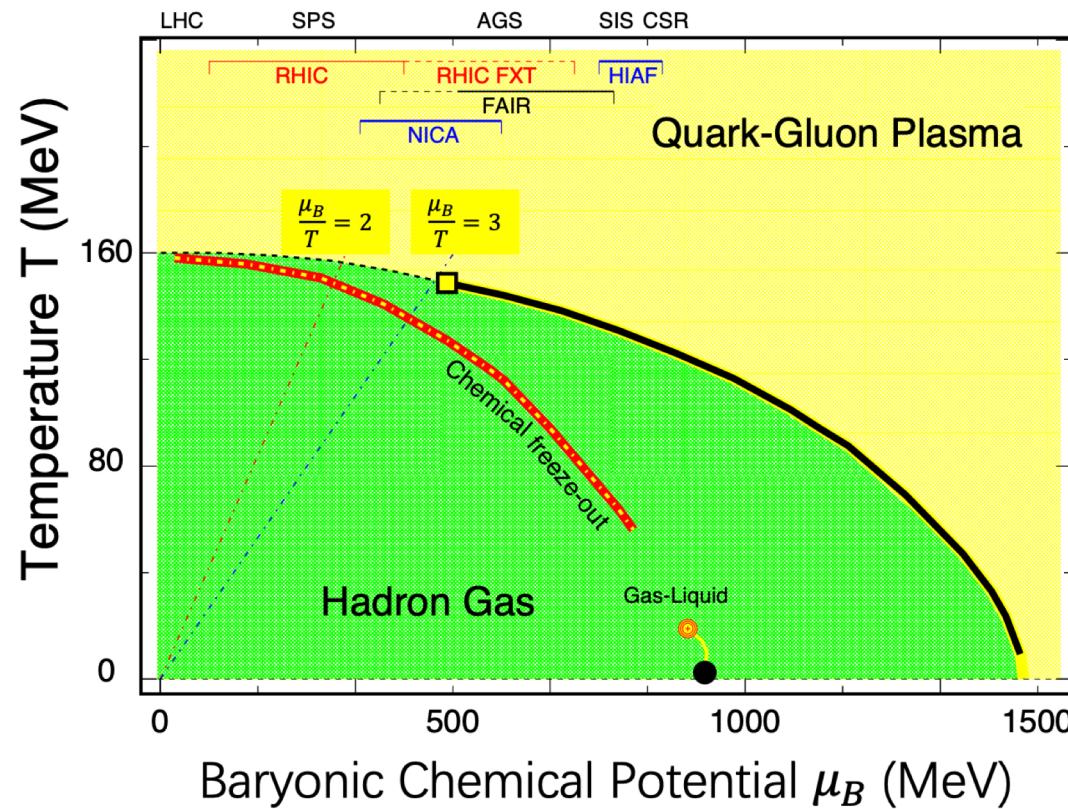
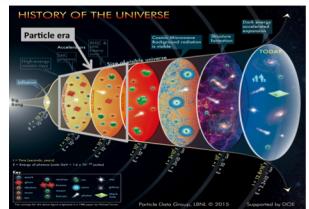
**Quark-Gluon Plasma (QGP):** a state of matter where the quarks and gluons are the relevant degrees of freedom, exist at few  $\mu$ s after the Big-Bang



Relativistic heavy-ion collisions are a unique tool to create and study hot QCD matter and its phase transition under controlled conditions

T. D. Lee and G. C. Wick, Phys. Rev. D 9, 2291 (1974). Vacuum stability and vacuum excitation in a spin-0 field theory.

# QCD Phase Diagram



Y. Aoki et al., Nature 443, 675 (2006); A. Bazavov et al, PRD 85, 054503 (2012).

K. Fukushima and C. Sasaki, Prog. Part. Nucl. Phys, 72, 99 (2013).

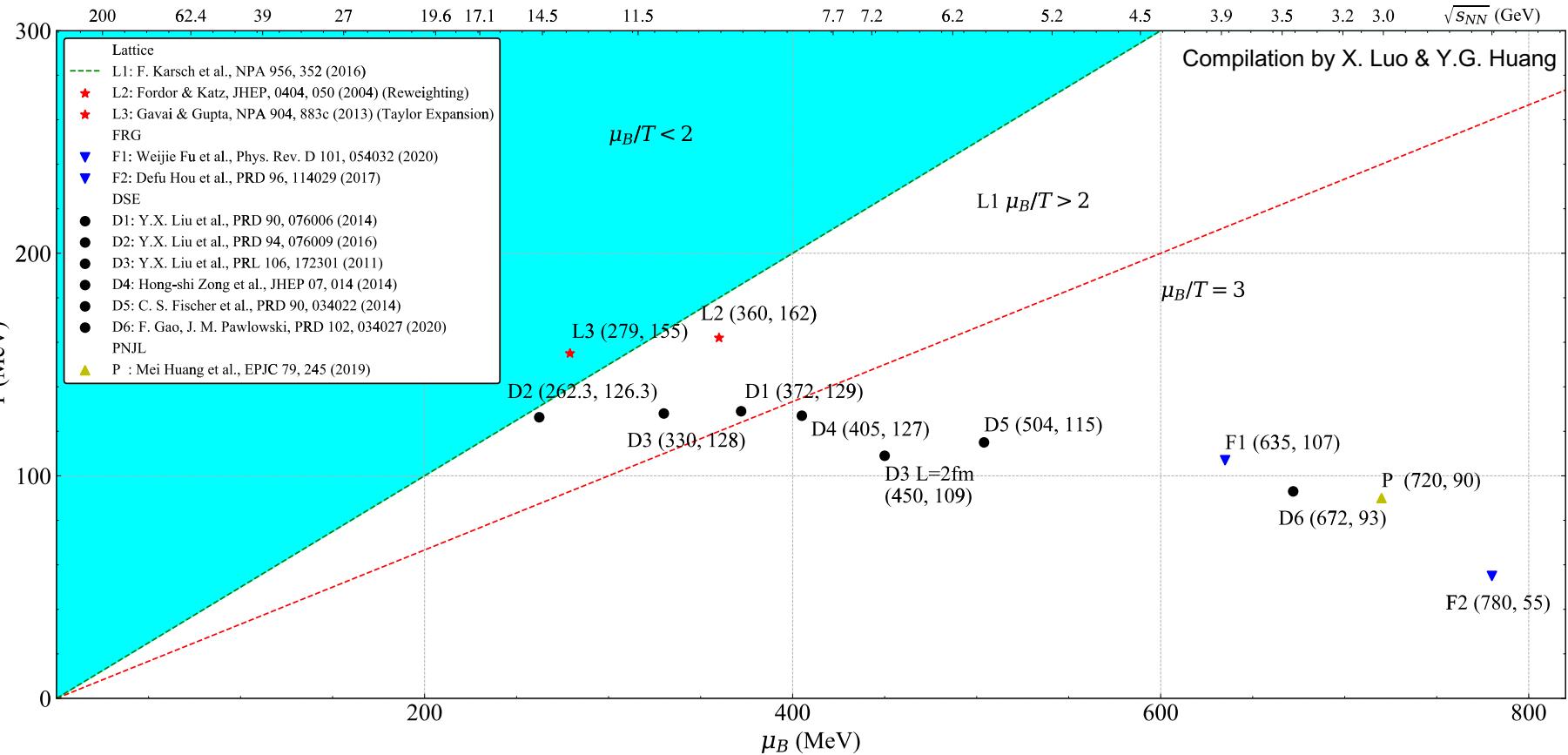
A. Bzdak et al., Phys. Rep. 853, 1 (2020).

**Key question : is there a QCD critical point at finite baryon density region?**

Its confirmation will greatly enhance our understanding of the universe evolution and structure of visible matter.

# Location of CP : Theoretical Prediction

*A preliminary collection from Lattice, DSE, FRG and PNJL (2004-2020)*

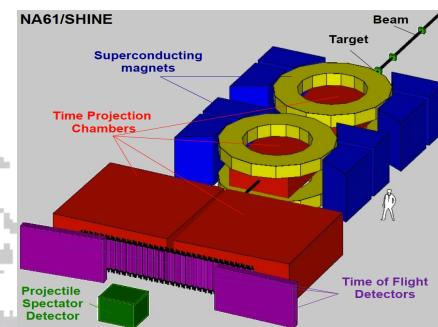


Large uncertainties for the theoretical estimation of CP location.



# Current and Future Facilities for exploring the QCD Phase Structure

## CERN SPS



Fix target

$\sqrt{s_{NN}} = 5\text{-}17 \text{ GeV}$

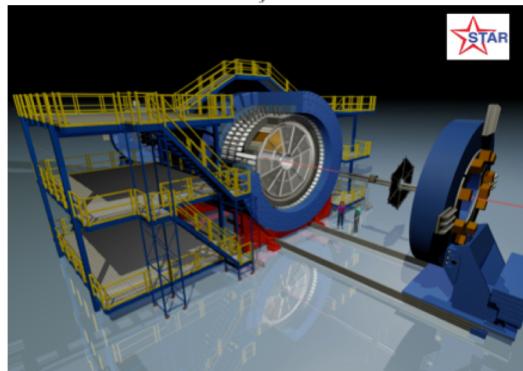
SPS

BNL/RHIC STAR

RHIC

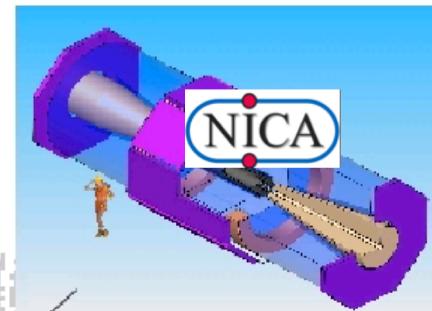
BES-I (2010-2017)

BES-II (2018-2021) is ongoing.



Collider  $\sqrt{s_{NN}} = 7.7\text{-}200 \text{ GeV}$

## Construction....



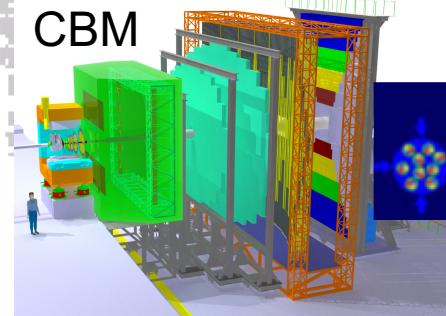
Collider

$\sqrt{s_{NN}} = 4\text{-}11 \text{ GeV}$  (2023-)

CEE@Lanzhou

JPARC@Japan

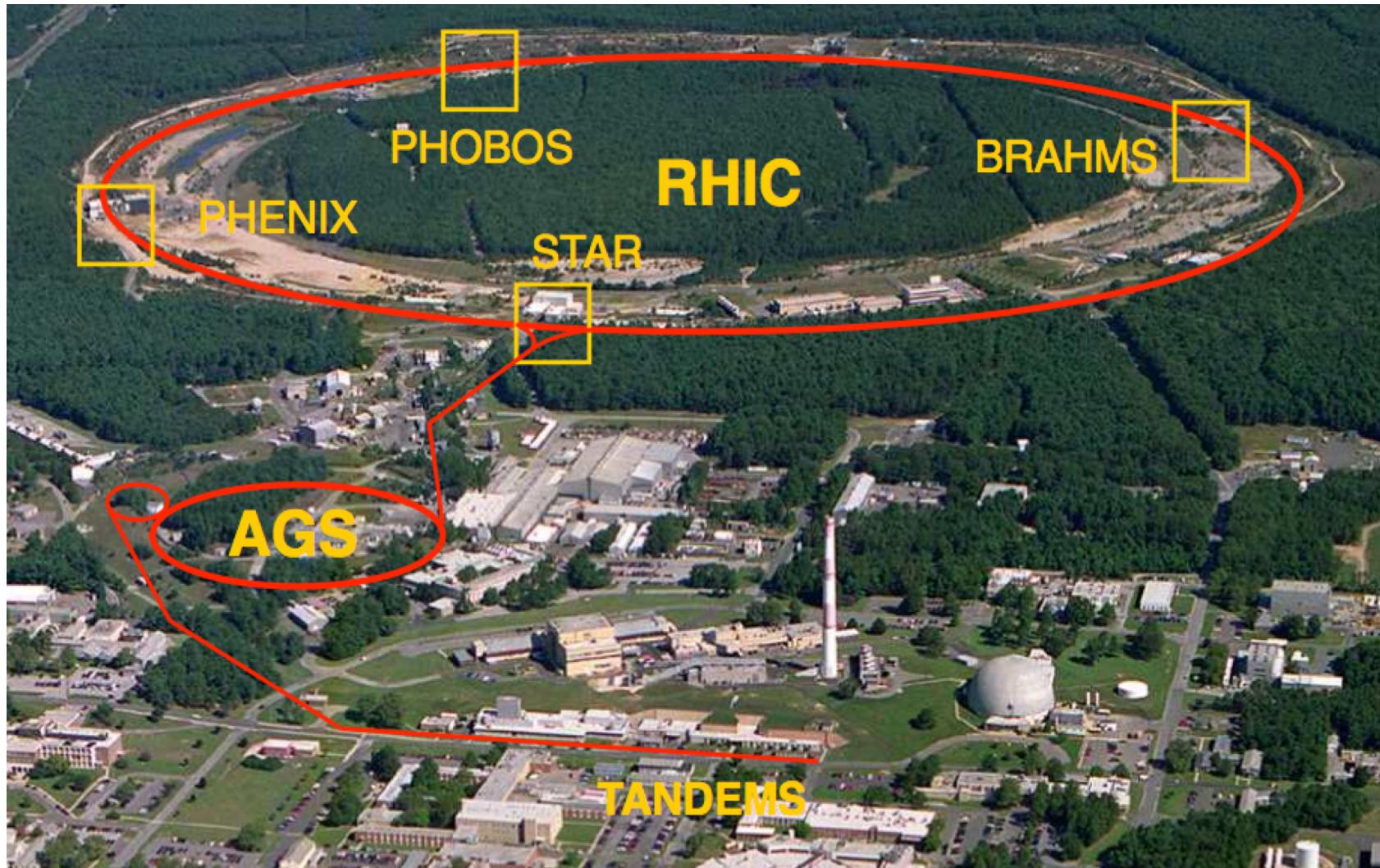
## Construction....



Fix target

$\sqrt{s_{NN}} = 2\text{-}5 \text{ GeV}$  (2025-)

# Relativistic Heavy-ion Collider (RHIC)



- RHIC: The high energy heavy-ion collider  $\sqrt{s} = 200 - 5 \text{ GeV}$
- RHIC: The highest energy polarized proton collider (500 GeV)

# STAR Detector System

EEMC

Magnet

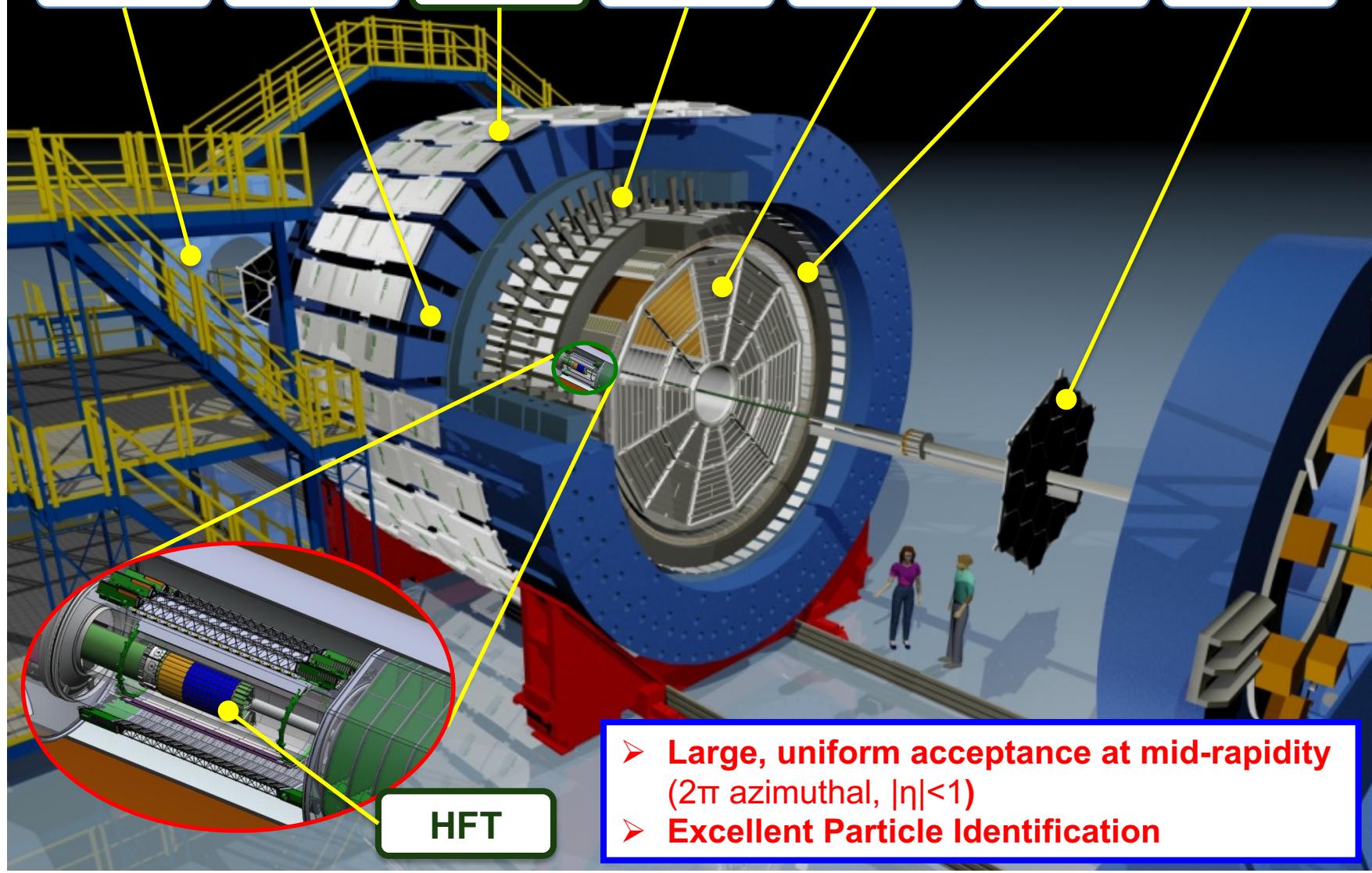
MTD

BEMC

TPC

TOF

BBC





# RHIC Beam Energy Scan - I (2010-2017)

## Au+Au Collisions

| $\sqrt{s_{NN}}$<br>(GeV) | Events<br>( $\times 10^6$ ) | Year | ${}^*\mu_B$<br>(MeV) | ${}^*T_{CH}$<br>(MeV) |
|--------------------------|-----------------------------|------|----------------------|-----------------------|
| 200                      | 238                         | 2010 | 25                   | 166                   |
| 62.4                     | 46                          | 2010 | 73                   | 165                   |
| 54.4                     | 1200                        | 2017 | 83                   | 165                   |
| 39                       | 86                          | 2010 | 112                  | 164                   |
| 27                       | 30                          | 2011 | 156                  | 162                   |
| 19.6                     | 15                          | 2011 | 206                  | 160                   |
| 14.5                     | 13                          | 2014 | 264                  | 156                   |
| 11.5                     | 7                           | 2010 | 315                  | 152                   |
| 7.7                      | 3                           | 2010 | 420                  | 140                   |

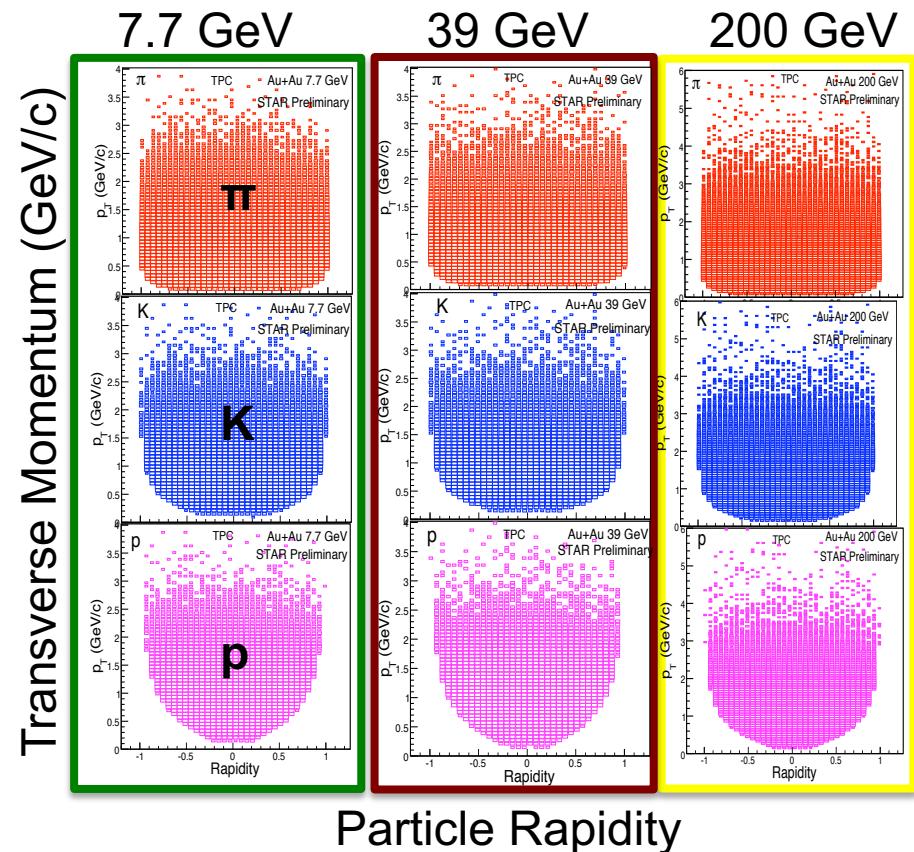
$(\mu_B, T_{CH})$  : J. Cleymans et al., PRC73, 034905 (2006)

STAR, arXiv:1007.2613

<https://drupal.star.bnl.gov/STAR/starnotes/public/sn0493>

<https://drupal.star.bnl.gov/STAR/starnotes/public/sn0598>

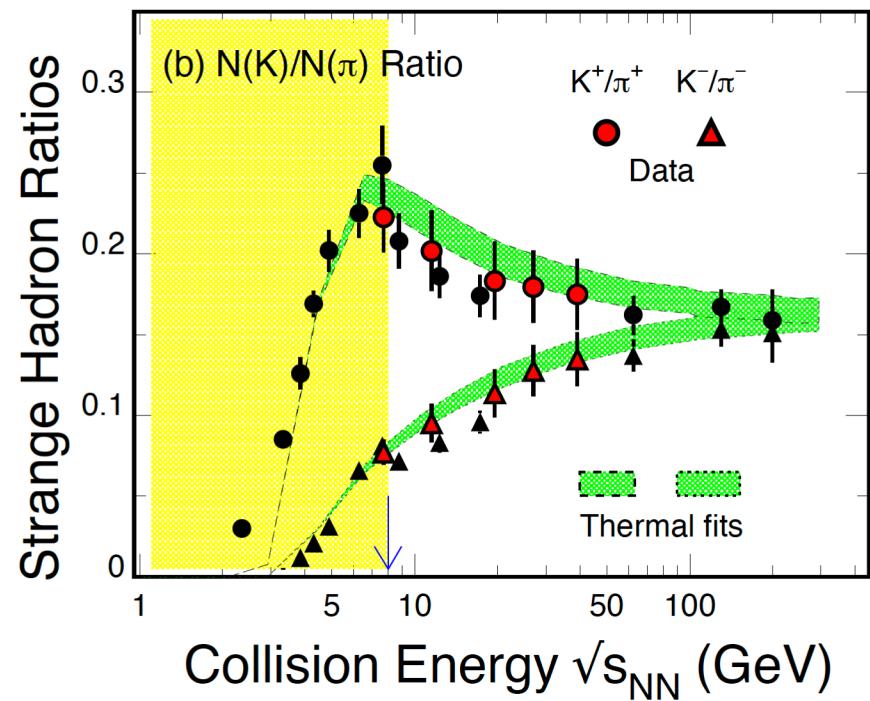
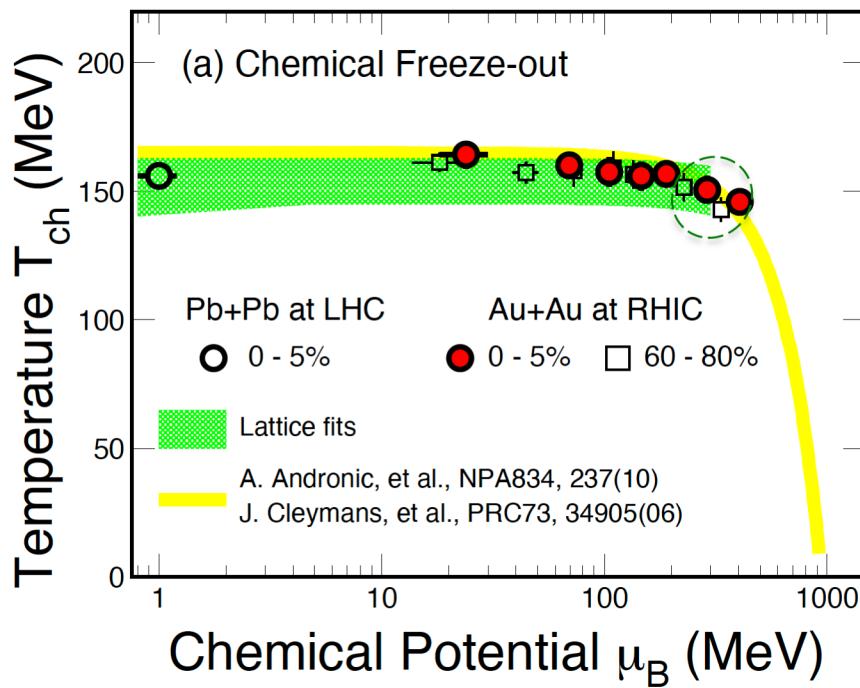
## Uniform acceptance at Mid-rapidity



- Access the QCD phase diagram: vary collision energies and/or system size.
- RHIC BES-I :  $25 < \mu_B < 420$  MeV**

# Chemical freeze-out and QCD phase boundary

By courtesy of Dr. N. Xu

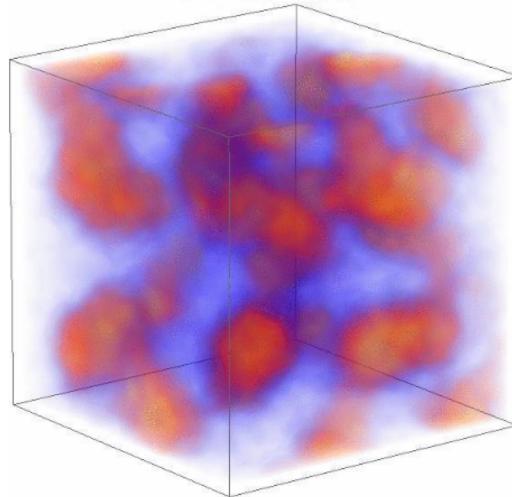


- The chemical freeze-out  $T$  and  $\mu_B$  (GCE) are close to the phase boundary determined from Lattice QCD with  $\mu_B < 300$  MeV.
- The peak of  $K^+/\pi^+$  ratio around 8 GeV can be well described by thermal model, where the system start to enter into “high baryon density region”. ( $< 8$  GeV,  $\mu_B > 420$  MeV)

STAR : PRC96, 044904 (2017); PRC 102, 034909 (2020). ALICE : PRL 109, 252301 (2012), PRC 88, 044910 (2013).

A. Andronic, P. Braun-Munzinger, K. Redlich, J. Stachel, Nature 561, 321 (2018). X. Luo, S. Shi, N. Xu and Y. Zhang, Particle 3, 278 (2020); K. Fukushima, B. Mohanty, N. Xu, arXiv: 2009.03006; J. Randrup et al., Phys. Rev. C74, 047901(2006).

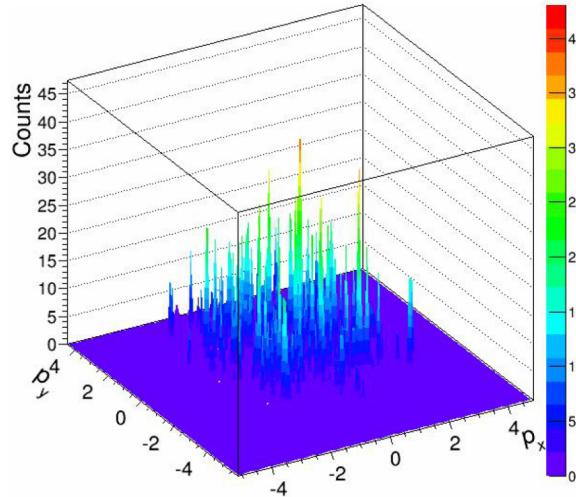
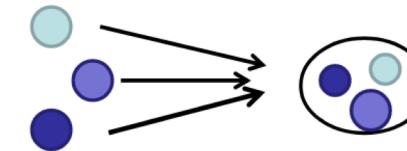
# Sensitive observables for QCD phase transition



In the vicinity of critical point and/or  
1<sup>st</sup> order phase transition



Large density fluctuations and Baryon clustering



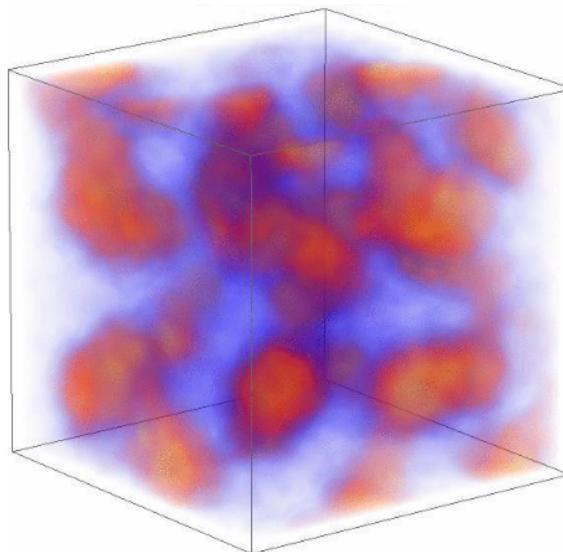
Higher moments of  
conserved charge  
(B, Q, S) distributions

light nuclei production

**Experimental Signatures:  
Non-monotonic variation as a function of  
collision energy.**

# Light nuclei production as probes of QCD phase structure

Near first order P.T. or critical point :  
large density fluctuations and baryon clustering



Based on coalescence model:

$$N_d = \frac{3}{2^{1/2}} \left( \frac{2\pi}{m_0 T_{eff}} \right)^{3/2} N_p \langle n \rangle (1 + C_{np})$$

$$N_t = \frac{3^{\frac{3}{2}}}{4} \left( \frac{2\pi}{m_0 T_{eff}} \right)^3 N_p \langle n \rangle^2 (1 + \Delta n + 2C_{np})$$

**New observable : Yield ratio of light nuclei**

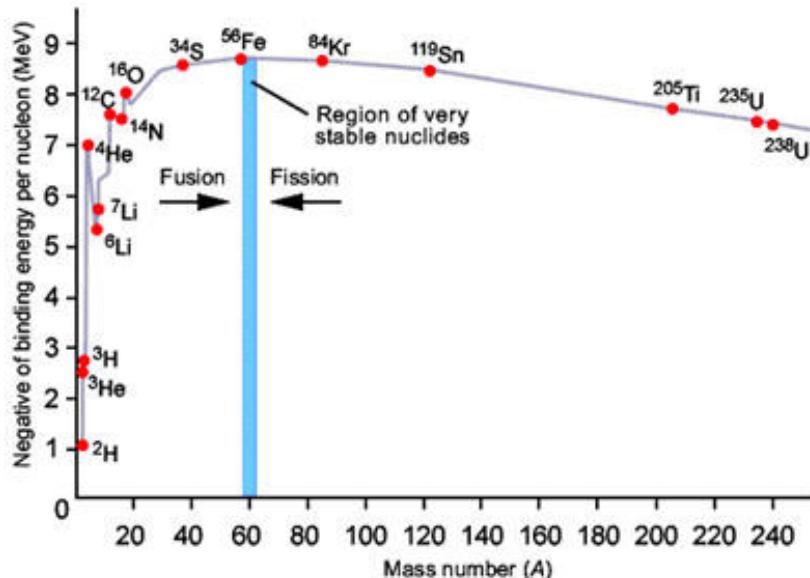
$$N_t \cdot N_p / N_d^2 \approx g(1 + \Delta n)$$

Neutron density fluctuations  $\Delta n = \langle (\delta n)^2 \rangle / \langle n \rangle^2$   
 $g=0.29$

Yield ratio of light nuclei is sensitive to the baryon density fluctuations and can be used to probe the signature of 1st order phase transition and/or critical point in heavy-ion collisions.

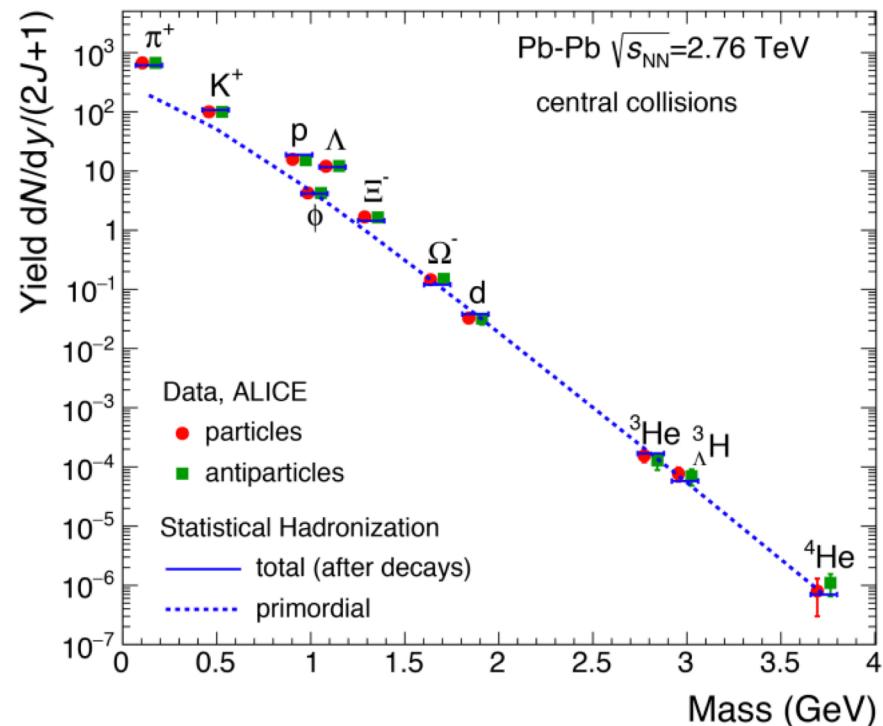
- K.J. Sun, L.W. Chen, C.M. Ko, and Z.B. Xu, PLB 774, 103 (2017);
- K.J. Sun, L.W. Chen, C.M. Ko, J. Pu, and Z.B. Xu, PLB781, 499 (2018)
- Edward Shuryak, Juan M. Torres-Rincon, PRC 100, 024903 (2019); PRC 101, 034914 (2020); EPJA 56, 241 (2020).

# Light Nuclei production in high energy nuclear collisions



| nucleus       | rms radius (fm)     |
|---------------|---------------------|
| deuteron      | $2.1421 \pm 0.0088$ |
| triton        | $1.7591 \pm 0.0363$ |
| $^3\text{He}$ | $1.9661 \pm 0.0030$ |
| $^4\text{He}$ | $1.6755 \pm 0.0028$ |
| $^3\text{H}$  | 4.9                 |
| $\Lambda$     |                     |

Braun-Munzinger, Dönigus, NPA 987, 144 (2019).  
 Benjamin Dönigus, IJMPPE 29, 2040001 (2020).  
 J. Chen, et al., Phys. Rep. 760, 1 (2018).  
 D. Oliinychenko, et al., Phys. Rev. C 99, 044907 (2019).  
 Y. Oh, Z.W. Lin, C.M. Ko, Phys. Rev. C 80, 064902 (2009).  
 S. Sombun et al., Phys. Rev. C 99, 014901 (2019).

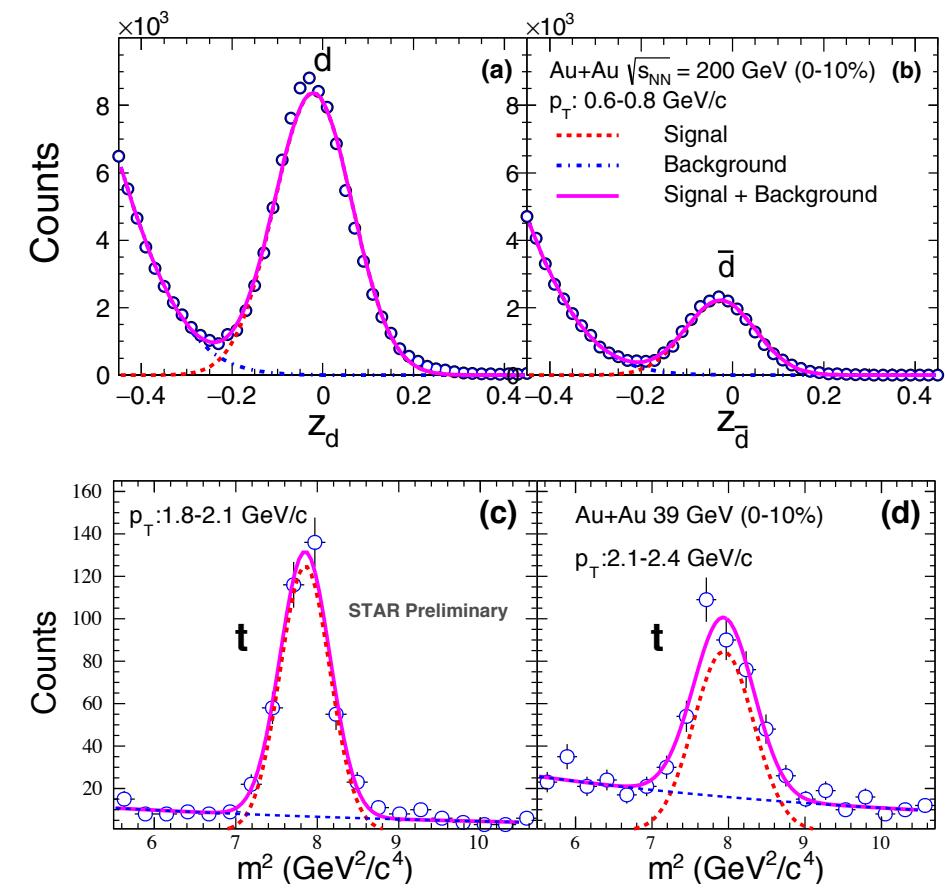
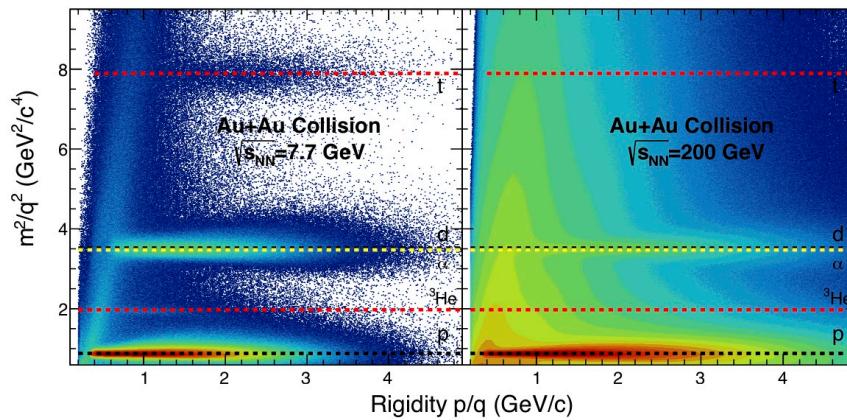
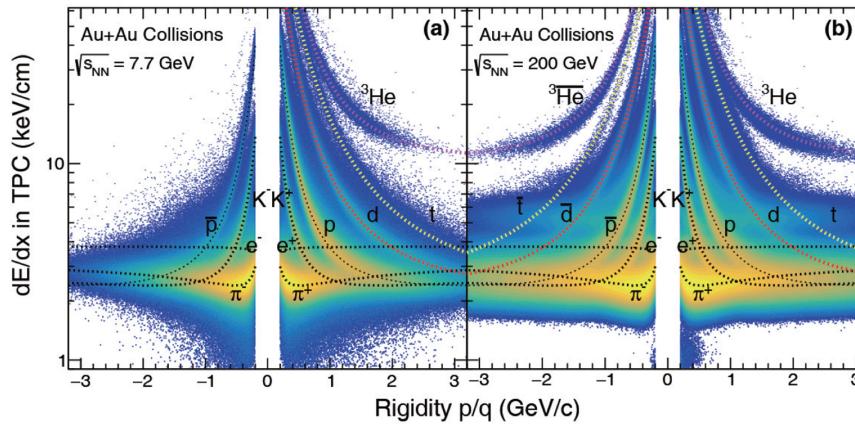


“Snowball in hell” ?

- Light nuclei ( $d$ ,  $t$ ,  $^3\text{He}$ ): loosely bond object with few MeV binding energies can be produced in HIC.
- Understanding the production mechanism of light nuclei in HIC will provide baseline to map the QCD phase boundary.  
coalescence、 microscopic interactions、 thermal production ?

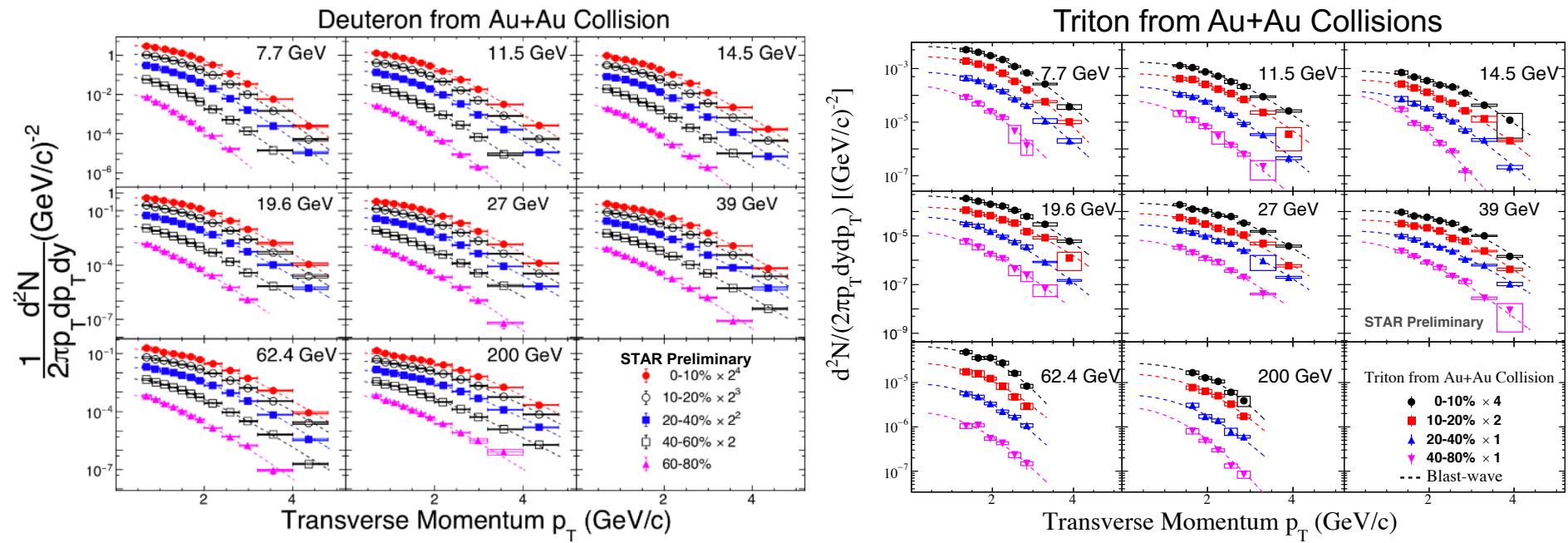
# Particle Identification

TPC : Low  $p_T$    TPC+TOF : High  $p_T$



- 1) TPC and TOF efficiency correction
- 2) Energy loss corrections
- 3) Absorption corrections
- 4) Background subtraction

# Deuteron and triton production from BES-I at RHIC



Dash lines (blast-wave function fits) : 
$$\frac{d^2N}{p_T dp_T dy} \propto \int_0^R r dr m_T I_0\left(\frac{p_T \sinh \rho}{T}\right) K_1\left(\frac{m_T \cosh \rho}{T}\right)$$

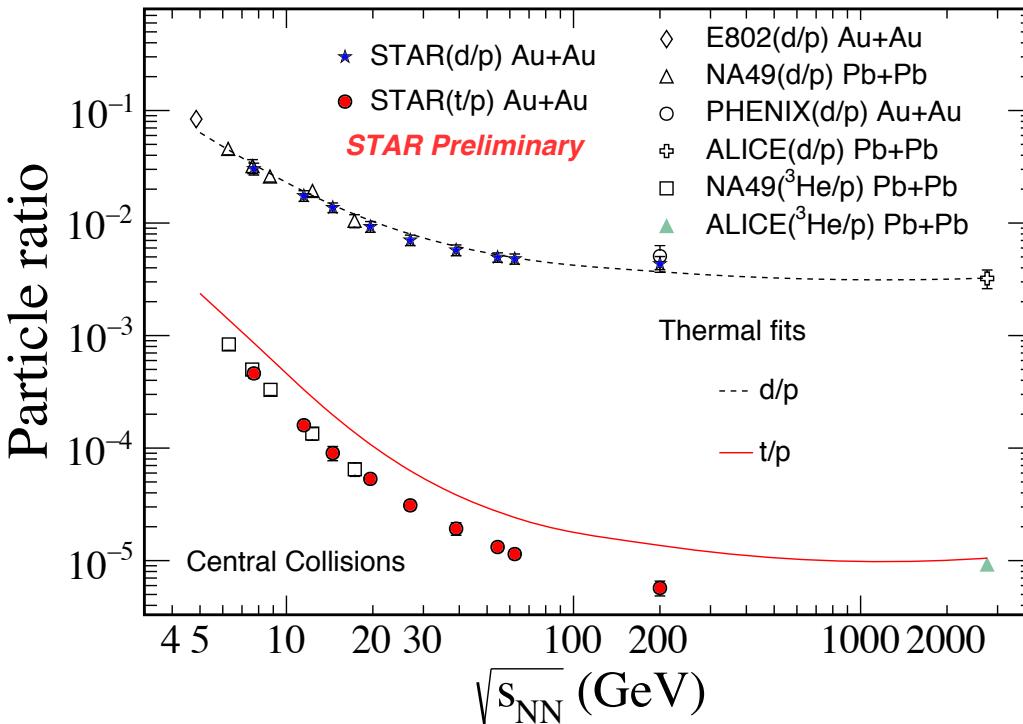
E. Schnedermann, J. Sollfrank, and U. Heinz, PRC 48,2462 (1993).

STAR BES-I data :

Deuteron, Phys. Rev. C 99, 064905 (2019).

Triton : Dingwei Zhang (for STAR), QM2019 [arXiv : 2002.10677]; Hui Liu, Poster, QM2019.

# Energy dependence of d/p and t/p ratios



Thermal model inputs:

$$T_{CF} = T_{CF}^{lim} / (1 + \exp(2.60 - \ln(\sqrt{s_{NN}})/0.45))$$

$$\mu_B = a / (1 + 0.288\sqrt{s_{NN}})$$

With  $\sqrt{s_{NN}}$  in GeV

$T_{CF}^{lim} = 158.4$  MeV and  $a = 1307.5$  MeV

A. Andronic, P. Braun-Munzinger, J. Stachel, H. Stöcker, PLB 697 (2011) 203.

Proton yield corrected for weak decay feed down based on a STAR paper using UrQMD + GEANT simulation :  
<https://journals.aps.org/prl/supplemental/10.1103/PhysRevLett.121.032301>

- The d/p ratios from LHC、RHIC down to AGS energies can be well described by thermal model.
- t/p and  $^3$ He/p ratios are significant deviation and below the thermal model expectations at RHIC and SPS energies.

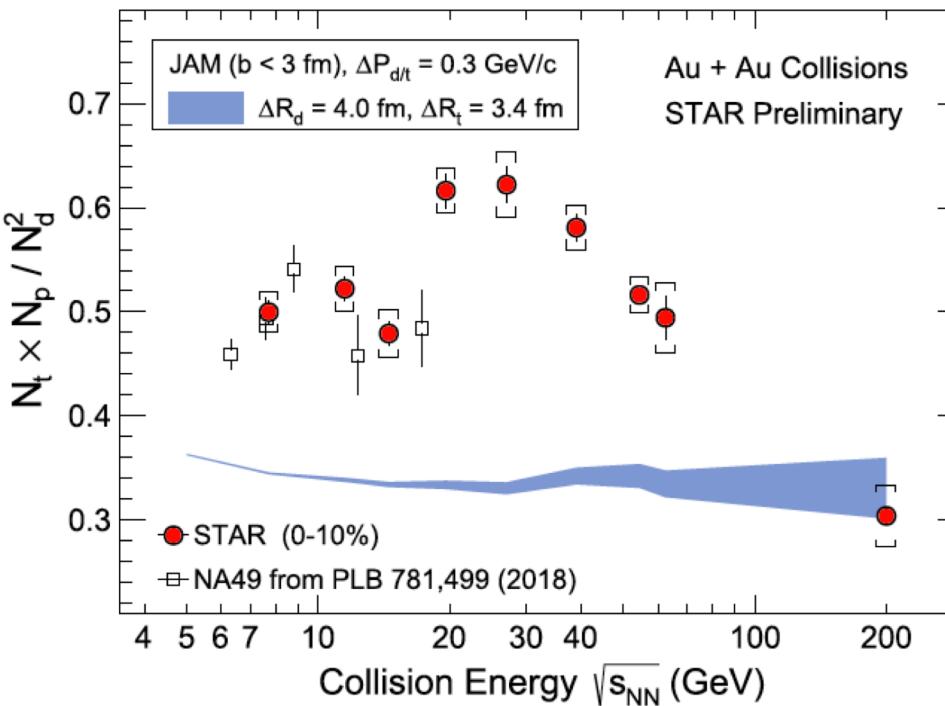
ALICE data : Phys. Rev. C 93, 024917 (2016)

STAR data : Deuteron, Phys. Rev. C 99, 064905 (2019).

Triton : Dingwei Zhang (for STAR), QM2019 [arXiv : 2002.10677]; Hui Liu, Poster, QM2019.

# Energy Dependence of Light Nuclei Yield Ratio

Dingwei Zhang (STAR), QM2019 [arXiv: 2002.10677]



The yield ratio is related to neutron density fluctuations.

$$N_t \cdot N_p / N_d^2 = g(1 + \Delta n),$$

with  $g = 0.29$

Proton yield corrected for weak decay feed down used in the left plot based on a STAR paper using UrQMD + GEANT simulation :  
<https://journals.aps.org/prl/supplemental/10.1103/PhysRevLett.121.032301>

- Yield ratio shows a non-monotonic dependence on collision energy in 0-10% Au + Au collisions, with a peak around 20-30 GeV.
- Flat energy dependence of yield ratio observed in JAM, AMPT, UrQMD, hybrid model.

JAM : H. Liu et al, Phys. Lett. B 805, 135452 (2020).  
 AMPT : K. Sun, C. M. Ko, arXiv: 2005.00182.

Hydro + transport + coal. : W. Zhao et al., arXiv: 2009.06959  
 UrQMD: X. G. Deng, Y. G. Ma, Phys. Lett. B 808, 135668 (2020)

# Higher Moments of Conserved Quantities (B, Q, S)

1. Higher order cumulants/moments: describe the shape of distributions and quantify fluctuations.  
(sensitive to the correlation length ( $\xi$ ))

$$\langle \delta N \rangle = N - \langle N \rangle$$

$$C_1 = M = \langle N \rangle$$

$$C_2 = \sigma^2 = \langle (\delta N)^2 \rangle$$

$$C_3 = S\sigma^3 = \langle (\delta N)^3 \rangle$$

$$C_4 = \kappa\sigma^4 = \langle (\delta N)^4 \rangle - 3 \langle (\delta N)^2 \rangle^2$$

M. A. Stephanov, Phys. Rev. Lett. 102, 032301 (2009).

M. Asakawa, S. Ejiri and M. Kitazawa, Phys. Rev. Lett. 103, 262301 (2009).

M. A. Stephanov, Phys. Rev. Lett. 107, 052301 (2011).

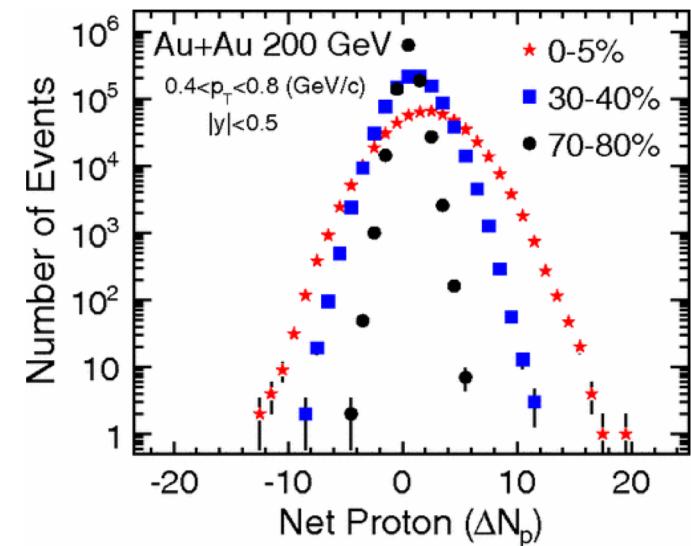
2. Direct connect to the susceptibility of the system.

$$\frac{\chi_q^4}{\chi_q^2} = \kappa\sigma^2 = \frac{C_{4,q}}{C_{2,q}} \quad \frac{\chi_q^3}{\chi_q^2} = S\sigma = \frac{C_{3,q}}{C_{2,q}},$$

$$\chi_q^{(n)} = \frac{1}{VT^3} \times C_{n,q} = \frac{\partial^n (p/T^4)}{\partial (\mu_q)^n}, q = B, Q, S$$

S. Ejiri et al, Phys. Lett. B 633 (2006) 275. Cheng et al, PRD (2009) 074505. B. Friman et al., EPJC 71 (2011) 1694. F. Karsch and K. Redlich , PLB 695, 136 (2011). S. Gupta, et al., Science, 332, 1525(2012). A. Bazavov et al., PRL109, 192302(12) // S. Borsanyi et al., PRL111, 062005(13)

## Event-by-Event Distribution



First Measurement : 2009-2010

STAR, PRL105, 022302 (2010).

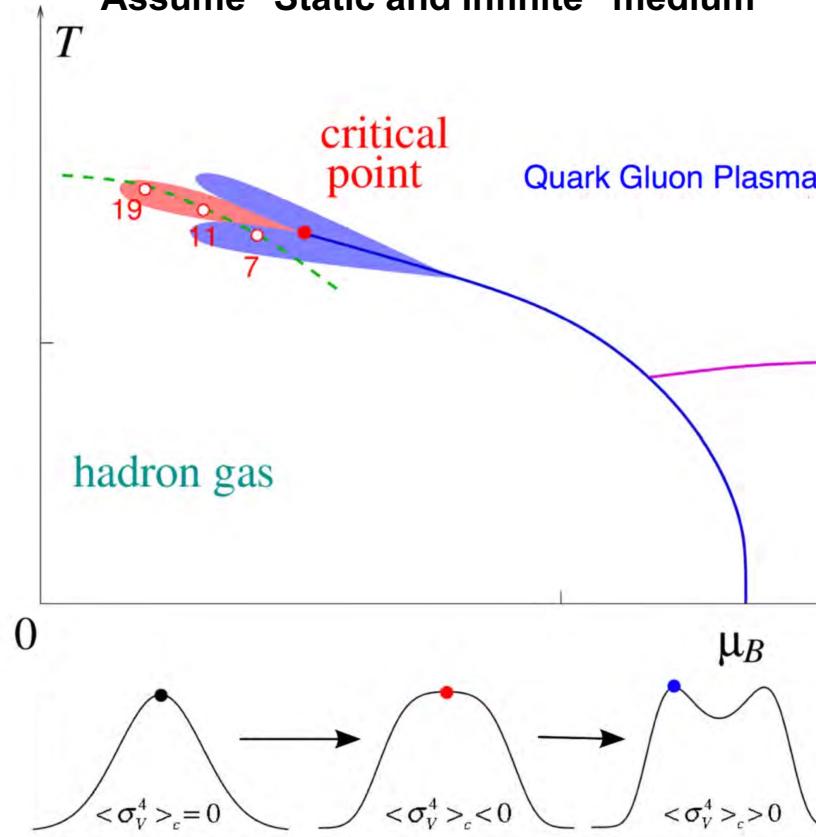
➤ **Net-Proton:**  $N_p - N_{\bar{p}}$   
(proxy: Net-Baryon)

➤ **Net-Charge:**  $N_{Q^+} - N_{Q^-}$

➤ **Net-Kaon:**  $N_{K^+} - N_{K^-}$   
(proxy: Net-Strangeness)

# Signals of QCD Critical Point : Theory/Model

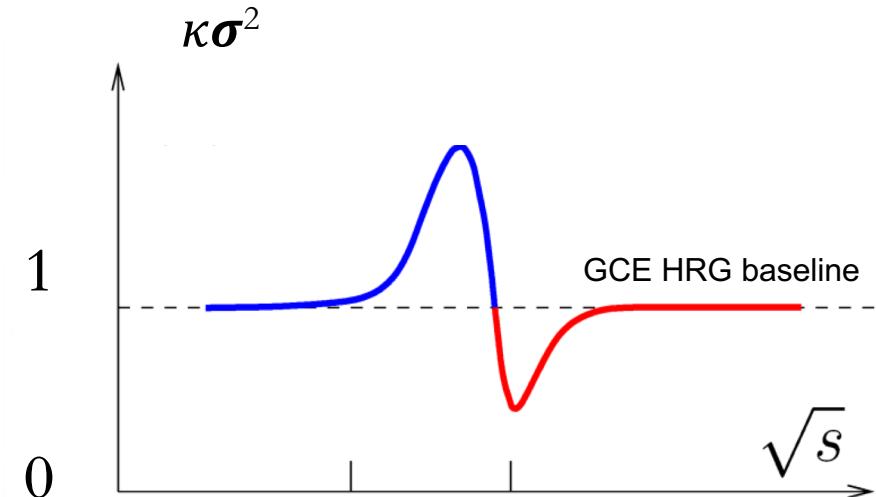
Assume "Static and Infinite" medium



M. Stephanov, PRL107, 052301 (2011); J. Phys. G 38, 124147 (2011).  
 Schaefer et al., PRD 85, 034027 (2012); W. Fu et al., PRD 94, 116020 (2016).  
 J.W. Chen, J. Deng, et al., PRD 93, 034037 (2016). PRD 95,014038 (2017).  
 W. K. Fan, X. Luo, H.S. Zong, IJMPA 32, 1750061 (2017);  
 G. Shao et al., EPJC 78, 138 (2018) ; Z. Li et al., EPJC 79, 245 (2019).  
 A. Bzdak et al., Phys. Rep. 853, 1(2020). D. Mroczek et al, arXiv: 2008.04022.

Caveats : Non-equilibrium, finite size/time effects

M. Asakawa, M. Kitazawa, B. Müller, PRC 101, 034913 (2020).  
 S Mukherjee, R. Venugopalan, Y Yin, PRL 117, 222301 (2016).  
 S. Wu, Z. Wu, H. Song, PRC 99, 064902 (2019).

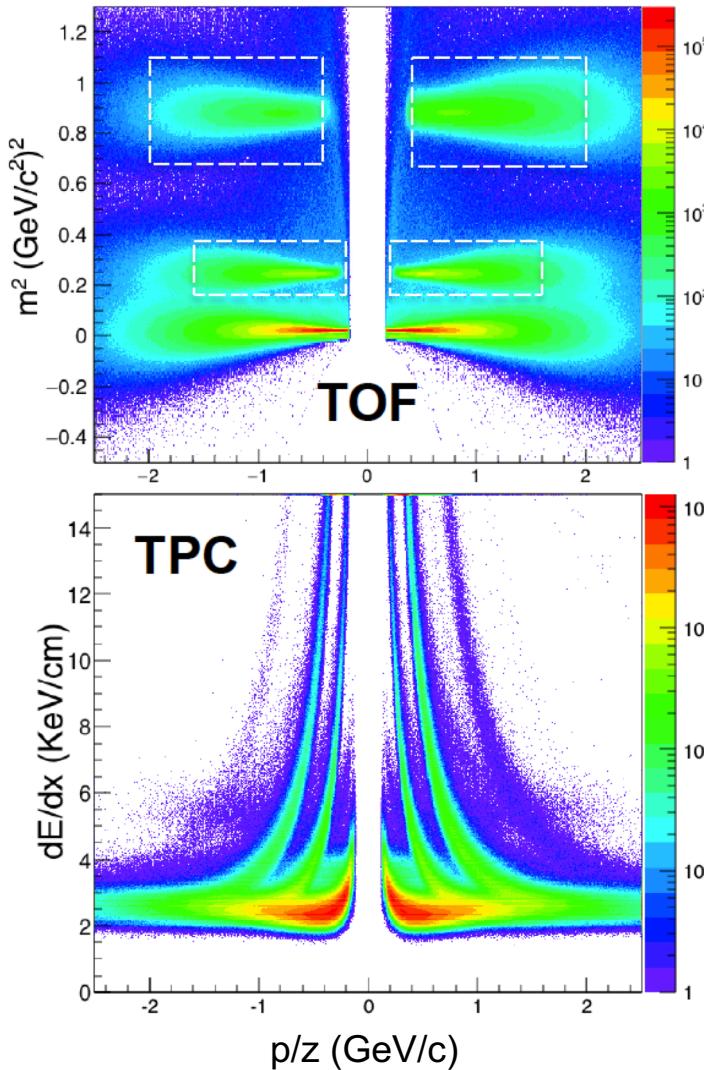


$\kappa\sigma^2 = 1$  (Poisson Fluctuations)

Characteristic signature of CP:  
Non-monotonic energy dependence

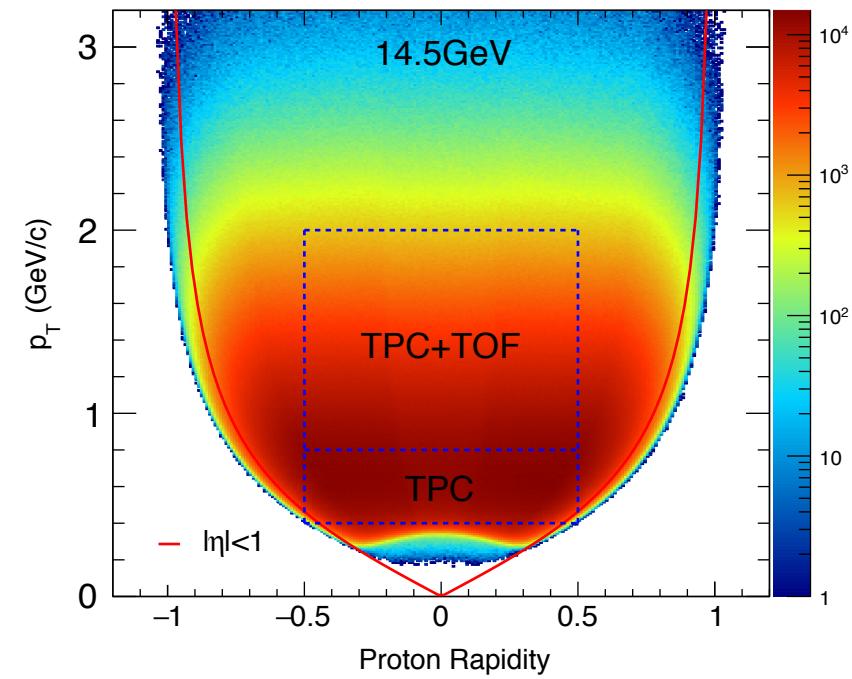
**“Oscillation Pattern”**  
**Especially the Peak at low energies**

# (Anti-) Proton PID and Acceptance



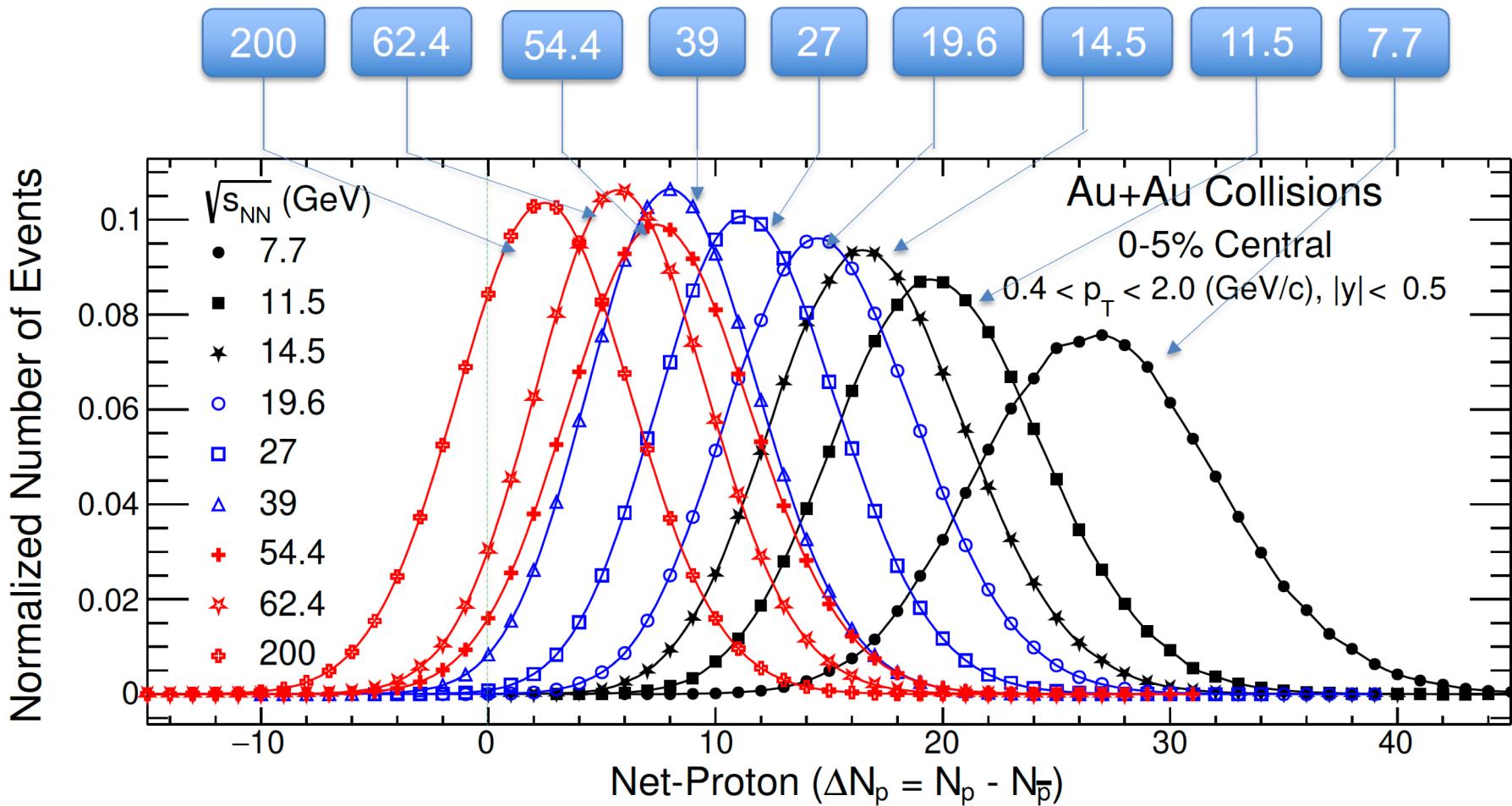
Extend the phase space coverage by TOF.  
Doubled the accepted number of proton/anti-proton

$|y| < 0.5$ ,  $0.4 < p_T (\text{GeV}/c) < 0.8$  (Low  $p_T$ , TPC PID)  
 $0.8 < p_T (\text{GeV}/c) < 2$  (High  $p_T$ , TPC+TOF PID)



- Purity of proton and anti-proton identification > 97%.

# Event-by-Event Net-Proton Distributions (0-5%)



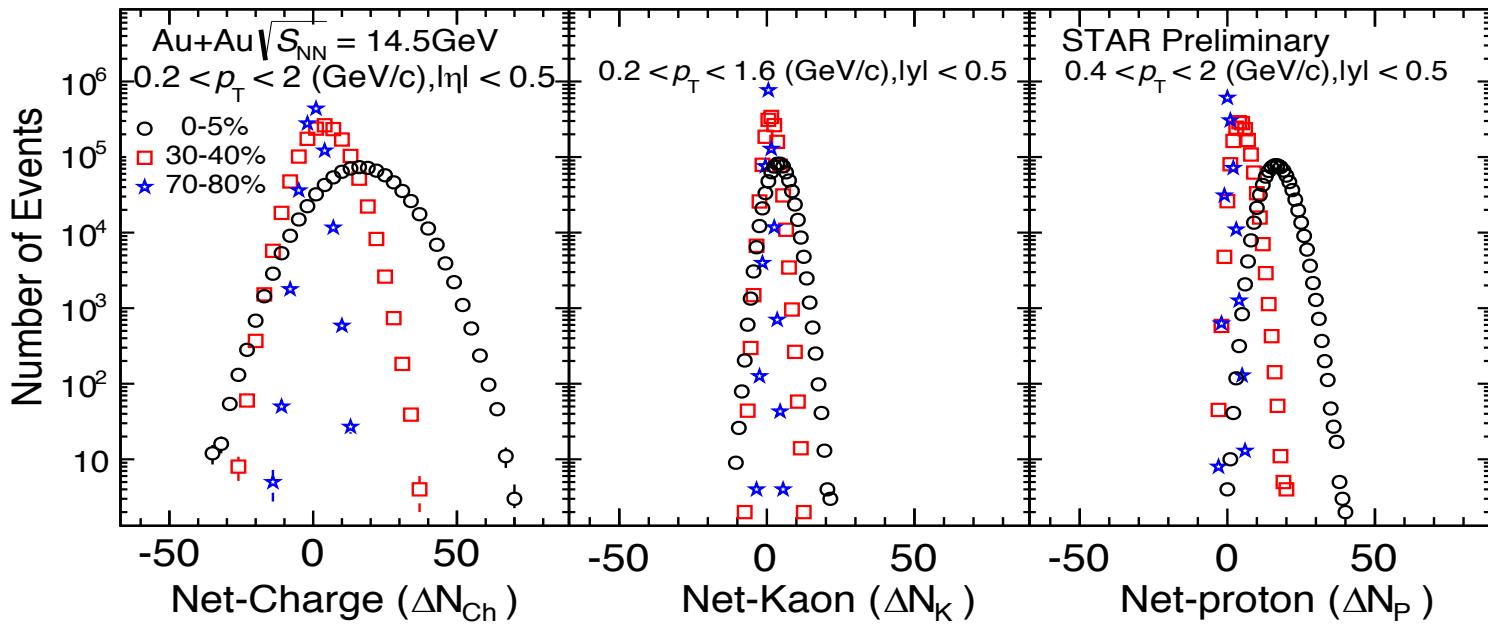
Efficiency uncorrected.

Mean values increase when decreasing energy:

Interplay between baryon stopping and pair production.

STAR, arXiv: 2001.02852

# Analysis Details

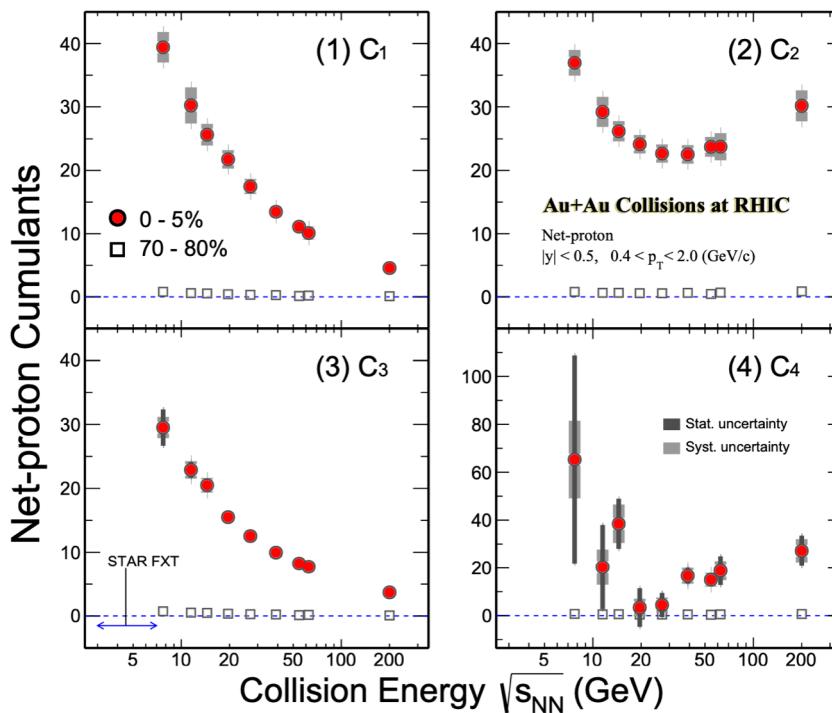


1. Statistical errors estimation : Delta theorem or bootstrap
2. Avoid auto-correlation effects: New centrality definition.
3. Suppress volume fluctuation: Centrality bin width correction (CBWC)
4. Detector efficiency correction : Binomial model

Review Article : X. Luo and N. Xu, Nucl. Sci. Tech. 28, 112 (2017).

X.Luo, J. Phys. G39, 025008 (2012); A. Bzdak and V. Koch, PRC86, 044904 (2012); X.Luo, et al. J. Phys. G40, 105104(2013); X.Luo, Phys. Rev. C 91, 034907 (2015); A . Bzdak and V. Koch, PRC91, 027901 (2015). T. Nonaka et al., PRC95, 064912 (2017). M. Kitazawa and X. Luo, PRC96, 024910 (2017). S. He, X. Luo, Chin. Phys. C43, 104001 (2018), X. Luo and T. Nonaka, PRC99, 044917 (2019); Arghya Chatterjee, et al. PRC 101,034902 (2020)

# Energy Dependence of Net-Proton Cumulant ( $C_1 - C_4$ )



Efficiency and CBWC corrections applied.

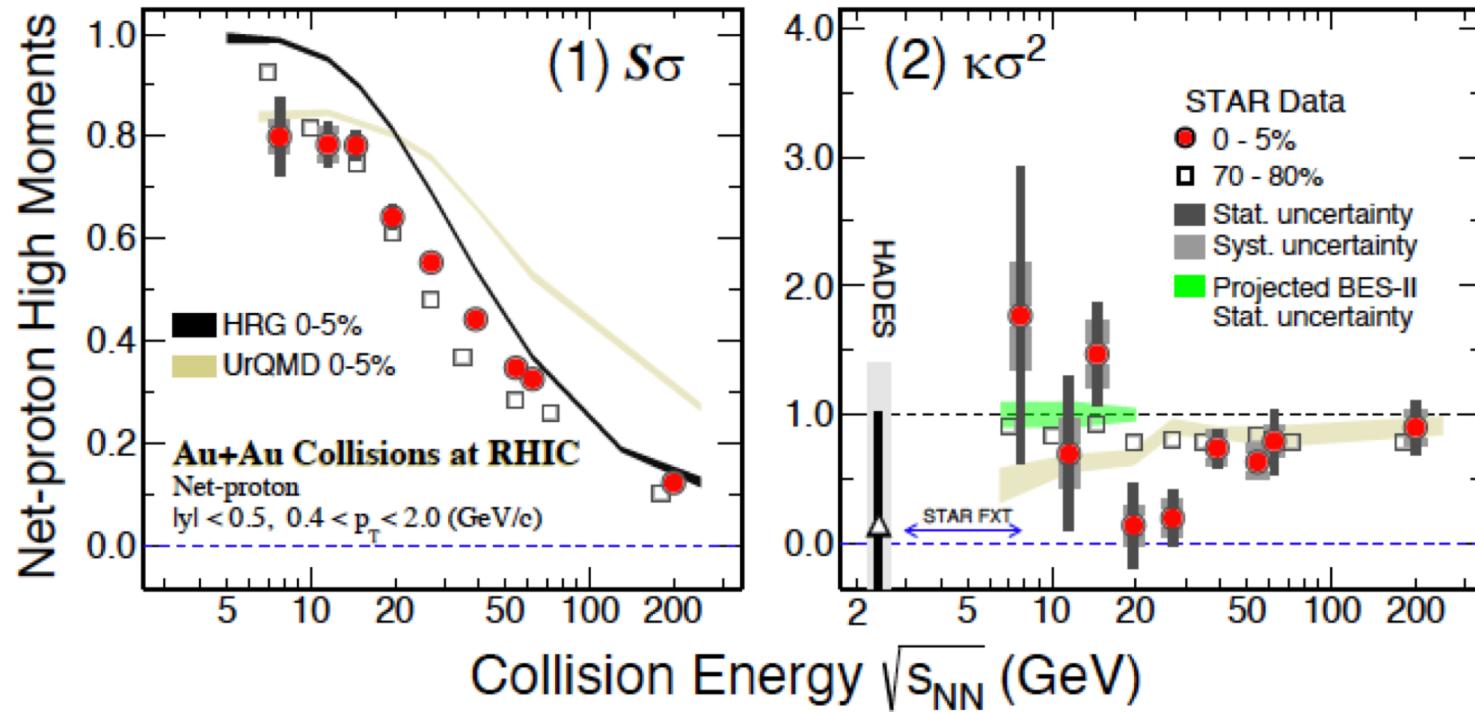
STAR: arXiv: 2001.02852 (short version)

A long paper is prepared and under review process within collaboration.

- 1) Net-p, proton and anti-proton cumulants
- 2) Correlation functions of protons and anti-protons
- 3) Energy, Centrality, acceptance dependence ( $p_T, y$ ).
- 4) Compare the data with various model results .

- Cumulants of net-proton distributions from 0-5% central and 70-80% peripheral collisions.
- Mean values increase when energy decreases due to baryon stopping.
- Cumulants can be decomposed into various order correlation functions, which will provide additional information for underlying physics.

# Energy Dependence of Cumulant Ratios : $S\sigma$ and $\kappa\sigma^2$



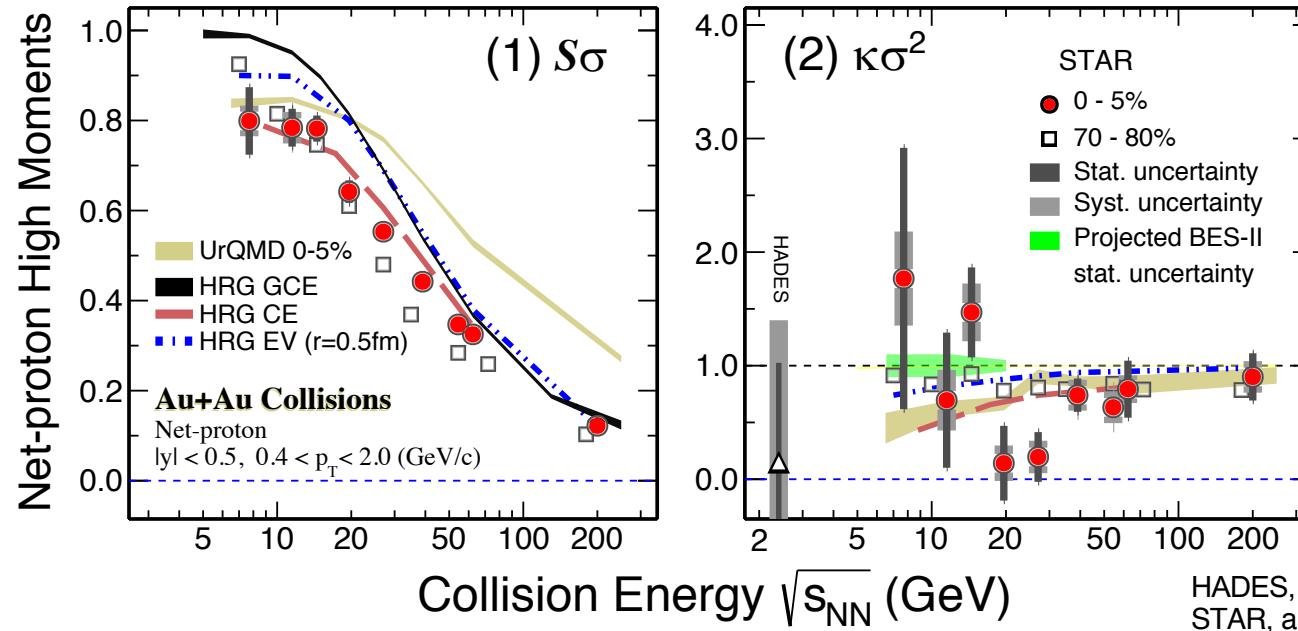
- HRG (GCE) and transport model predicted monotonical energy dependence. Suppression at low energy due to conservation.
- Observe a non-monotonic energy dependence (7.7-62.4 GeV) in 0-5% net-proton  $\kappa\sigma^2$  with a significant of  $3.1\sigma$

HADES, PRC 102, 024914 (2020)  
 STAR, arXiv: 2001.02852

Is there a peak structure below 20 GeV ?

Need precise measurement at STAR (BES-II), CBM, NICA etc.

# Comparison between model calculations and exp. data



- PBM et al. proposed the Canonical Ensemble (CE) for describing the system at high baryon density (baryon number conservation). Their calculations are consistent with transport model results.
- Excluded volume (EV) approach also leads to suppression at high baryon region.  
**'repulsive force' suppress the fluctuations.** 'Attractive' of protons at the 7.7 GeV collisions ?
- Goodness of the description between data and model results are evaluated with the  $p$  values obtained from  $\chi^2$  test.

PBM et al., arXiv: 2007.02463, S. He et al., PLB 762 296 (2016).

J.H. Fu, PLB 722, 144 (2013), A. Bhattacharyya et al., PRC 90, 034909(2014).

HRG+VDW: Vovchenko et al., PRC92,054901 (2015); PRL118,182301 (2017).

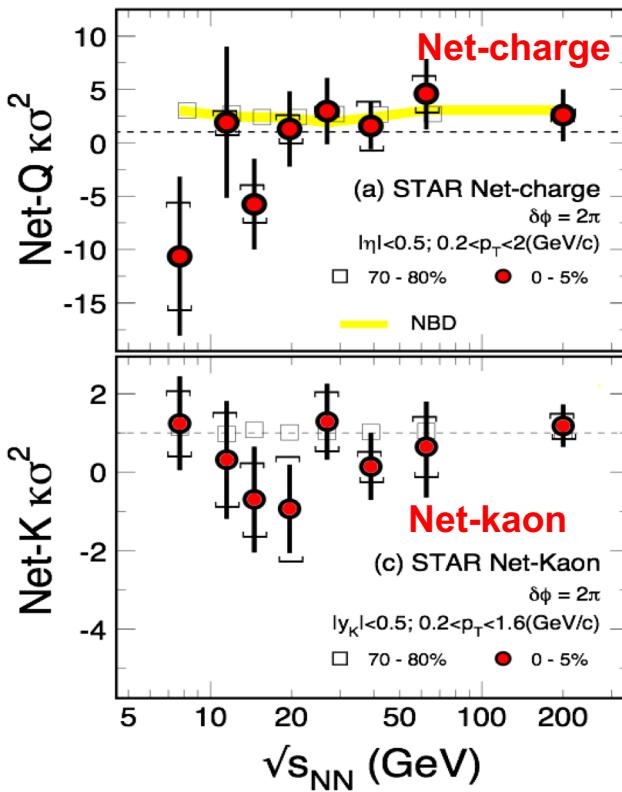
RMF: K. Fukushima, PRC91 044910 (2015)

$p$  values from  $\chi^2$  test below 27 GeV

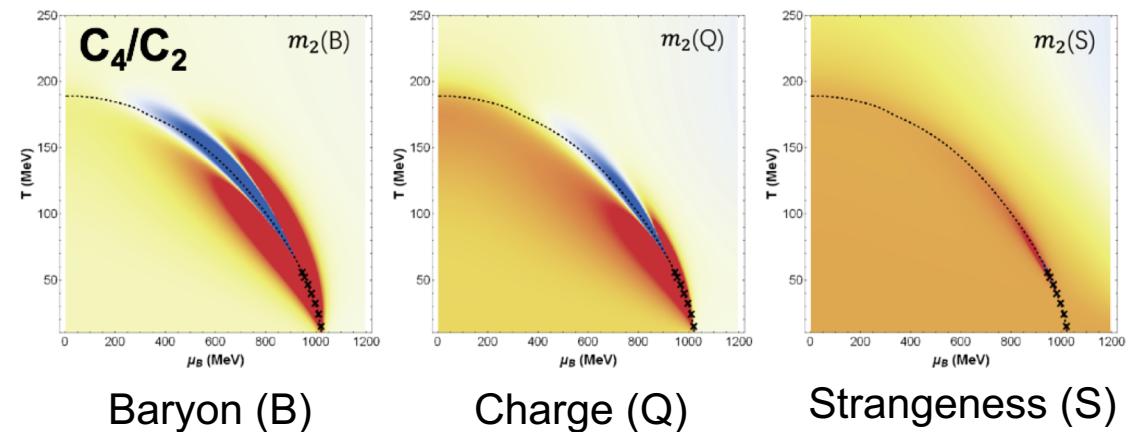
| Moments          | HRG GCE | HRG EV ( $r = 0.5 \text{ fm}$ ) | HRG CE | UrQMD   |
|------------------|---------|---------------------------------|--------|---------|
| $S\sigma$        | < 0.001 | < 0.001                         | 0.0754 | < 0.001 |
| $\kappa\sigma^2$ | 0.00553 | 0.0450                          | 0.0145 | 0.0221  |

# Net-charge and Net-kaon Fluctuations

## STAR Data



## NJL Model calculations



W. Fan, X. Luo, H.S. Zong, IJMPA 32, 1750061 (2017).

Critical signals: B>Q>S

(Due to the mass of strange quark is much larger than u,d quarks,  $m_s \gg m_{u,d}$ )

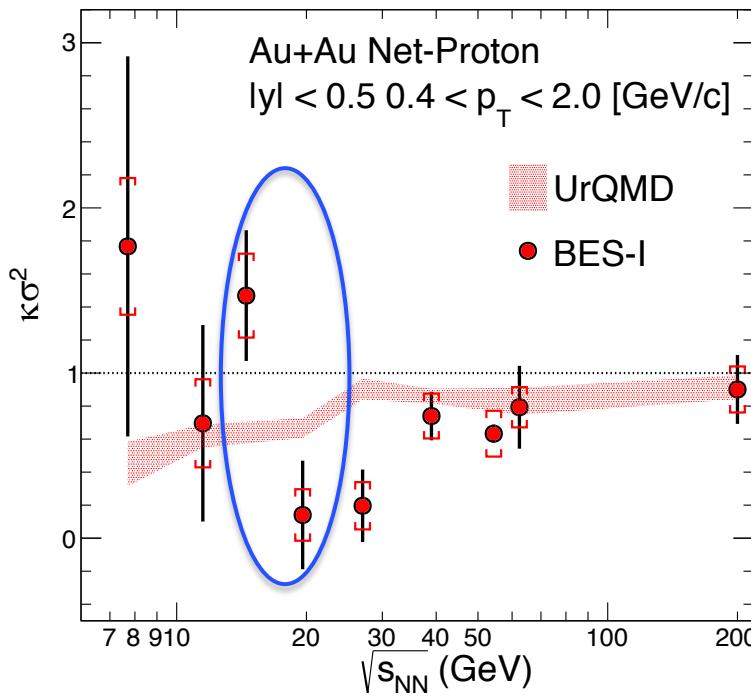
$$\text{error}(\kappa\sigma^2) \propto \frac{\sigma^2}{\varepsilon^2} \frac{1}{\sqrt{N_{\text{evts}}}}$$

STAR : Phys. Rev. Lett. 113 092301 (2014).

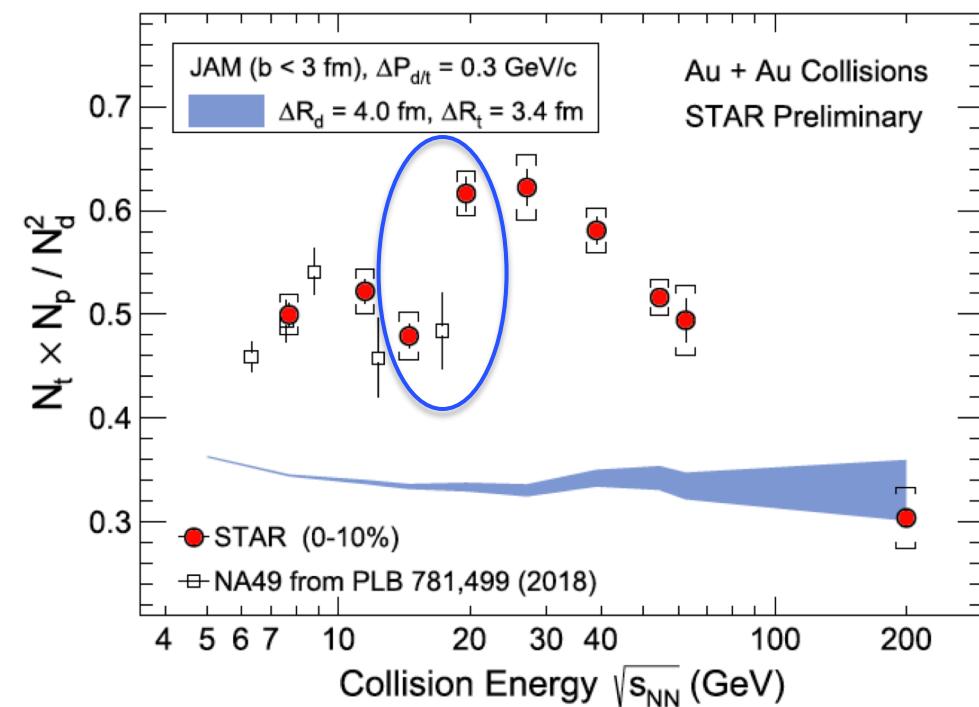
Phys. Lett. B 785, 551 (2018).

- 1) Within errors, the results of net-Q and net-Kaon show flat energy dependence.
- 2) More statistics are needed, especially at low energies (BES-II will help).

# Propose to take the data of Au+Au collisions at 17.1 GeV



STAR: arXiv: 2001.02852



Dingwei Zhang (STAR), QM2019 [arXiv: 2002.10677]

1. Value jumps between 19.6 and 14.5 GeV in both net-proton flu. and light nuclei yield ratio.
2. STAR has proposed to take a new energy point in 2021 (Run 21) : **17.1 GeV ( $\mu_B \sim 235$  MeV)** with  $\mu_B$  lie between 14.5 ( $\mu_B \sim 266$  MeV) and 19.6 GeV ( $\mu_B \sim 205$  MeV ).

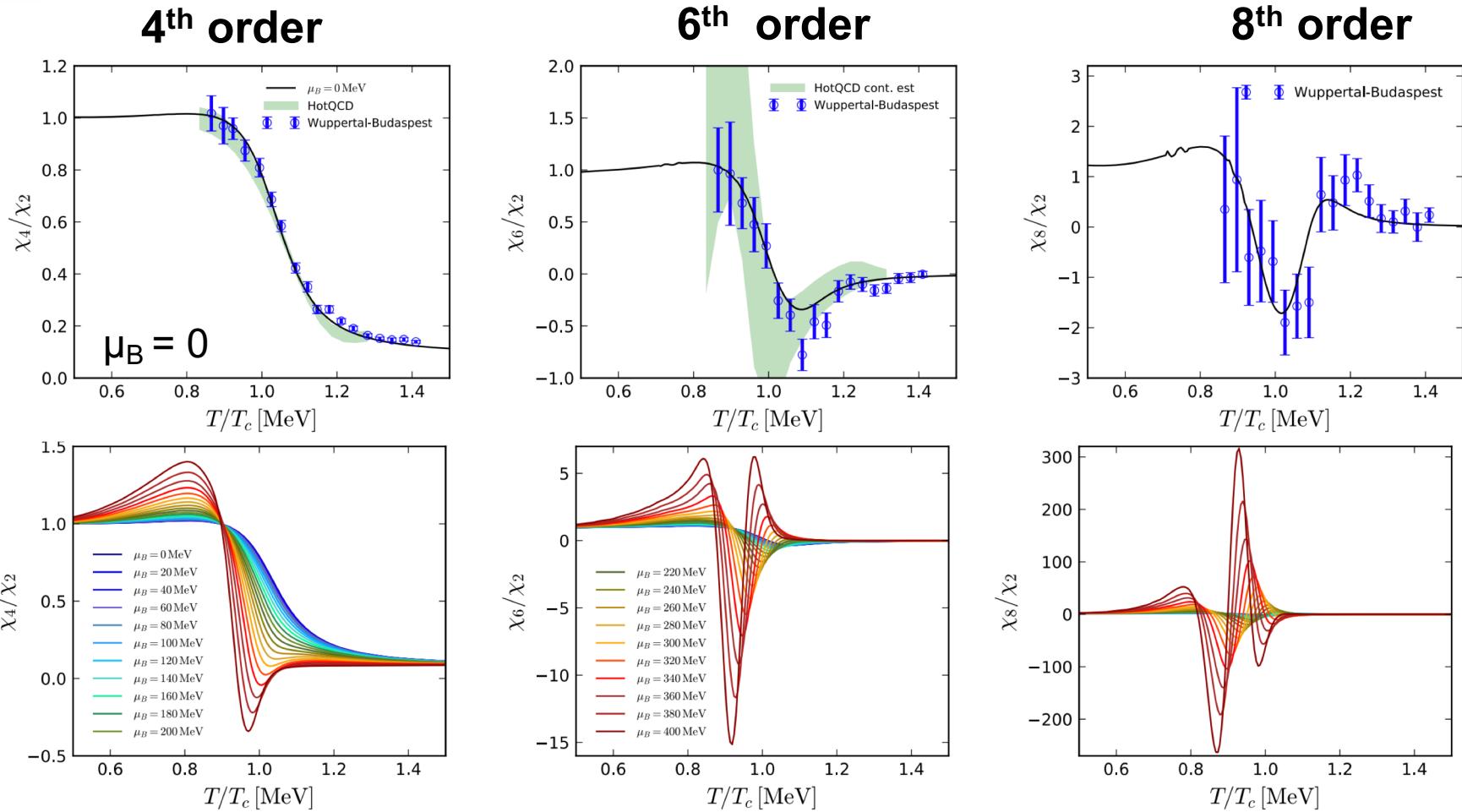
Model calculations trying to explain both observations :

Pre-cluster at chemical freeze-out due to attractive  $NN$  potential :

Edward Shuryak, Juan M. Torres-Rincon, PRC 100, 024903 (2019);  
 PRC 101, 034914 (2020); EPJA 56, 241 (2020).

Propose to take data of Au+Au 17.1 GeV in Run 21  
 : 2.5 Weeks with  $\sim 250$  million events.

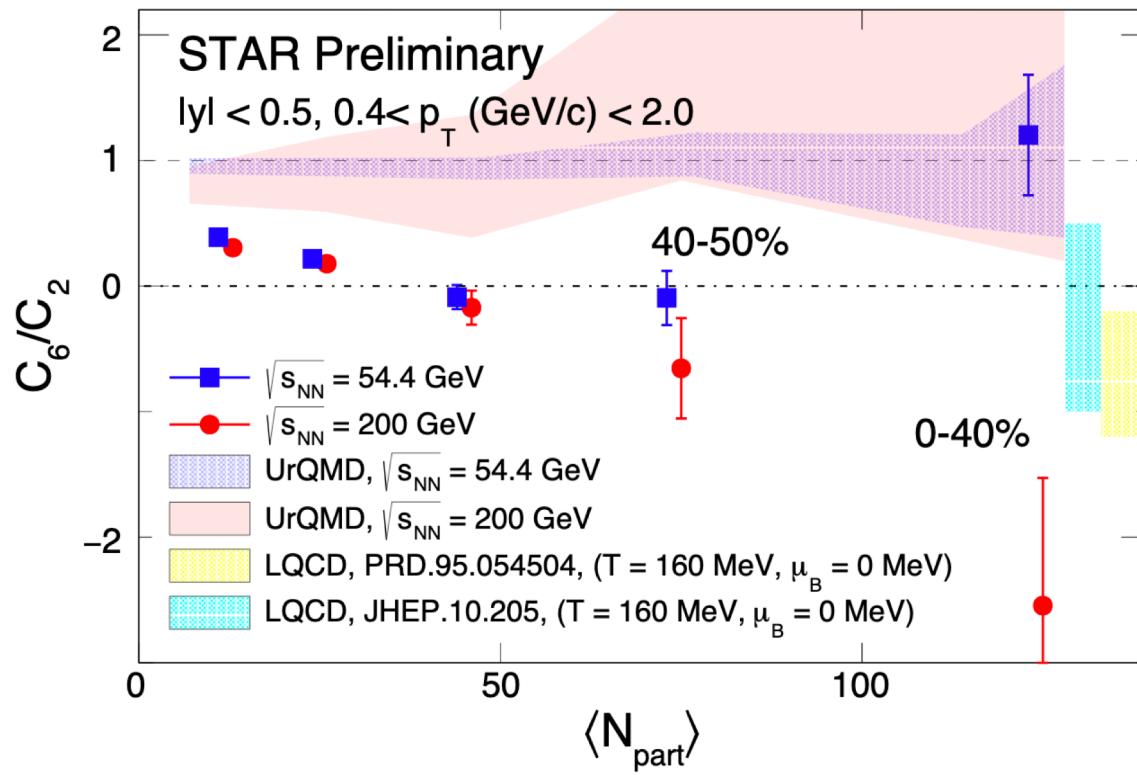
# Higher-order baryon number fluctuations: PQM+FRG Model



- Higher-order fluctuations are more sensitive to QCD phase transition.
- At  $\mu_B = 0$ ,  $C_6 \sim 0$  or negative, and  $C_8$  become negative when chemical freeze-out temperature close to  $T_c$ .
- > could serve as experimental evidence of chiral crossover.

Wei-jie Fu et al., In preparation.

# Net-proton C<sub>6</sub> measurement



$$\text{error}(C_n/C_2) \propto \frac{\sigma^{n-2}}{\sqrt{N} \varepsilon^\alpha}$$

- Results from three energies are consistent in peripheral collisions.
- $C_6/C_2 > 0$  at 54.4 GeV and  $C_6/C_2 < 0$  at 200 GeV in 0-40% central collisions.

Ashish and Toshihiro, QM2019

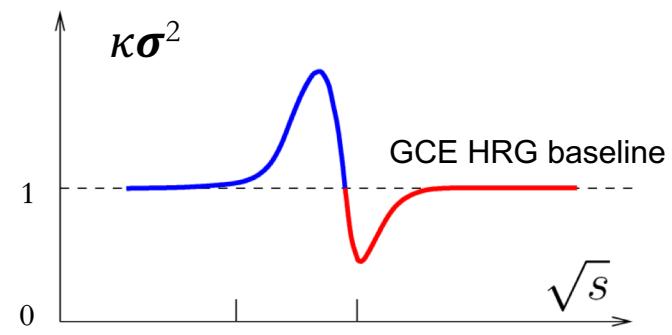
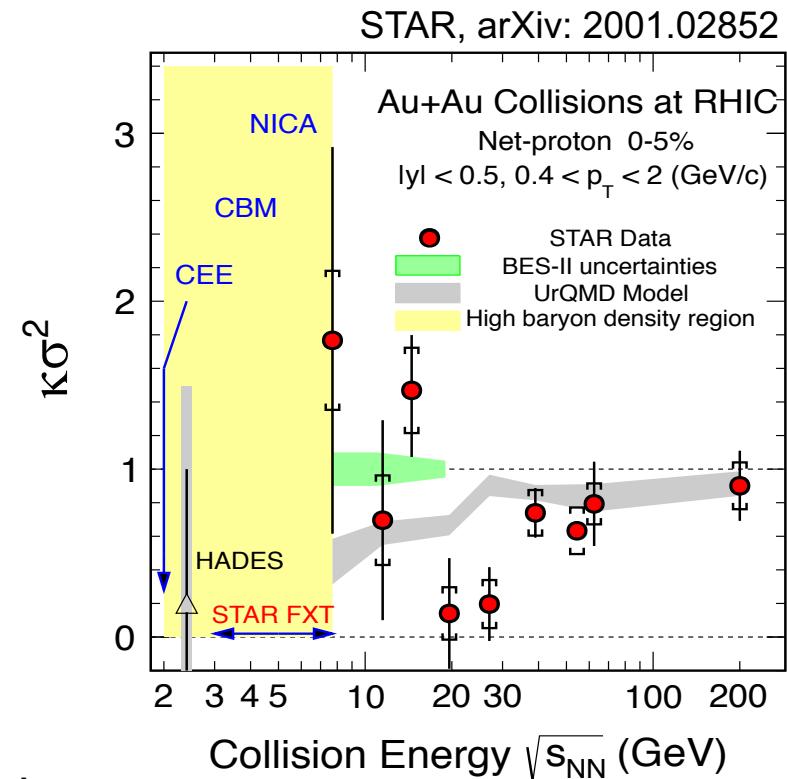
# BES-II at RHIC (2019-2021)

| $\sqrt{s_{NN}}$<br>(GeV) | Events<br>( $10^6$ ) | BES II / BES I  |
|--------------------------|----------------------|-----------------|
| 19.6                     | 538                  | 2019 / 2011     |
| 14.6                     | 325                  | 2019 / 2014     |
| 11.5                     | 230                  | 2020 / 2010     |
| 9.2                      | 160                  | 2020 / 2008     |
| 7.7                      | 100                  | 2021 / 2010     |
| 17.1                     | 250                  | 2021 (proposed) |

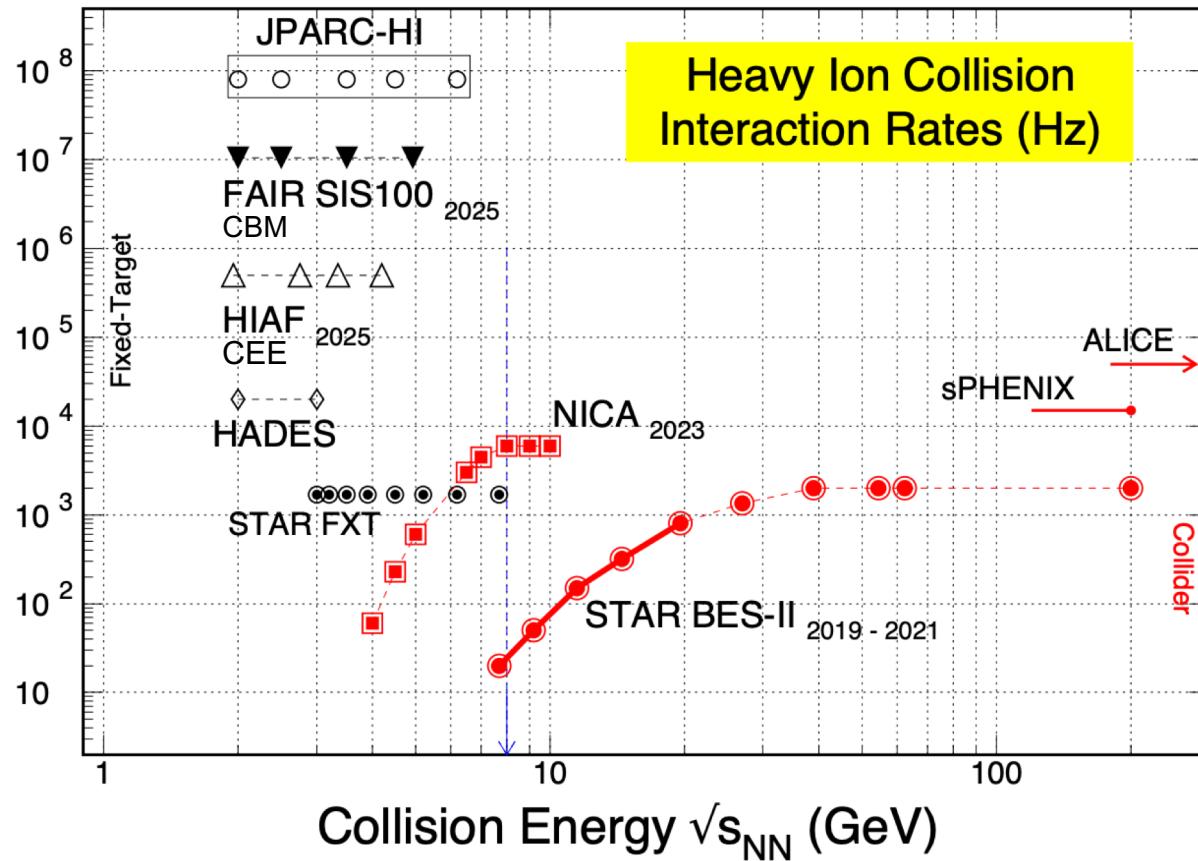
- BES-II: 10-20 times higher statistics than BES-I.
- FIX-target mode :  $\sqrt{s_{NN}} = 3\text{-}7.7 \text{ GeV}$  (2018-2021).

iTPC, ETOF, EPD upgrade completed.

- Enlarge Acceptance :  $\eta$  coverage from 1.0 to 1.5
- Improve dE/dx and forward PID
- Improve centrality/event plane determination



# Future Facilities for Heavy-Ion Collisions



X. Luo, N. Xu, Nucl. Sci. Tech. 28, 112 (2017).

X. Luo, S. Shi, N. Xu and Y. Zhang, Particle 3, 278 (2020)

A. Bzdak, S. Esumi, V. Koch, J. Liao, M. Stephanov, N. Xu Phys. Rep. 853, 1 (2020).

K. Fukushima, B. Mohanty, N. Xu, arXiv: 2009. 03006

## Exploring the QCD phase structure at high baryon density region



# Summary and Outlook

Higher moments of conserved quantities and light nuclei production are sensitive observables of CP ( large density fluctuations and long range correlations)

- Yield ratio of light nuclei and fourth order net-proton fluctuations ( $C_4/C_2$ ) in central Au+Au collisions shows non-monotonic energy dependence, which could serve as important experimental basis for critical point search.
- $C_6$  and  $C_8$  can be used to probe the chiral crossover at  $\mu_B=0$ . Large statistics are needed to conduct precise measurements.
- Need to study the background/non-equilibrium contributions carefully and build-up dynamical modeling of heavy-ion collisions with critical fluctuations.
- Explore the QCD phase structure at **high baryon density** with **high precision**:
  - (1) RHIC BES-II : Collider ( $\sqrt{s_{NN}} = 7.7 - 19.6$  GeV) and FXT ( $\sqrt{s_{NN}} = 3 - 7.7$  GeV) mode.
  - (2) Future Facilities ( $\sqrt{s_{NN}} = 2 - 11$  GeV) : FAIR/CBM, NICA/MPD, HIAF/CEE, JPARC-HI.



## Acknowledgements :

*Thanks to the members of the STAR Collaboration  
and the kind invitation from the organizers.*

***Thank you for your attention !!***



# BES-I & II at RHIC (2010-2017, 2019-2021)

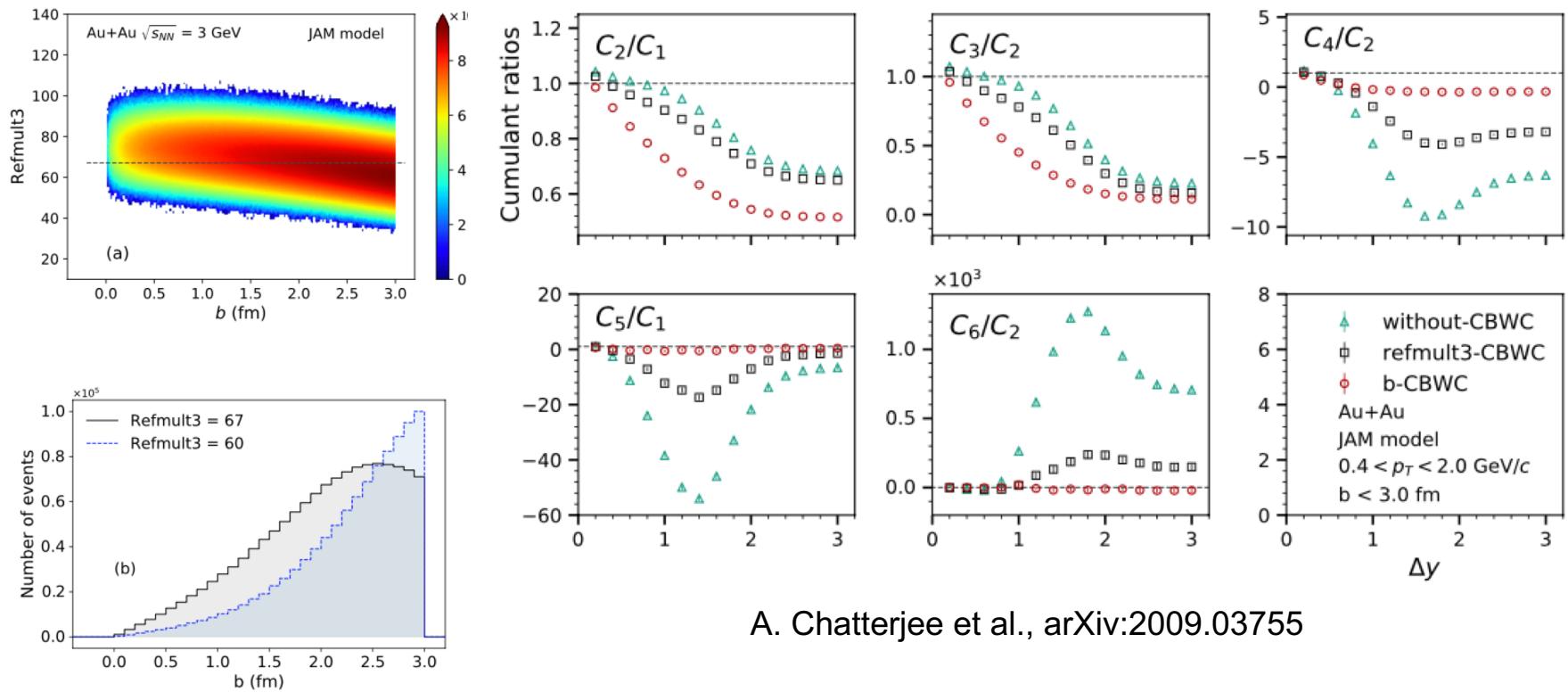
| Collider mode            |                      | Au+Au Collisions |                  | FXT mode          |  |
|--------------------------|----------------------|------------------|------------------|-------------------|--|
| $\sqrt{s_{NN}}$<br>(GeV) | Events<br>( $10^6$ ) | BES II / BES I   | $\mu_B$<br>(MeV) | $T_{ch}$<br>(MeV) |  |
| 200                      | 238                  | 2010             | 25               | 166               |  |
| 62.4                     | 46                   | 2010             | 73               | 165               |  |
| 54.4                     | 1200                 | 2017             | 83               | 165               |  |
| 39                       | 86                   | 2010             | 112              | 164               |  |
| 27                       | 30 (560)             | 2011/2018        | 156              | 162               |  |
| 19.6                     | 538 / 15             | 2019/2011        | 206              | 160               |  |
| 14.5                     | 325 / 13             | 2019/2014        | 264              | 156               |  |
| 11.5                     | 230 / 7              | 2020/2010        | 315              | 152               |  |
| 9.2                      | 160 / 0.3            | 2020/2008        | 355              | 140               |  |
| 7.7                      | 100 / 3              | 2021/2010        | 420              | 140               |  |
| 17.1*                    | 250                  | 2021             | 230              | 158               |  |

$T_{ch}$  and  $\mu_B$  from J. Cleymans et al. PRC73, 034905 (2006)  
 \*New Proposed Energy in Beam User Request 2020/2021.

## BES-II Program:

- Precisely map the QCD phase diagram  $200 < \mu_B < 420$  MeV
- The FXT program extends  $\mu_B$  coverage up to 720 MeV (3 GeV)

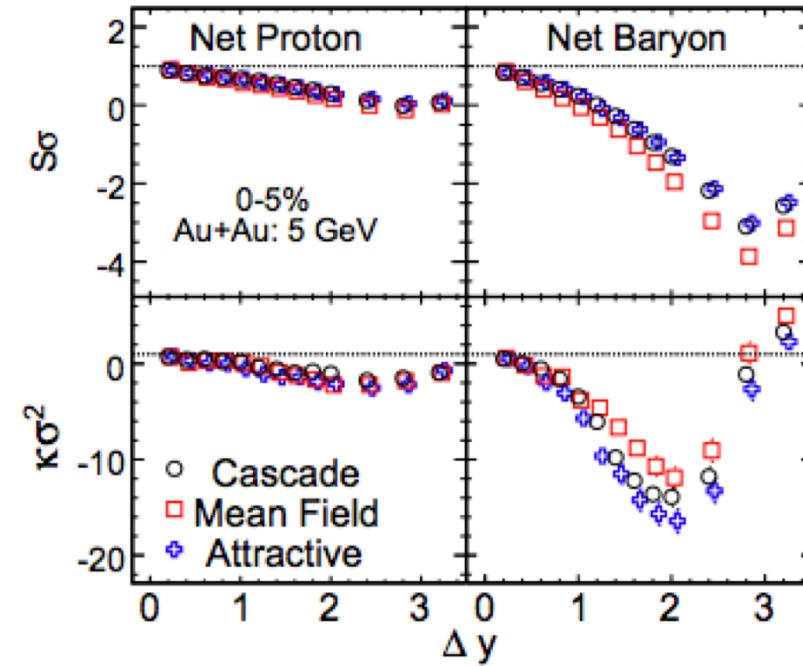
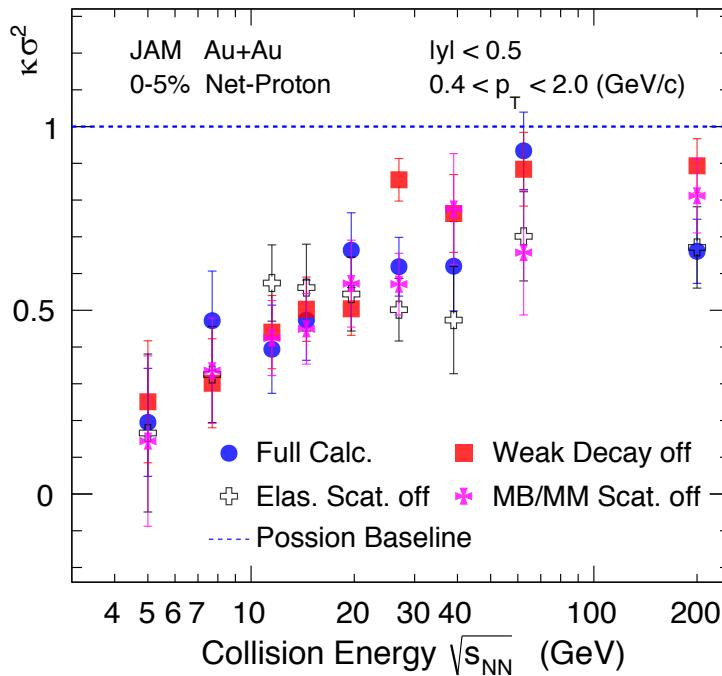
# Centrality determination at lower energies



- At low energies, centrality resolution obtained from charge particle multiplicities is very poor and CBWC is not efficient.
- New methods, such as machine learning technique could be helpful.  
F. P. Li et al., J. Phys. G 47, 115104 (2020). M. O. Kuttan et al., arXiv : 2009.01584
- Volume fluctuations corrections ?

T. Sugiura et al., Phys. Rev. C 100, (2019) 044904; Braun-Munzinger et al., Nucl. Phys. A 960 (2017)114-130  
 Skokov et al., Phys. Rev. C88 (2013) 034911; HADES, PRC 102, 024914 (2020)

# Non-critical contributions: transport model studies



UrQMD, JAM, AMPT : Dominated by baryon number conservations at low energies

- Effects of weak decay and hadronic scattering are not significant within uncertainties.
- No significant effects observed for mean field potential and attractive scattering (to simulate softening of EOS )

Z. Feckova, et al., PRC92, 064908(2015); J. Xu, et. al., PRC94, 024901(2016); X. Luo et al., NPA931, 808(14), P.K. Netrakanti et al., NPA947, 248(2016), P. Garg et al. PLB 726, 691(2013). S. He, et. al., PLB762, 296 (2016); PLB 774, 623 (2017).

J. Li et al, PRC 97,014902 (2018). H. J. Xu, PLB 765, 188 (2017); Y. X. Ye et al., PRC 98, 054620 (2018). C. Zhou, et al., PRC 96, 014909 (2017). Y. Zhang, et al. PRC101, 034909 (2020). L. Jiang et al., PRC94, 024918 (2016); M. Bluhm, EPJC77, 210 (2017).